Higgs-Unparticle Interplay Antonio Delgado University of Notre Dame

- Motivation: What are the unparticles?
- Higgs-unparticle interaction: curing the IR divergence
- Pole structure & spectral analysis
- Decays?
- (Un)Conclusions

Work done in collaboration with: J.R. Espinosa, J.M. No and M. Quirós: JHEP 0710:094,2007 JHEP 0804:028,2008 arXiv 0804:4574 [hep-ph]

Motivation

• The Higgs boson can act as a portal to a hiddensector of the SM (Schabinger, Wells; Patt, Wilczek)



- Higgs physics is yet to be explored therefore there are very few constrains
- The Higgs forms the smallest dimension singlet operator: $|H|^2$

 $\kappa |H|^2 \mathcal{O}$

- Then we have different scenarios depending on the nature of O:
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 - Hidden-valleys
 - Unparticles

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What is an unparticle?

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- In general, a conformal theory, is one where there is exact scale invariance (apart from more technical aspects...)
- The first consequence is that on a conformal theory there are no masses!!!

- Coupling the SM directly to this conformal sector goes at follows:
 - First we can imagine the following "normal" coupling between the SM and a hidden sector of dimension d

$$\frac{1}{M^k}O_{SM}O_{hid} \quad O_{hid} \equiv q\overline{q}, \lambda\lambda, \dots \ \mathbf{k}=\mathbf{d}_{sm}+\mathbf{d}$$

 Then we will suppose that the new sector, through RGE evolution, will reach an IR conformal fixed point

$$\frac{\Lambda^{d-d_U}}{M^k} O_{SM} \mathcal{O}_U$$

There is a change on dimensions!!

- Through this flow, the dynamics of the hidden sector are such that the operator acquires a big anomalous dimension
- The theory is describe not in terms of particles but in terms of operators like the one coupling to the SM
- Because there is conformal symmetry in the theory some correlation functions are exactly known:

$$< \mathcal{O}_U(x)\mathcal{O}_U(y) > \sim \frac{1}{|x-y|^{2d_U}}$$

$$P_U(p^2) = \frac{A_{d_U}}{2\sin(\pi d_U)} \frac{i}{(-p^2 - i\epsilon)^{2-d_U}}$$

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Higgs-unparticle interaction

 I will focus in the case where Ou is a scalar unparticle operator with I <d<2 and with the following scalar potential:

$$V_0 = m^2 |H|^2 + \lambda |H|^4 + \kappa_U |H|^2 \mathcal{O}_U$$

• As shown in the previous slides, the Ou has the following correlator:

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$$\langle \mathcal{O}\mathcal{O} \rangle \xrightarrow{\Delta \to 0} \quad \langle \mathcal{O}_U \mathcal{O}_U \rangle$$

• The potential now reads:

$$V = m^{2}|H|^{2} + \lambda|H|^{4} + \frac{1}{2}\sum_{n} M_{n}^{2}\varphi_{n}^{2} + \kappa_{U}|H|^{2}\sum_{n} F_{n}\varphi_{n}$$

 Imposing that EWSB is broken gives the following vev's for the deconstructed fields:

$$v_n \equiv \langle \varphi_n \rangle = -\frac{\kappa_U v^2}{2M_n^2} F_n$$

• And in the continuous limit gives an IR divergence:

$$\langle \mathcal{O}_U \rangle = -\frac{\kappa_U v^2}{2} \int_0^\infty \frac{F^2(M^2)}{M^2} dM^2$$

 $F^2(M^2) = \frac{A_{d_U}}{2\pi} (M^2)^{d_U - 2}$

 One way of solving this IR problem is to include the following new term in the potential:

$$\delta V = \zeta |H|^2 \sum_n \varphi_n^2$$

• Which in turn generates the following finite vev for the unparticle operator (note the mass gap)

$$\langle \mathcal{O}_U \rangle = -\frac{\kappa_U v^2}{2} \int_0^\infty \frac{F^2(M^2)}{M^2 + \zeta v^2} \ dM^2$$

• It is interesting to point out that EWSB exists even when the origin is a minimum $m^2 > 0$

$$\lambda = -\frac{m^2}{v^2} + \frac{d_U}{8\pi} A_{d_U} \zeta^{d_U - 2} \Gamma(d_u - 1) \Gamma(2 - d_U) \kappa_U^2 v^{2d_U - 4}$$

Pole structure & Spectral analysis

 Once the true vacuum is found the spectrum is obtained diagonalizing the infinite matrix that mixes h and φ_n:

$$M_{hh}^2 = 2\lambda v^2 \equiv m_{h0}^2$$

$$M_{hn}^2 = \kappa_U v F_n \frac{M_n^2}{M_n^2 + m_g^2} \qquad m_g^2 \equiv \zeta v^2$$

$$M_{nm}^2 = (M_n^2 + m_g^2)\delta_{nm}$$

• The inverse of the hh entry corresponds to the propagator of the higgs in the interaction basis:

$$iP_{hh}(p^2)^{-1} = p^2 - m_{h0}^2 + \frac{v^2 \kappa_U^2 A_{d_U}}{2\pi p^4} \Gamma(d_U - 1) \Gamma(2 - d_U) \\ \times \left[\left(m_g^2 - p^2 \right)^{d_U} + d_U p^2 (m_g^2)^{d_U - 1} - (m_g^2)^{d_U} \right]$$

Parameter space The Higgs can be embedded in the continuum!!! $d_{\rm U} = 1.2$ 10 8 $R_U \equiv \frac{A_{d_U} v^2 \kappa_U^2}{2\pi m_{\tilde{c}}^{6-2d_U}}$ Ia 6 IIa \mathbf{x}_{0} IIb Δ $x_0 \equiv \frac{m_{h0}^2}{m_{\gamma}^2}$ Tachyon 2 Ib

Ia. Single (complex) pole>mg Ib. Single (real) pole<mg IIa. Two (complex) poles>mg IIb. One (complex)>mg One (real)<mg</p>

 $R_{\rm U}$

10

0

















The effect occurs for every x₀>1 for x₀<1 there is always an isolated pole

Spectral analysis

• We can try to capture better the structure of our propagator calculating the spectral function

$$\rho_{hh}(s) = -\frac{1}{\pi} Im[-iP_{hh}(s+i\epsilon)]$$

• There are two pieces of the imaginary part of the propagator

• isolated poles:
$$\frac{1}{x+i\epsilon} \to P.V.\frac{1}{x} - i\pi\delta(x)$$

•
$$(m_g^2 - p^2)^{d_U} = (p^2 - m_g^2)^{d_u} (\cos(d_u \pi) + i \sin(d_u \pi)) \ p > m_g$$

• There are two forms for the spectral function depending on whether there is an isolated pole:

$$\rho_{hh}(s) = \frac{1}{K^2(m_h^2)} \delta(s - m_h^2) + \theta(s - m_g^2) \frac{T_U(s)}{\mathcal{D}^2(s) + \pi^2 T_U^2(s)}$$
$$\rho_{hh}(s) = \theta(s - m_g^2) \frac{T_U(s)}{\mathcal{D}^2(s) + \pi^2 T_U^2(s)}$$

 The spectral function is normalized to I and can be interpreted as the projection of mass eigenstates (H,U) into the higgs interaction state (h)

$$\int_0^\infty \rho_{hh}(s)ds = 1$$

 $\rho_{hh}(s) \equiv \langle h|s\rangle \langle s|h\rangle = |\langle H|h\rangle|^2 \delta(s-m_h^2) + \theta(s-m_g^2)|\langle U, M|h\rangle|^2$

These are two examples of spectral functions for $d_u=1.2$ one with an isolate pole the second with the higgs embedded in the continuum it is a broad resonance

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Note the mass gap

• Evolution of the pole for large R_{\cup} and appearance of the phantom higgs

 Projection onto the higgs interaction state of the isolated pole for different masses x=m_h²/m_g² it can be very diluted!!!

Decays?

- In the example I have been discussing until now where the higgs mixes with an unparticle operator there are decays but can be explained by the normal decays of the higgs
- I would like to study the case where the unparticles do not mixed but can decay
- Let's start with the following (toy)-lagrangian:

$$\mathcal{L} = \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi - \frac{1}{2} m_0^2 \phi^2 - \frac{1}{2} \kappa_u \phi^2 \mathcal{O}_U$$

 In order to avoid any problems with a tadpole for the unparticle operator, the following correlator will be supposed:

$$-iP^{(0)}(s) = \frac{1}{D^{(0)}} = \frac{A_d}{2\sin(\pi d)} \frac{1}{(-s+m_g^2-i\epsilon)^{2-d}}$$

• On the other hand I will suppose that the field ϕ will have m>0

• There is a one loop contribution to the 2point function of the unparticles that can be resumed in the following way:

$$-iP^{(1)} = \frac{1}{D^{(0)} + \Sigma}$$

$$\Sigma \simeq \frac{\kappa_u^2}{32\pi^2} \log \frac{\Lambda_U}{m^2} + i \frac{\kappa_u^2}{32\pi} \sqrt{1 - \frac{4m^2}{s}} \theta(s - 4m^2)$$

- The consequences of that polarization are as follows:
 - A new isolated pole appears with a mass less than mg
 - If $m_g > 2$ m this poles gets an imaginary part proportional to the polarization
- Therefore unparticles can decay!!!





d_u=1.25 K measures the normalization of the pole





 $k_u=5 m_g=4m$



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- A mass gap is generated for the unparticles, the higgs can appear as an isolated pole, be merged into the continuum or phantom (diluted) higgs can be obtained
- Unparticles can decay as resonances