

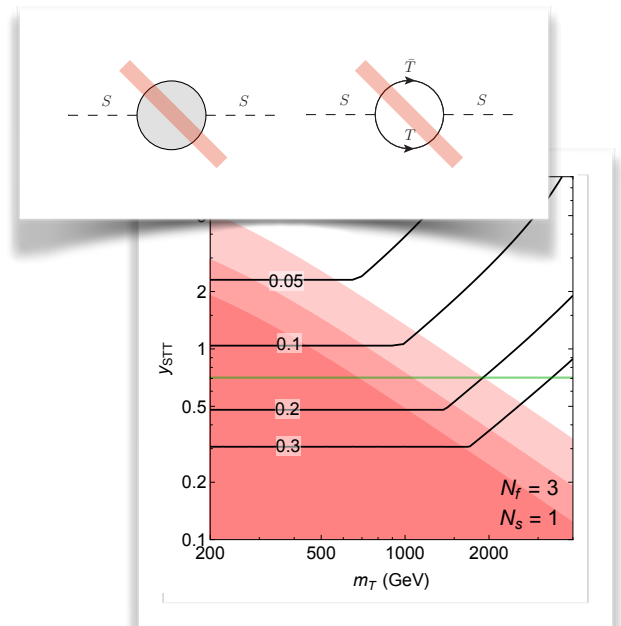
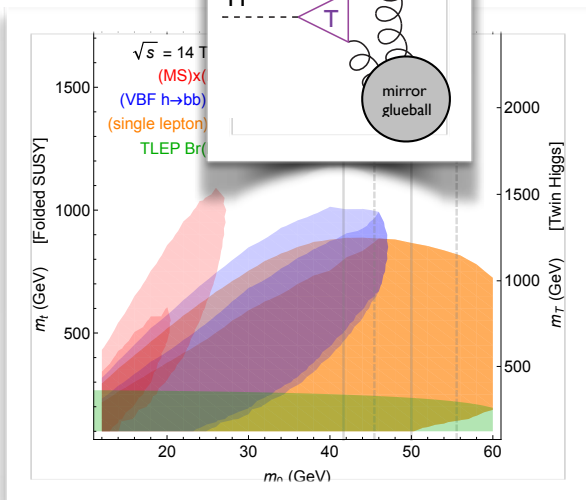
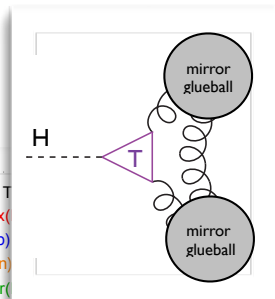
# Discovering Neutral Naturalness

Theory Seminar  
NHETC  
Rutgers University

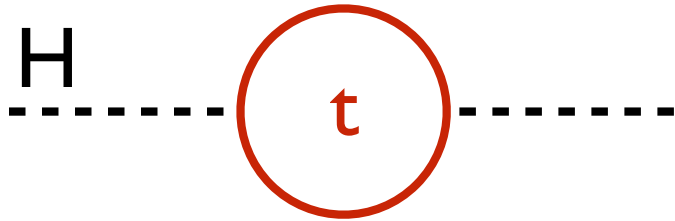
20. October 2015

David Curtin  
University of Maryland

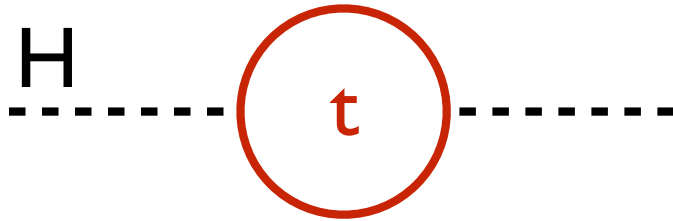
based on  
DC, Verhaaren 1506.06141  
DC, Saraswat 1509.04284  
Chacko, DC, Verhaaren, 1512.XXXXXX



# The Hierarchy Problem



# The Hierarchy Problem



... can be solved by top partners

# The Hierarchy Problem



... can be solved by top partners

top quark  $t$   $\xrightarrow{\text{continuous symmetry}}$

top partner  $T$

carries  
color charge

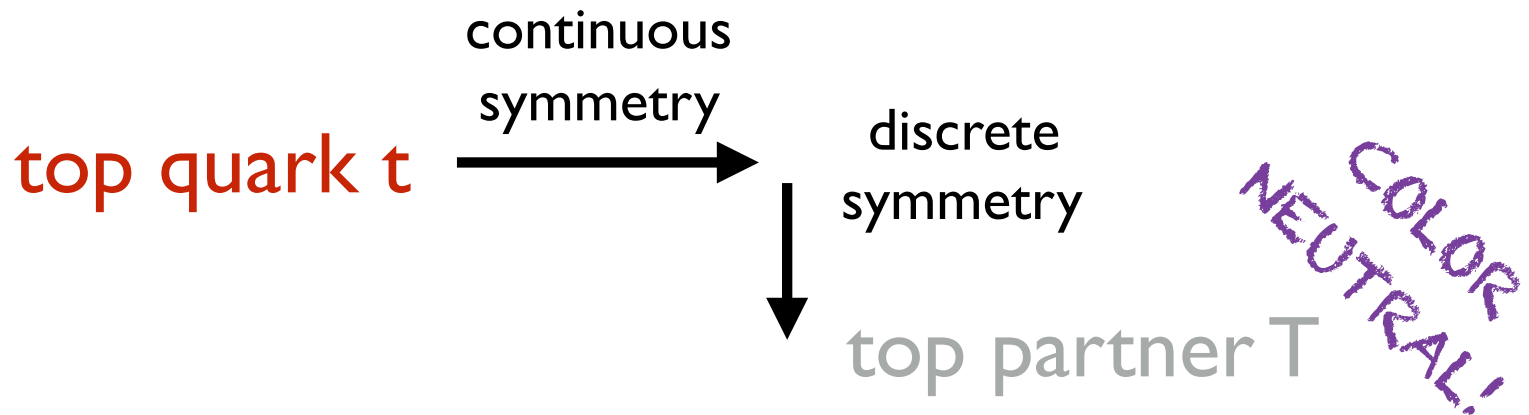
e.g.

*Supersymmetry, modern composite Higgs models, etc...*

# The Hierarchy Problem



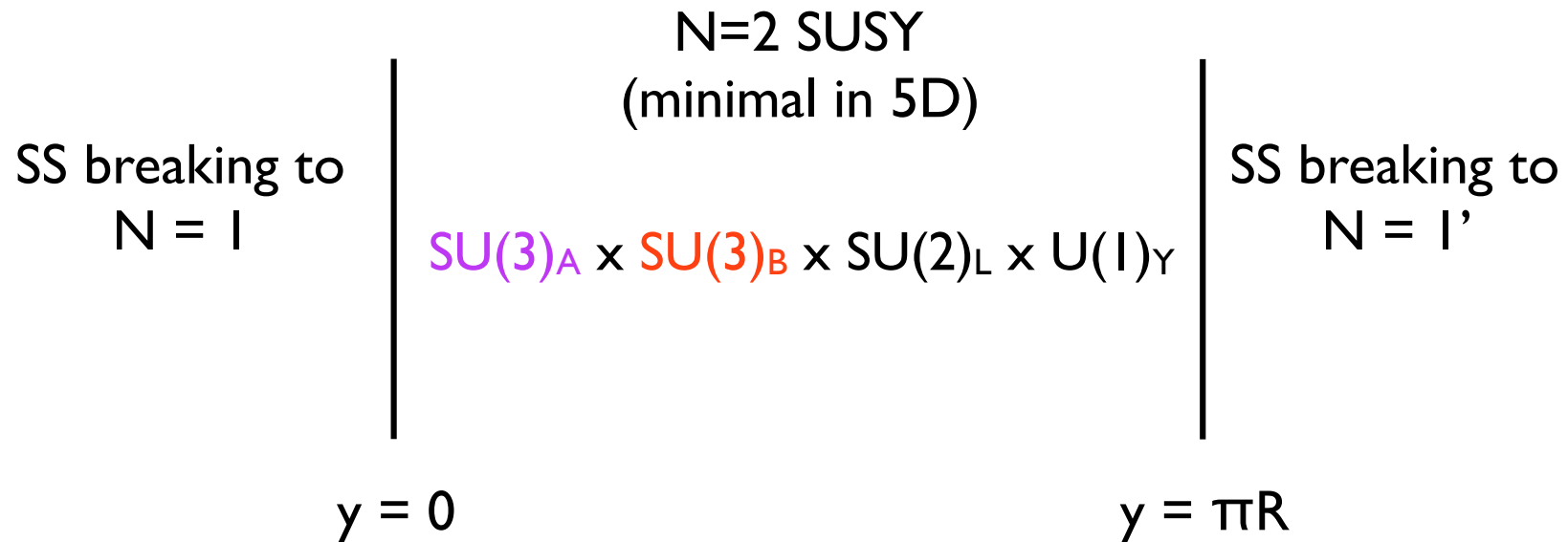
The symmetry need not commute with SM color!



e.g.

*Folded SUSY (EW-charged stops), Twin Higgs (SM singlet T-partners)*

# Theory Example: Folded SUSY



Boundary conditions break  $A \leftrightarrow B$  symmetry and globally break N=2 to N=0 SUSY.

Normal MSSM EW sector.

SU(3) sectors: only zero modes are A-fermions, B-sfermions.

'Accidental supersymmetry' protects Higgs @ 1-loop with EW charged top partners.

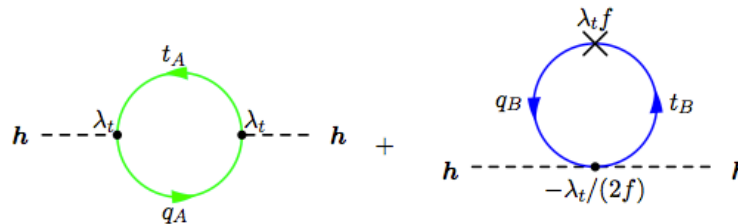
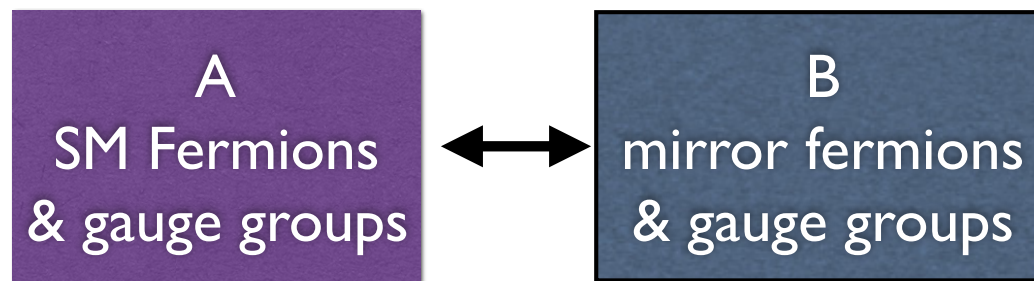
# Theory Example: Twin Higgs

$SM_A \times SM_B$  (mirror sector) particle content with  $Z_2$  symmetry

Higgs sector:  $SU(4)$ , broken by Gauge + Yukawa interactions to  $SU(2)_A \times SU(2)_B \times Z_2$ , which generate mass for goldstone boson.

$$\Delta V = \frac{3}{8\pi^2} \Lambda^2 \left( \lambda_A^2 H_A^\dagger H_A + \lambda_B^2 H_B^\dagger H_B \right) \quad \xrightarrow{\lambda_A = \lambda_B \equiv \lambda_t} \quad \Delta V = \frac{3\lambda^2}{8\pi^2} \Lambda^2 \left( H_A^\dagger H_A + H_B^\dagger H_B \right) = \frac{3\lambda^2}{8\pi^2} \Lambda^2 H^\dagger H$$

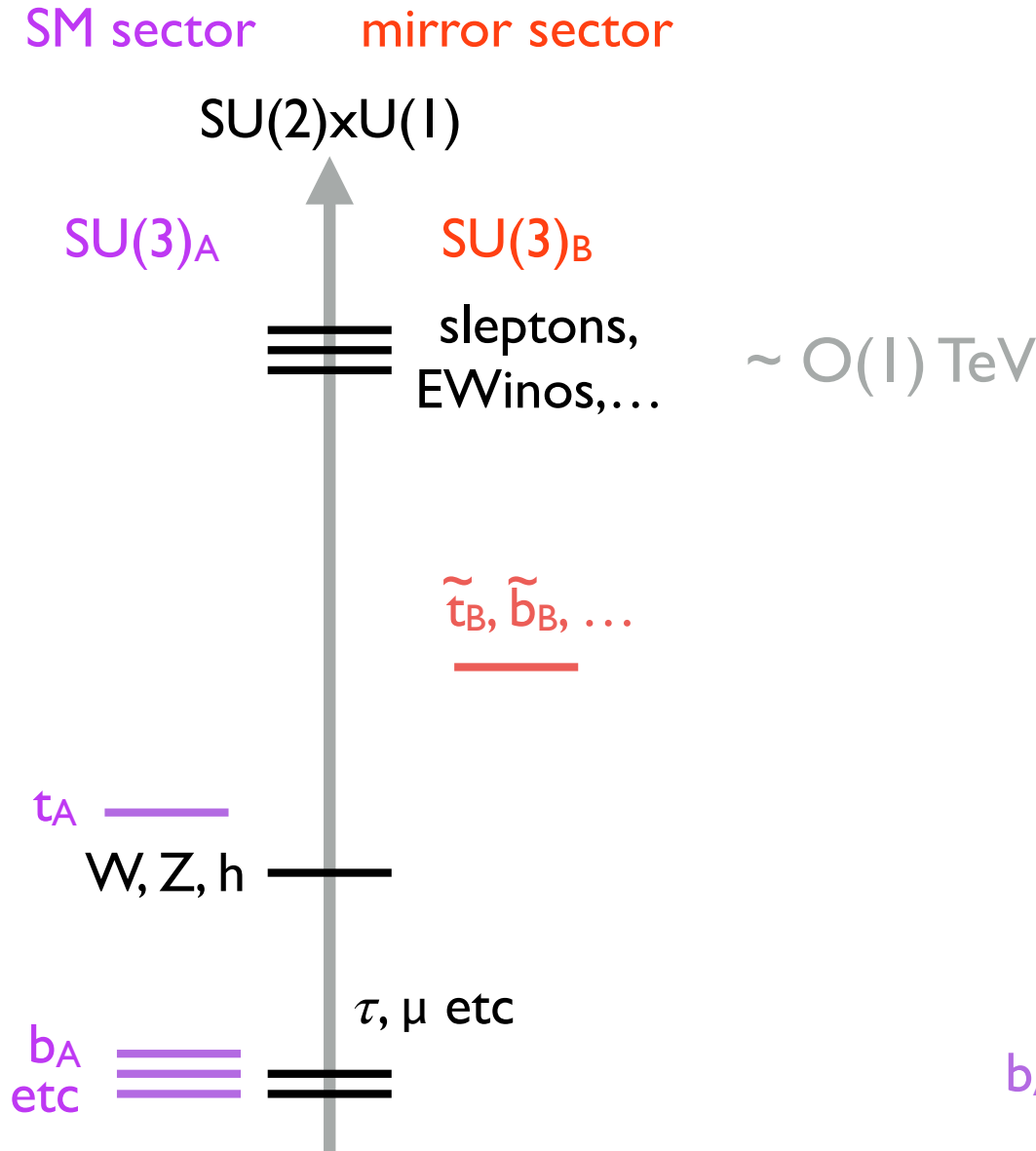
$Z_2$  symmetry of quadratically divergent contributions mimics full  $SU(4)$  symmetry, protects pNGB Higgs mass @ 1-loop.



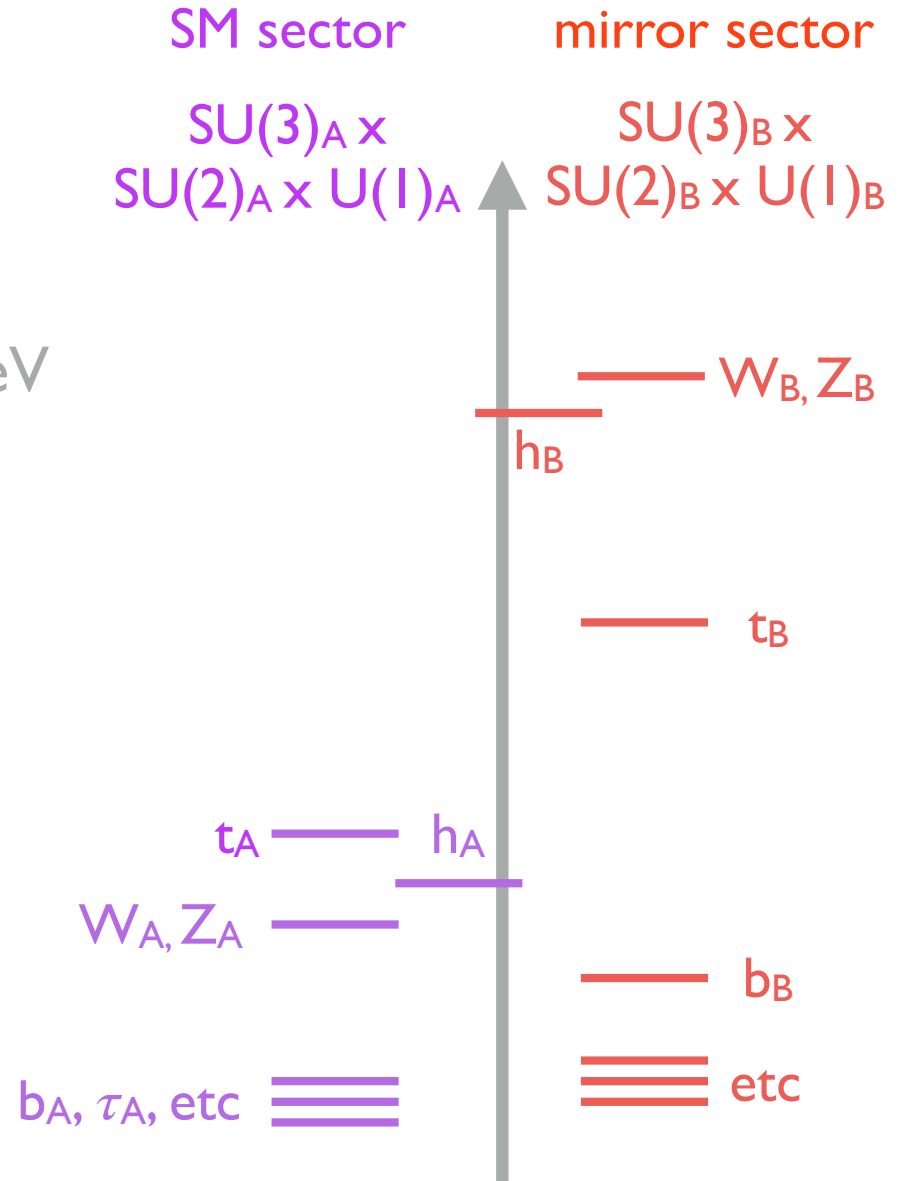
SM singlet  
top partners.

# Typical Low-Energy Spectra

## FSUSY (EW charged partners)



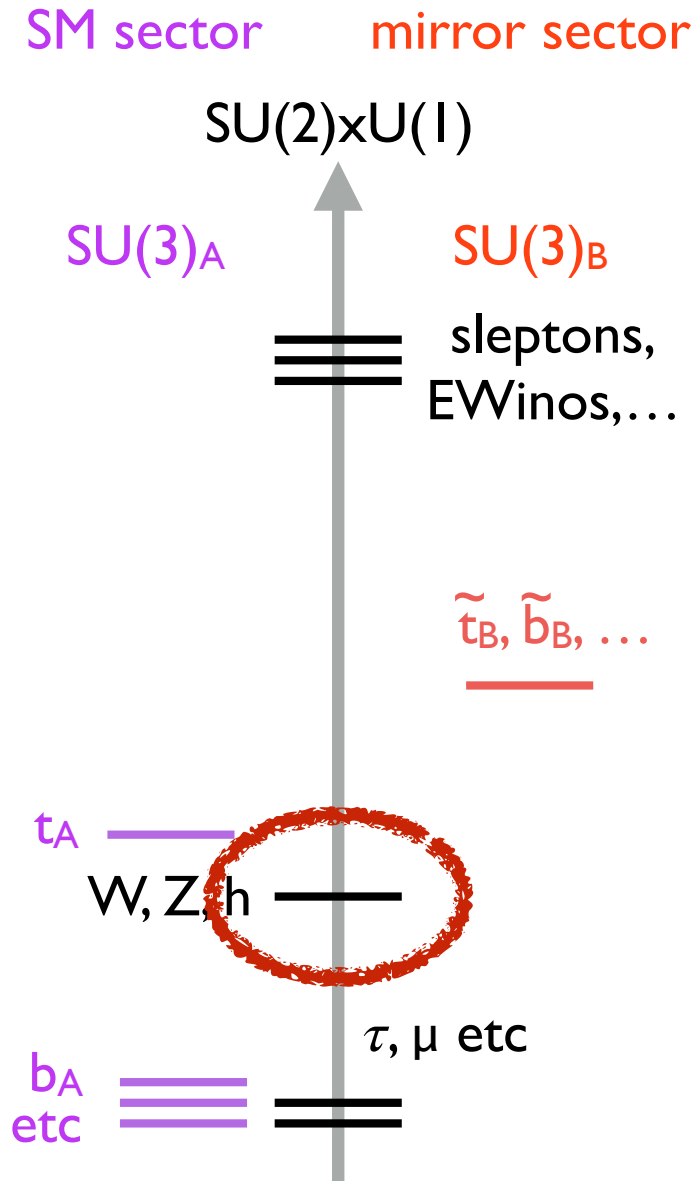
## Twin Higgs (SM singlet partners)



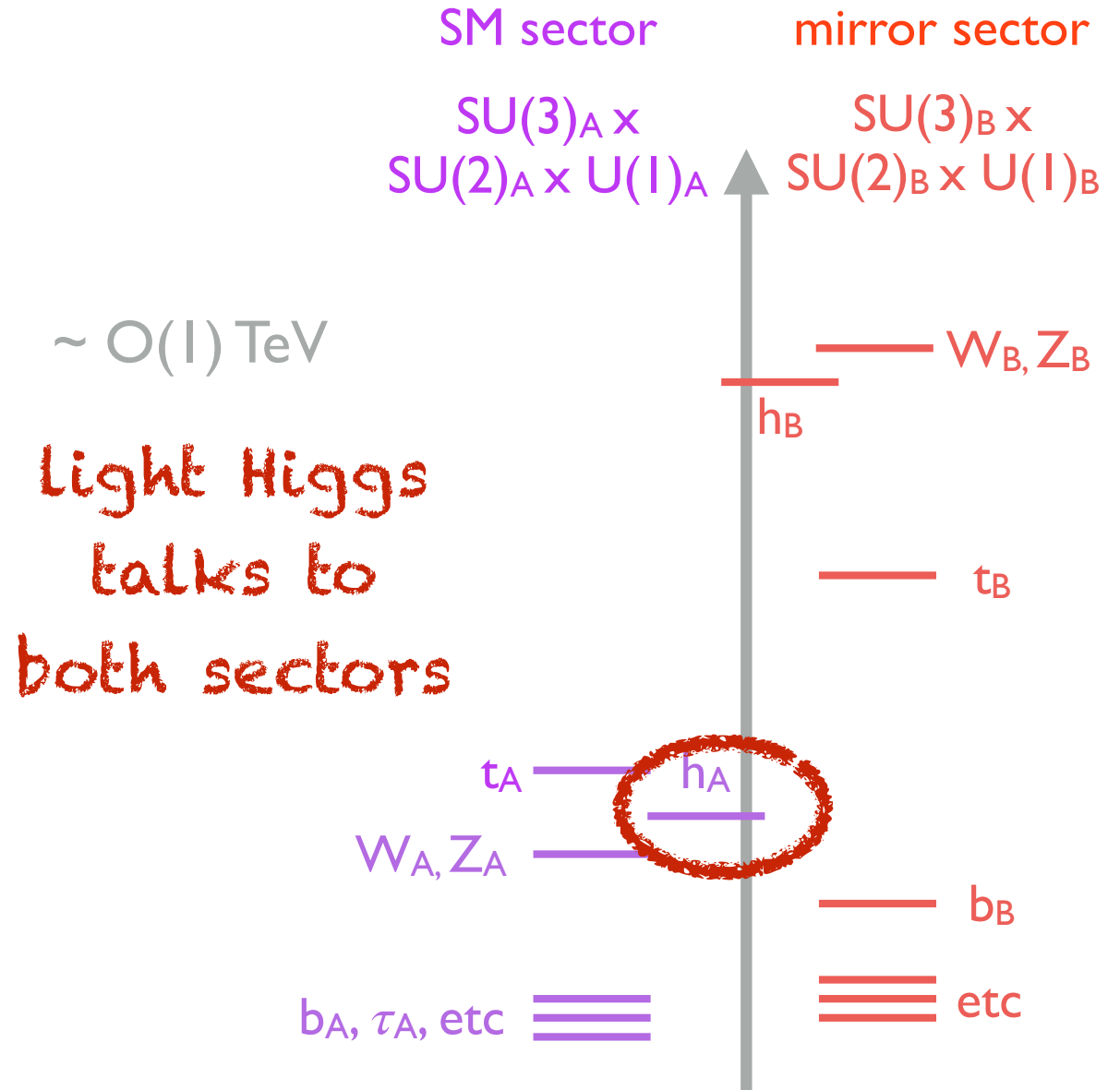


# Typical Low-Energy Spectra

## FSUSY (EW charged partners)



## Twin Higgs (SM singlet partners)



# Neutral Naturalness

Why would we think about this?

1. The LHC is \*great\* at making colored particles, but so far no top partner discovery...
2. Want to examine naturalness as generally as possible: **test the mechanism, not the model!**

**Neutral Naturalness generates radically different phenomenology from colored partners!**

What are the most  
important questions  
right now?

I. What signals of Neutral Naturalness could we probe **today**?

1. What signals of Neutral Naturalness could we probe **today**?
2. If the signatures are this malleable... will we be able to probe the *general mechanisms* underlying naturalness **tomorrow**?

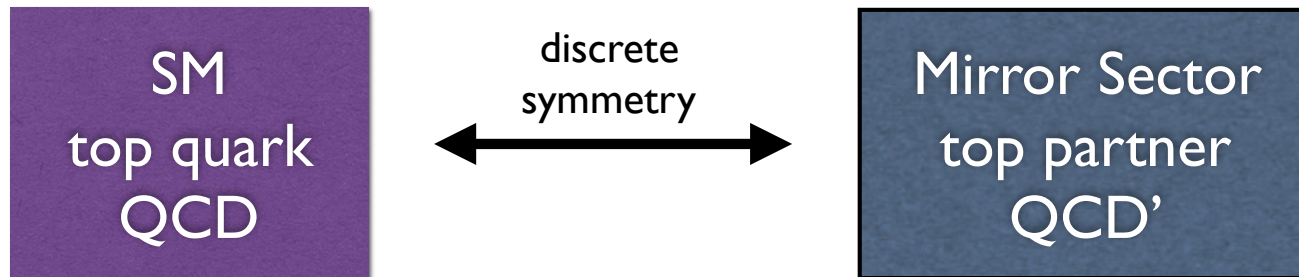
Probing Naturalness today:

**Signatures of  
Neutral Naturalness  
at the LHC**

# Hidden Valley Phenomenology

c.f. Strassler, Zurek '06 etc.

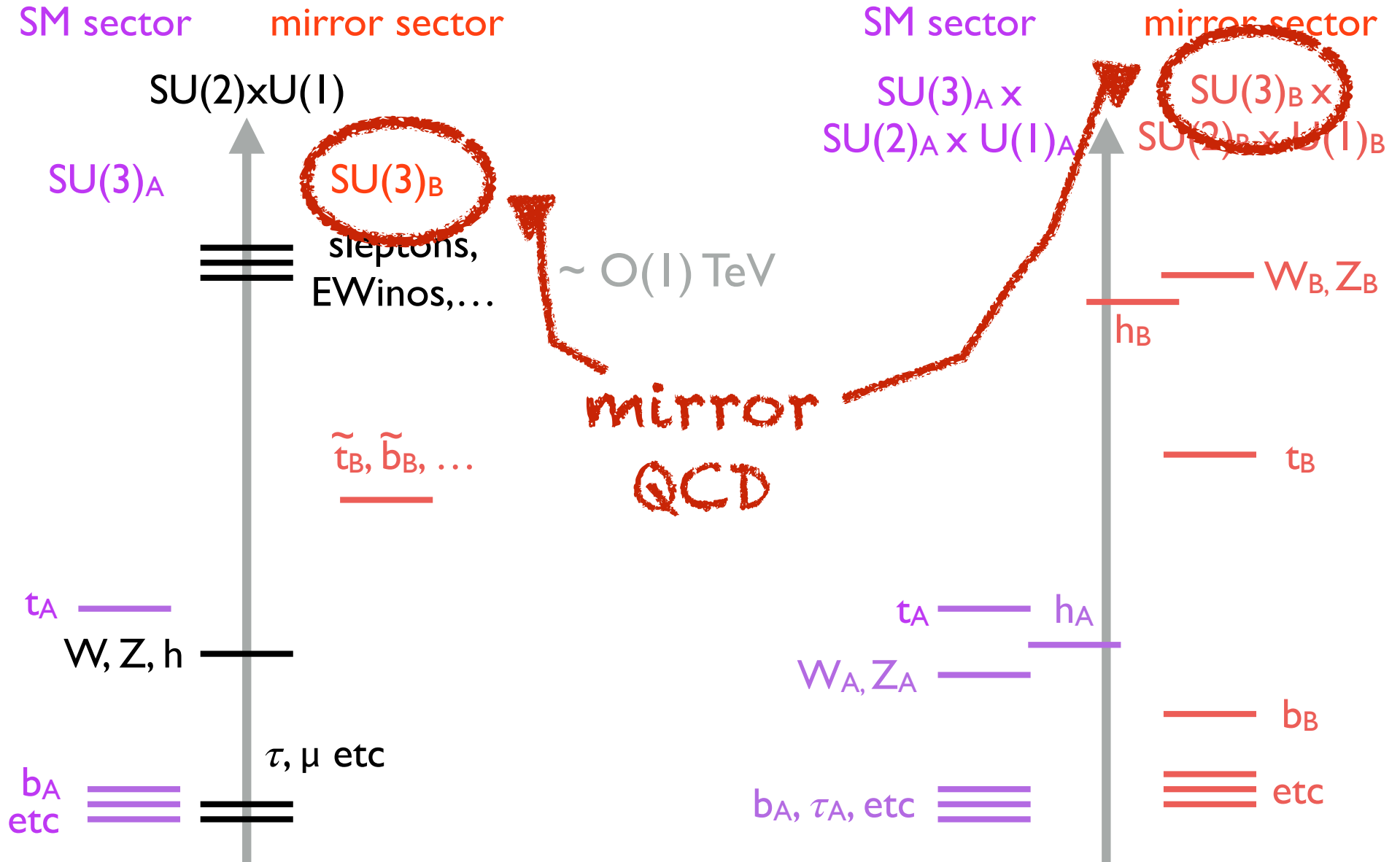
In theories of Neutral Naturalness, the partners in the mirror sector are usually charged under a copy of QCD



# Typical Low-Energy Spectra

FSUSY (EW charged partners)

Twin Higgs (SM singlet partners)





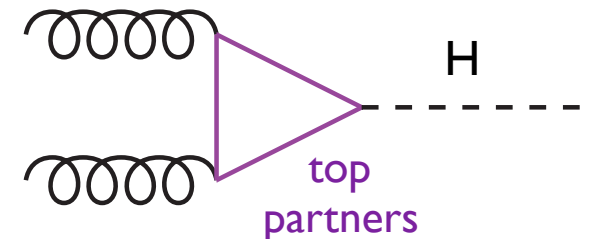
# Hidden Valley Phenomenology

c.f. Strassler, Zurek '06 etc.

Mirror gluons talk to the Higgs via top partner loops!

(just like the top quark connects the Higgs to SM QCD)

$$\mathcal{L}^{(6)} = \frac{\alpha_v y^2}{3\pi M^2} H^\dagger H \text{tr} \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu}$$



The mirror sector contains mirror hadrons.

Detailed consequences depend on the mirror spectrum:

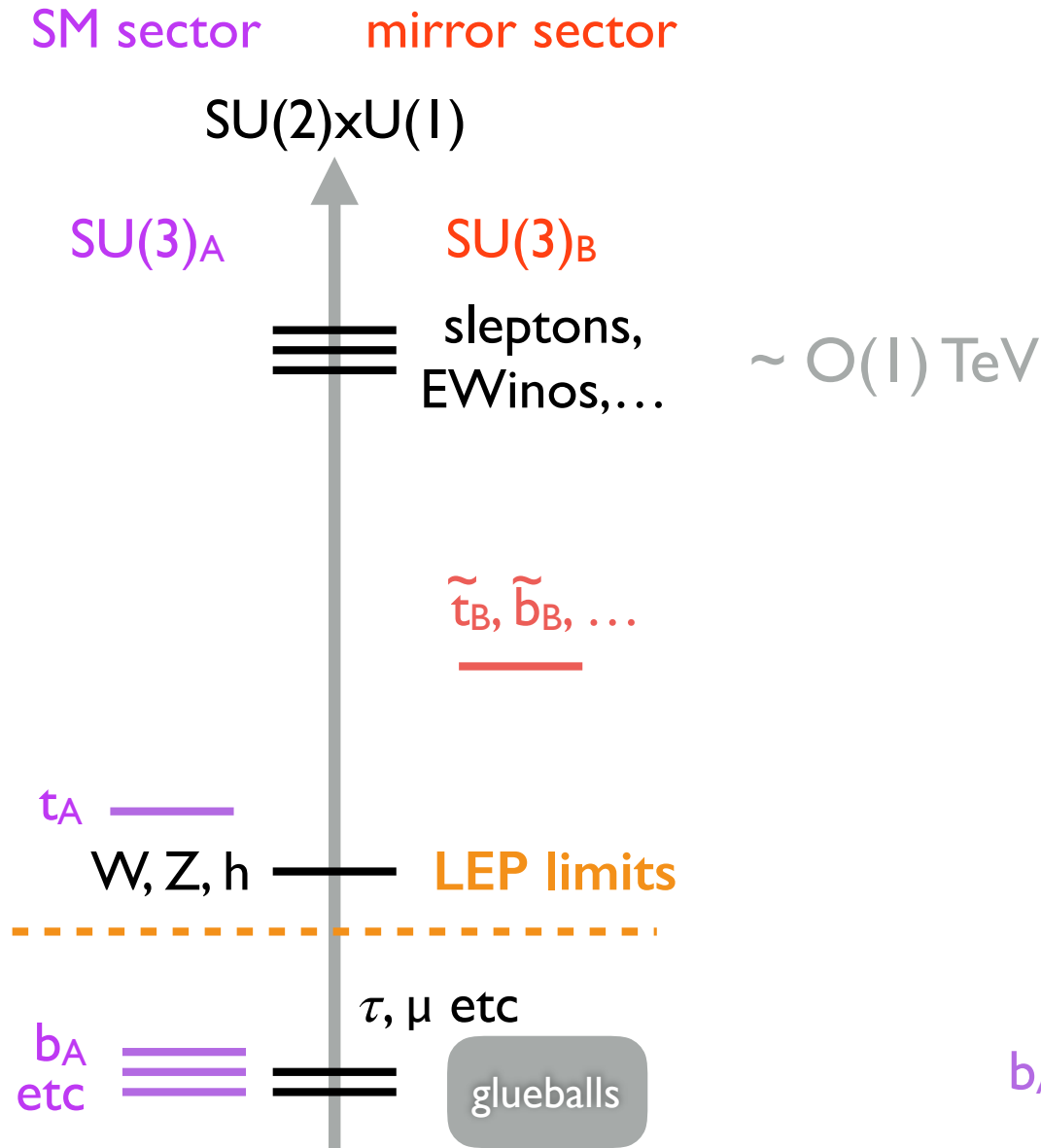
pions?

quarkonia?

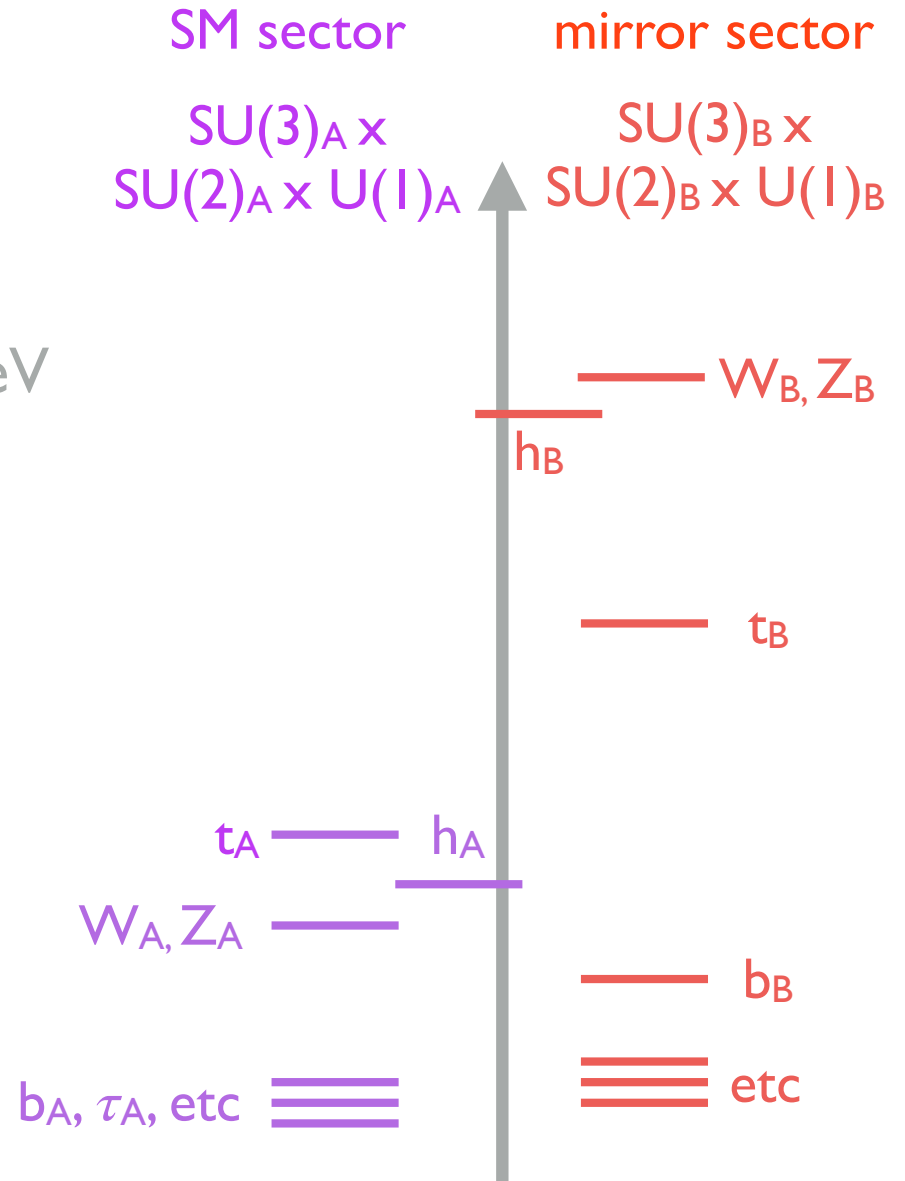
glueballs?

# Typical Low-Energy Spectra

## FSUSY (EW charged partners)



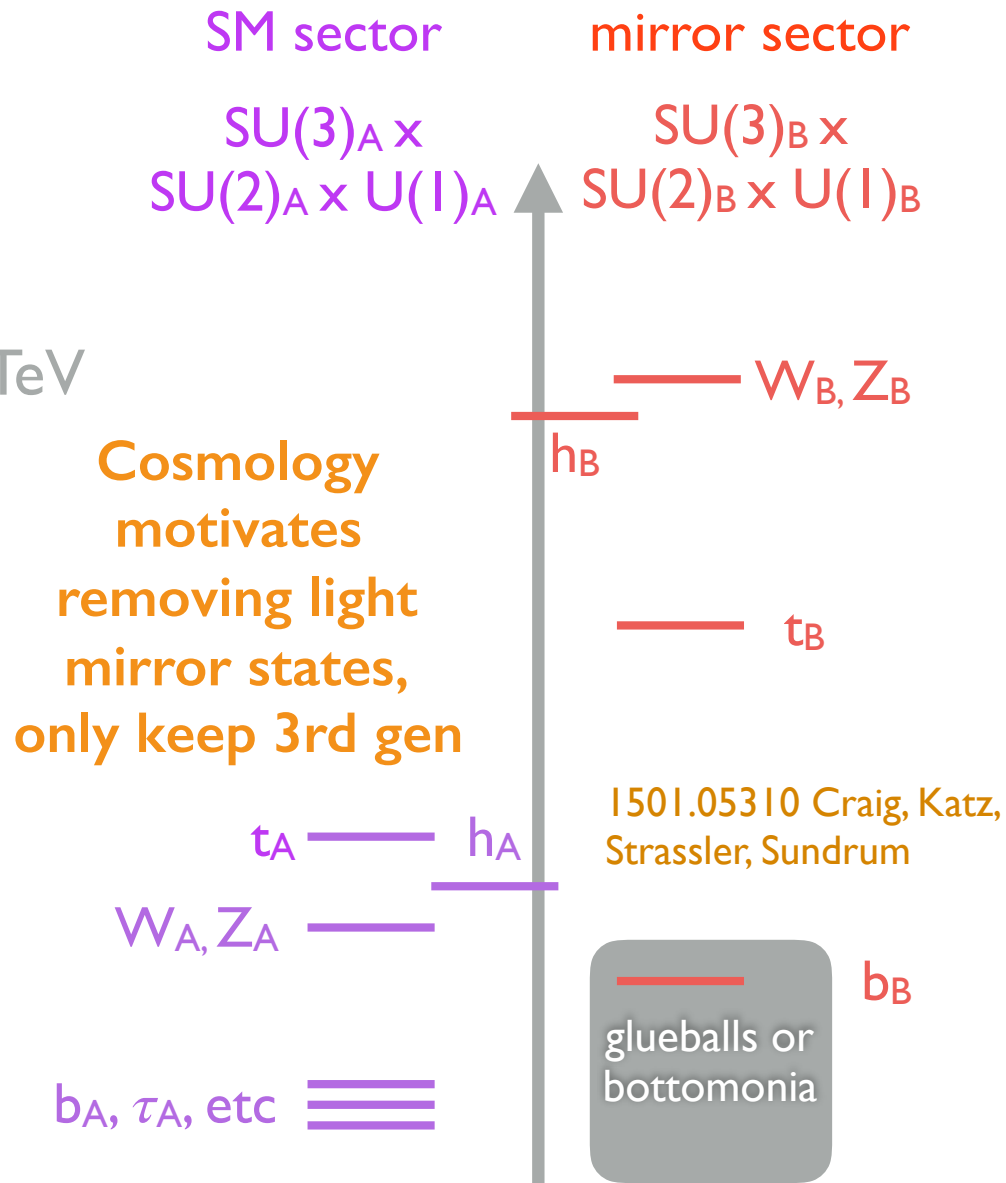
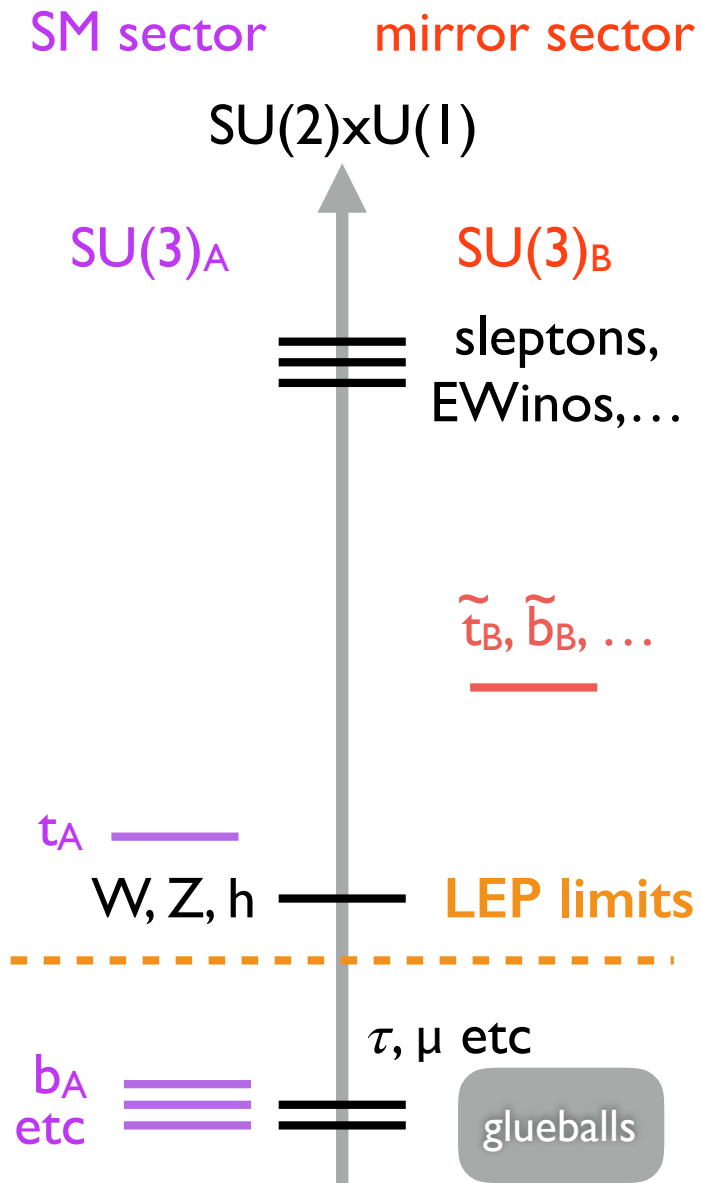
## Twin Higgs (SM singlet partners)



# Typical Low-Energy Spectra

FSUSY (EW charged partners)

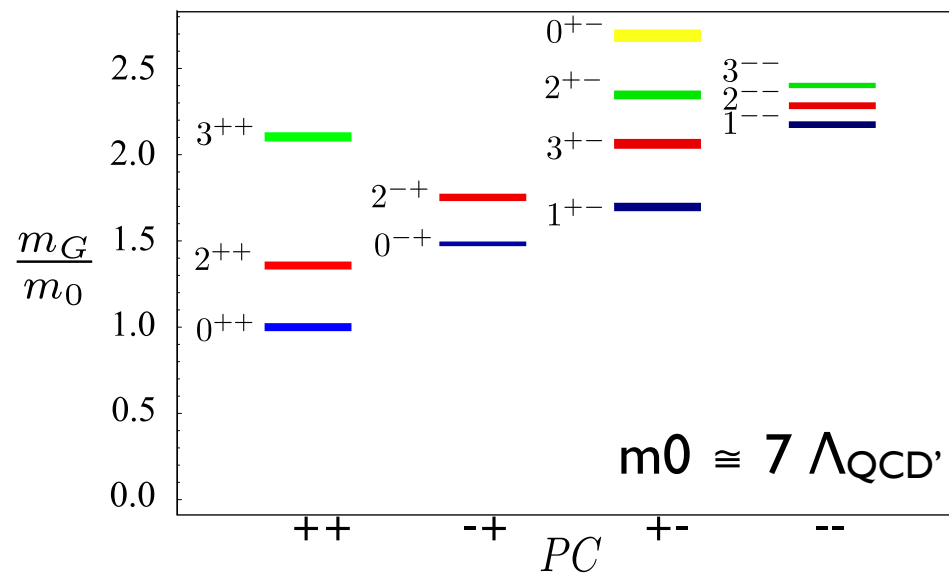
Fraternal Twin Higgs  
(SM singlet partners)



$\sim O(1)$  TeV

# Mirror Glueballs

If the mirror sector has no light matter, the mirror QCD hadrons are **glueballs**.



“Required” for EW charged top partners.

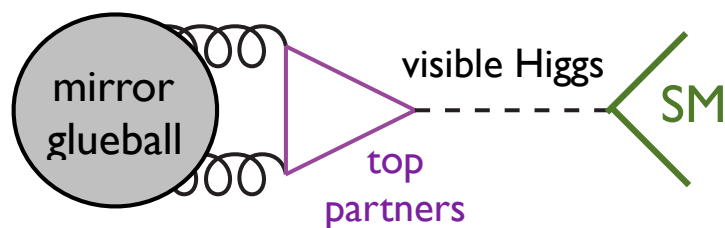
Possible (motivated by cosmology) for SM singlet top partners.

# Glueball-Higgs Coupling

0903.0883 Juknevich, Melnikov, Strassler; 0911.5616 Juknevich

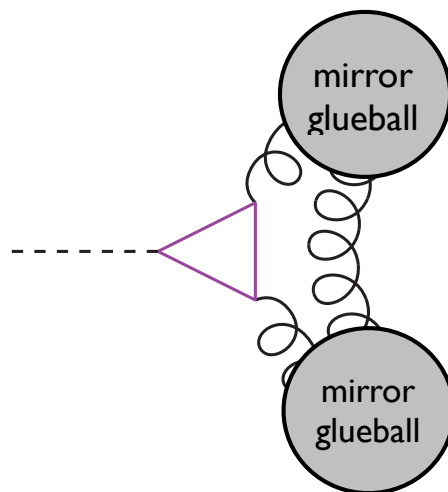
Glueballs mix with the Higgs via top partner loop:

**$0^{++}$  would eventually decay back to SM!**



The Higgs could also decay to these glueballs:

**exotic Higgs decays with displaced vertices!**



**Key signature of uncolored naturalness!**

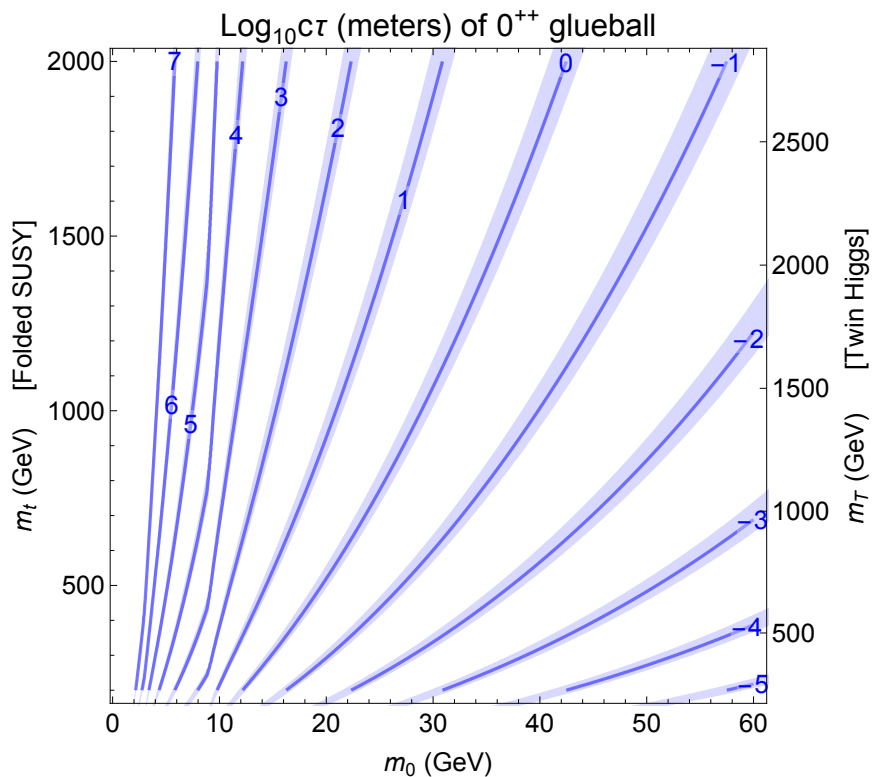
1501.05310 Craig, Katz, Strassler, Sundrum

# Is this signature realized?

**Mass:**  $m_0 \sim 7\Lambda_{\text{QCD}}, \sim 10 - 60 \text{ GeV}$  from RG arguments, but can move that around in Twin Higgs theories. DC, Verhaaren 1506.06141

**⇒ can be produced in exotic Higgs decays!**

**Lifetime of  $0^{++}$ :**  $c\tau \sim \mu\text{m} - 1\text{km}$  (using lattice results)



$$\Gamma(0^{++} \rightarrow \xi\xi) =$$

$$\left( \frac{1}{12\pi^2} \left[ \frac{y^2}{M^2} \right] \frac{v}{m_h^2 - m_0^2} \right)^2 (4\pi\alpha_s^{\text{BFS}} F_{0^{++}}^{\text{S}})^2 \Gamma_{h \rightarrow \xi\xi}^{\text{SM}}(m_0^2).$$

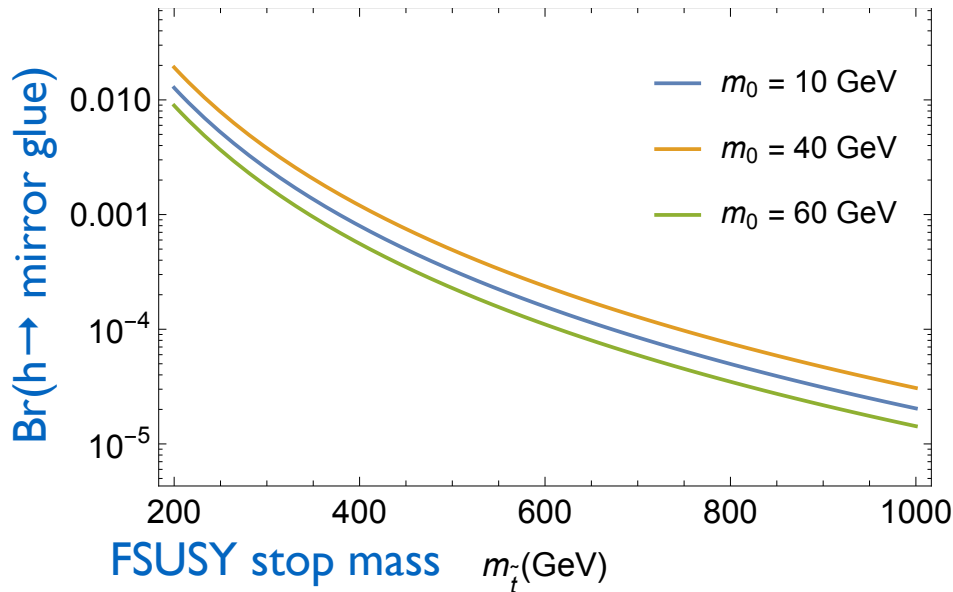
**⇒ displaced decays  
at colliders!**

**(mostly to  $bb, \tau\tau$ )**

**YES!**

# How many glueballs from Higgs decays?

Estimate **inclusive** mirror-gluon production by rescaling SM  $\text{Br}(h \rightarrow gg)$  by top partner loop and mirror  $\alpha_s'$  (also from RG arguments).



LHC 14 with 300fb-1 makes  $O(10 \text{ million})$  higgs bosons.

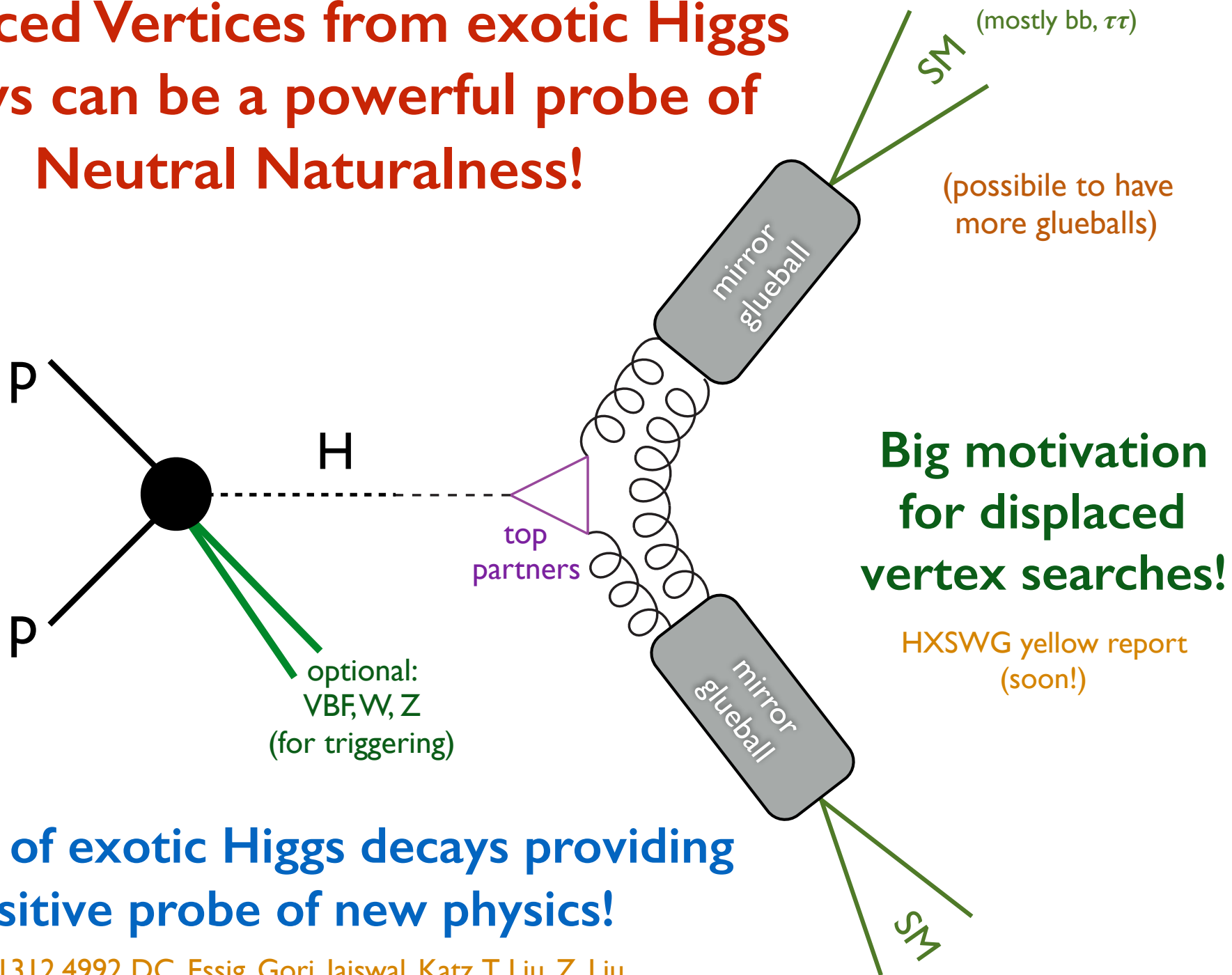
Could probe TeV-scale top partners if exotic Higgs decays conspicuous enough!

Conservatively estimate **exclusive** production of **unstable  $0^{++}$  glueball** by parameterizing our ignorance about mirror hadronization:

$$\text{Br}(h \rightarrow 0^{++}0^{++}) = \text{Br}(h \rightarrow \text{mirror glue}) \cdot \kappa \cdot \sqrt{1 - \frac{4m_0^2}{m_h^2}}$$

Let  $\kappa$  range from  
 $\sim 1/12$  (democratic) to  
 $\sim 1$  (optimistic).

# Displaced Vertices from exotic Higgs decays can be a powerful probe of Neutral Naturalness!



Example of exotic Higgs decays providing sensitive probe of new physics!

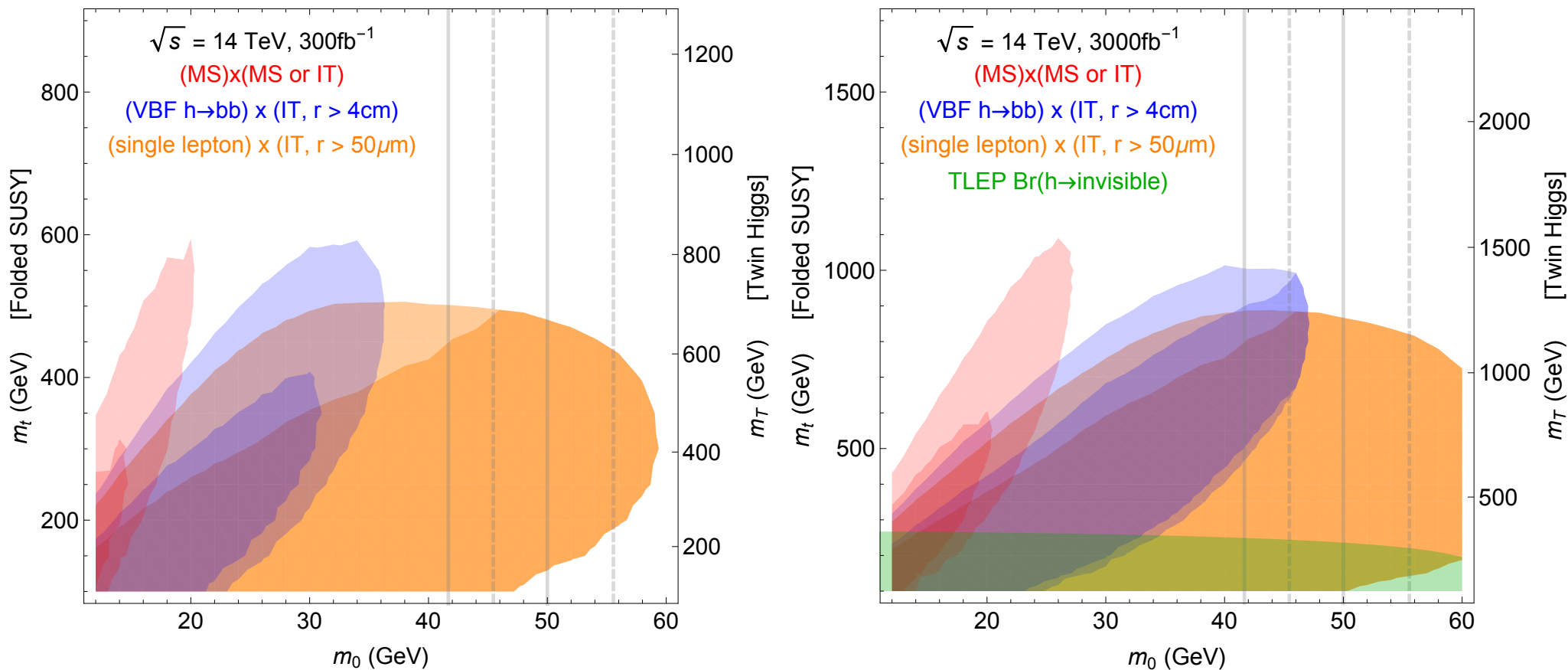
Review/Survey: 1312.4992 DC, Essig, Gori, Jaiswal, Katz, T. Liu, Z. Liu, McKeen, Shelton, Strassler, Surujon, Tweedie, Zhong

DC, Verhaaren 1506.06141



# LHC reach

## ATLAS sensitivity projections to LHC I4:



**Displaced searches probe TeV-scale uncolored top partners!**

# LHC reach

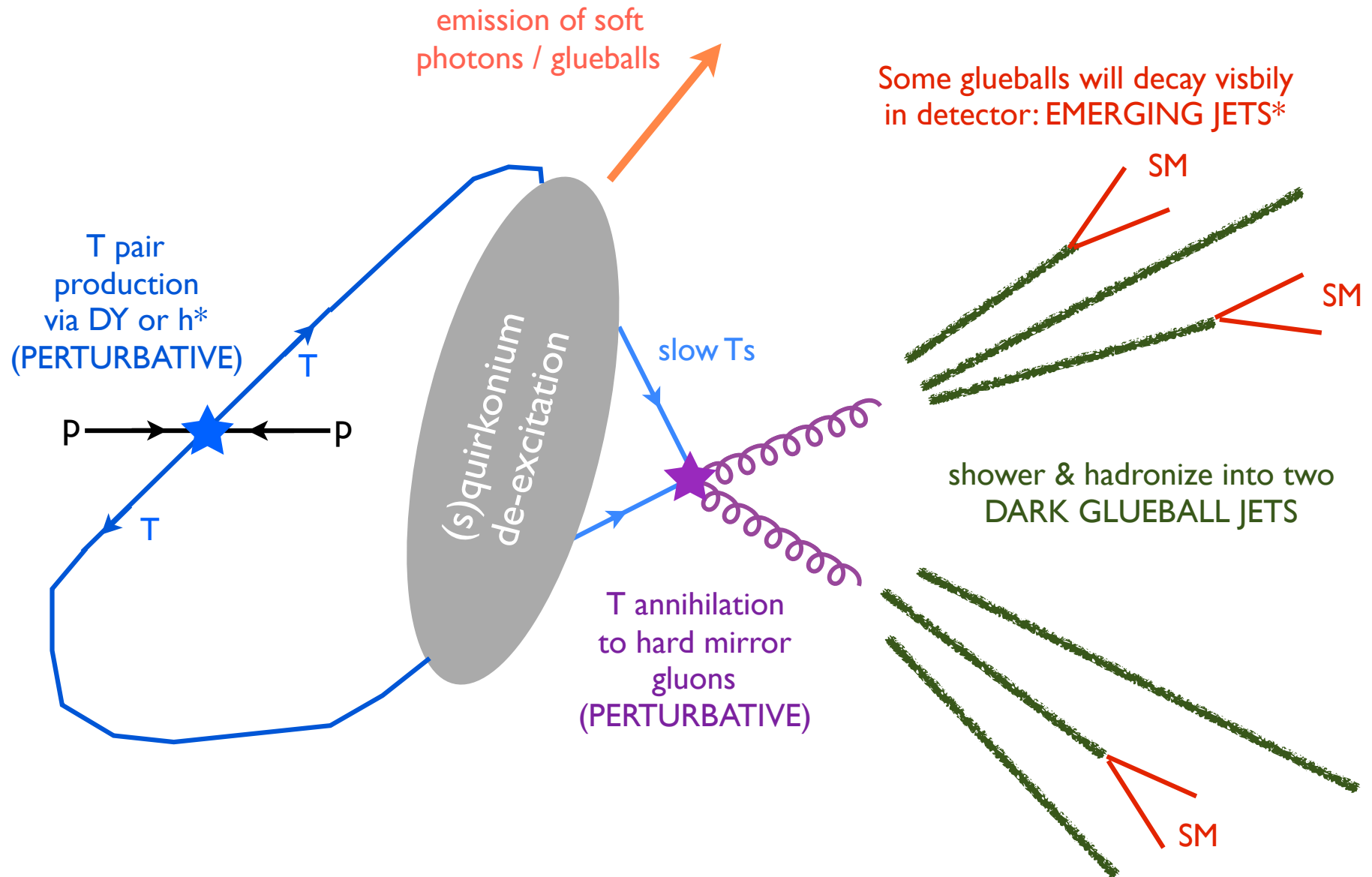
## ATLAS sensitivity projections to LHC14:



**Displaced searches probe TeV-scale uncolored top partners!**

# Top partner direct production

# Top partner direct production



# Top partner direct production

Great opportunity:

- direct evidence of uncolored top partners.
- might have comparable reach to exotic Higgs decays
- could allow measurement of couplings and masses.
- potentiall spectacular signatures: several DVs, or many  $bb$ ,  $\tau\tau$  pairs

**Main challenge: how to model mirror hadronization?**

Have to parameterize our ignorance again, but this time use DGLAP evolution of hypothetical fragmentation functions to estimate glueball multiplicity and mean  $p_T$ .

**Work in progress!**

# Prospects today

**Displaced signatures** are a great LHC opportunity, and a “smoking gun” for most theories with EW top partners (e.g. FSUSY). Can occur in some TH models.

Many signatures still unexplored, e.g. Flavor....

However: quasi-stable light mirror states are not guaranteed in theories of Neutral Naturalness.

What are the *unavoidable* signatures, at the LHC and at future **lepton** an **100 TeV** colliders?

Probing Naturalness exhaustively:

**A No-Lose Theorem**

**for Generalized Top**

**Partners.**

# Top Partners with SM Charge

Start with TeV-scale top partners that carry SM charge.

If QCD: produce plenty, discover at LHC or 100 TeV.

If partners carry any EW charge, regardless of decay mode etc, will be detectable up to  $\sim 2+ \text{TeV}$  @ 100 TeV due to RG effects in DY spectrum measurements!

Alves, Galloway, Rudermann, Walsh 1410.6810

TeV-scale SM-charged partners ARE DISCOVERABLE  
regardless of model details!



# Neutral Top Partners

explain twin higgs signatures  
how its tree tuning of soft  $z_2$  vs  
is that totally model-indep? no

We really only have one class of models for neutral top partners: **Twin Higgs**, which predicts Higgs coupling deviations  $\sim$  tuning at lepton colliders.

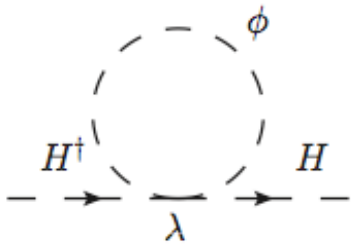
Is this general? Would like to understand signatures of neutral top partners **model-independently!**

**→ Bottom-Up EFT/Simplified Model Approach!**

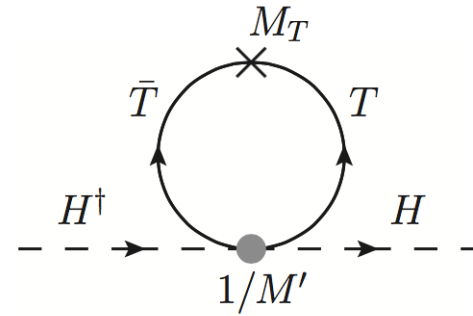
# Two distinct low-energy EFTs

## Scalar Partners

(Vector partners  
“same” as scalars)



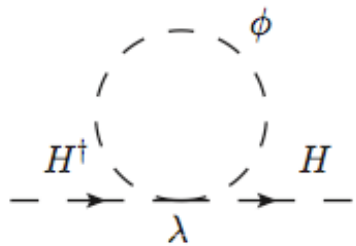
## Fermion Partners



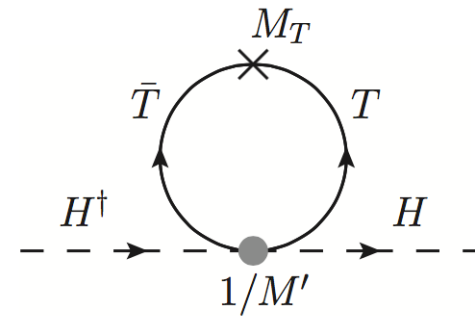
# Two distinct low-energy EFTs

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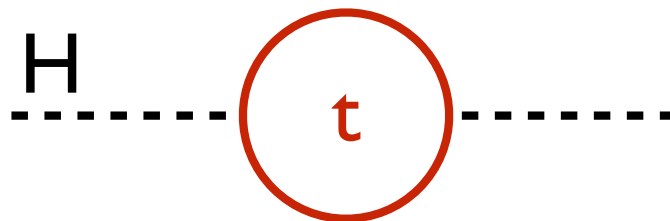
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## Fermion Partners



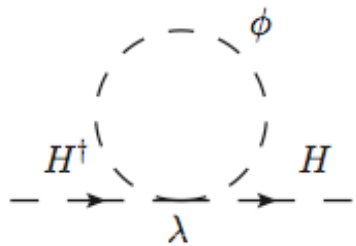
Only impose *one* condition on EFT:  
cancellation of quadratic divergence from top loop



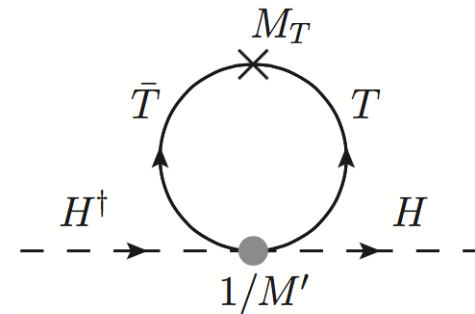
# Two distinct low-energy EFTs

## Scalar Partners

(Vector partners  
“same” as scalars)



## Fermion Partners



Relevant terms in the HEFT expansion:

$$\mathcal{L}_\phi \supset -\sum_i \phi_i^2 \left( \frac{1}{2} \mu_{\phi_i}^2 + \frac{1}{2} \lambda_i |H|^2 \right)$$

$$\mathcal{L}_T \supset \sum_i T_i \bar{T}_i \left( M_{T_i} - \frac{|H|^2}{2M'_i} \right)$$

Condition to cancel one-loop quadratic divergence from top quark:

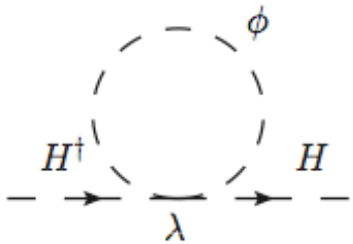
$$\lambda_\phi = \frac{12}{N_r} |y_t|^2$$

$$\frac{M_T}{M'} = \frac{3}{N_f} y_t^2$$

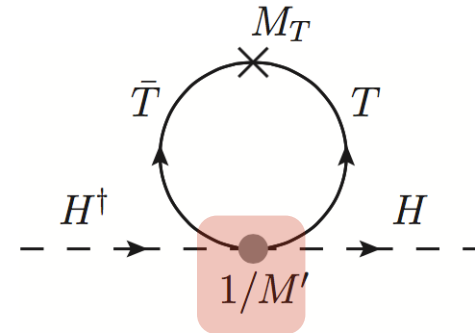
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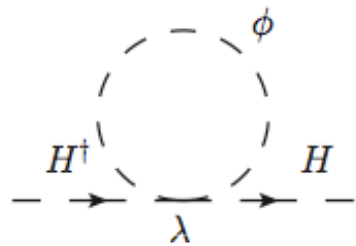
$$\lambda_\phi = \frac{12}{N_r} |y_t|^2$$

$$\frac{M_T}{M'} = \frac{3}{N_f} y_t^2$$

Non-renormalizable term limits what we can compute.  
Need partial UV completion for fermion partners!

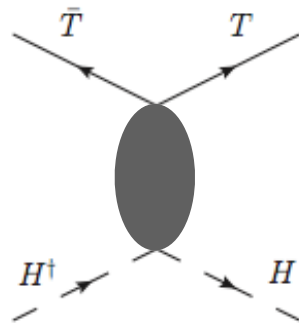
# Four possible Neutral Top Partner structures

## Scalar Partners

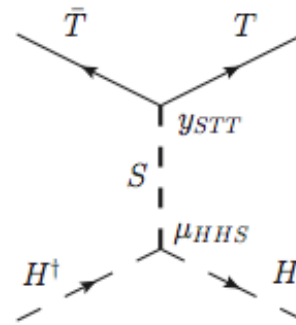


## Fermion Partners

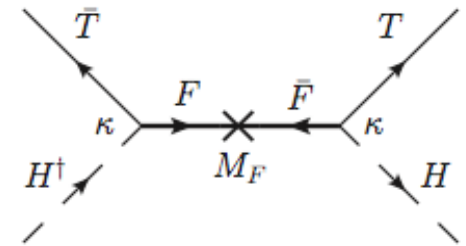
For fermion partners, have to distinguish how HHTT operator is generated.



Strong Coupling



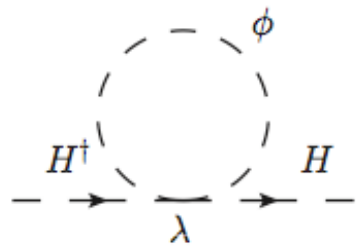
Scalar Mediator



Fermion Mediator

# Four possible Neutral Top Partner structures

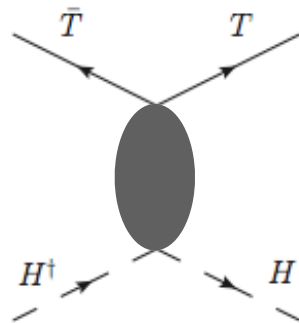
## Scalar Partners



↑  
?

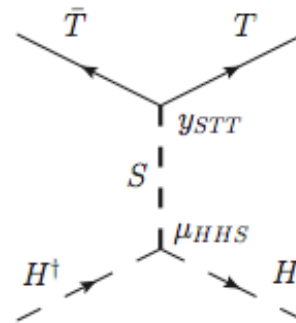
## Fermion Partners

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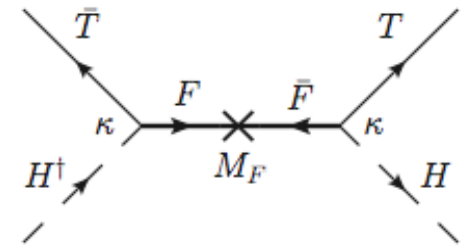
Strong Coupling

↑  
**Twin Higgs**  
with composite/  
holographic UV  
completion



Scalar Mediator

↑  
**Twin Higgs**  
with perturbative  
UV completion



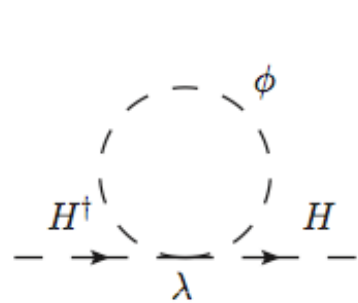
Fermion Mediator

↑  
?

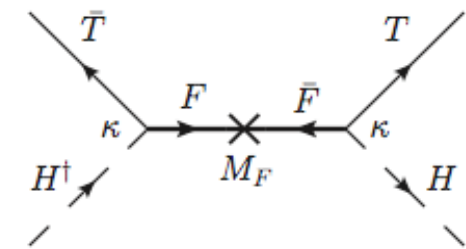
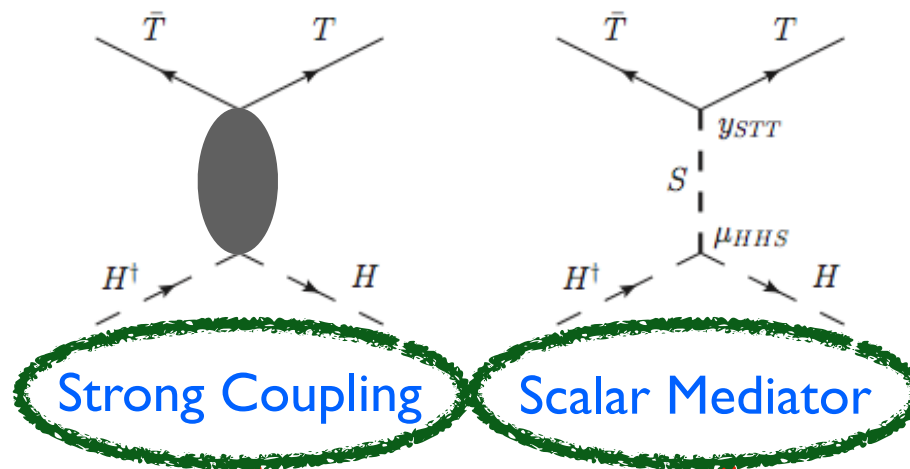
# Four possible Neutral Top Partner structures

## Scalar Partners

## Fermion Partners



For fermion partners, have to distinguish how HHTT operator is generated.



Strong Coupling

Scalar Mediator

Fermion Mediator

?

**Twin Higgs**  
with composite/  
holographic UV  
completion

**Twin Higgs**  
with perturbative  
UV completion

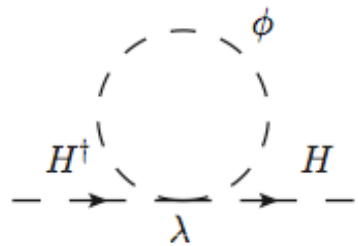
?

Much more general  
than Twin Higgs!



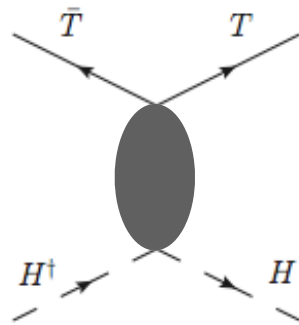
# Four possible Neutral Top Partner structures

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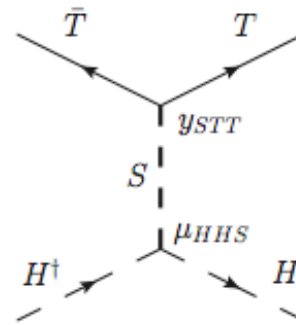


## Fermion Partners

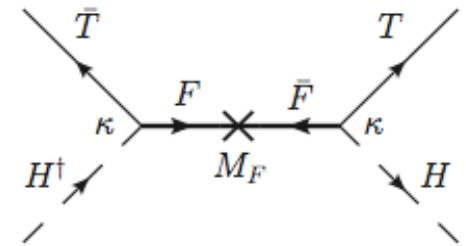
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Strong Coupling



Scalar Mediator



Fermion Mediator

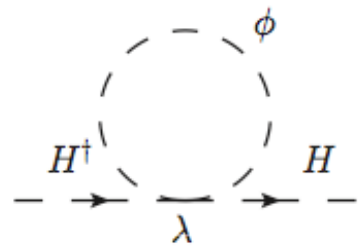
For each scenario, analyze:

Irreducible low-E signatures:

- Zh cross section (lepton collider)
- electroweak precision observables (lepton)
- higgs cubic coupling (100 TeV)
- top partner direct production (100 TeV)

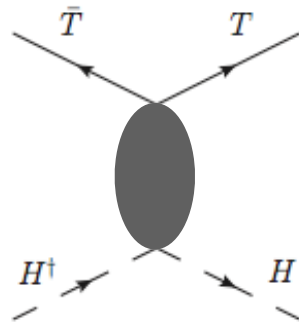
# Four possible Neutral Top Partner structures

## Scalar Partners

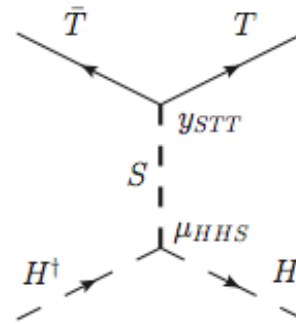


## Fermion Partners

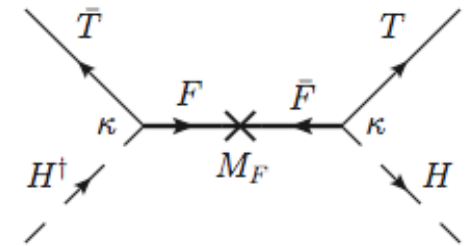
For fermion partners, have to distinguish how HHTT operator is generated.



Strong Coupling



Scalar Mediator



Fermion Mediator

For each scenario, analyze:

Irreducible low-E signatures:

- Zh cross section (lepton collider)
- electroweak precision observables (lepton)
- higgs cubic coupling (100 TeV)
- top partner direct production (100 TeV)

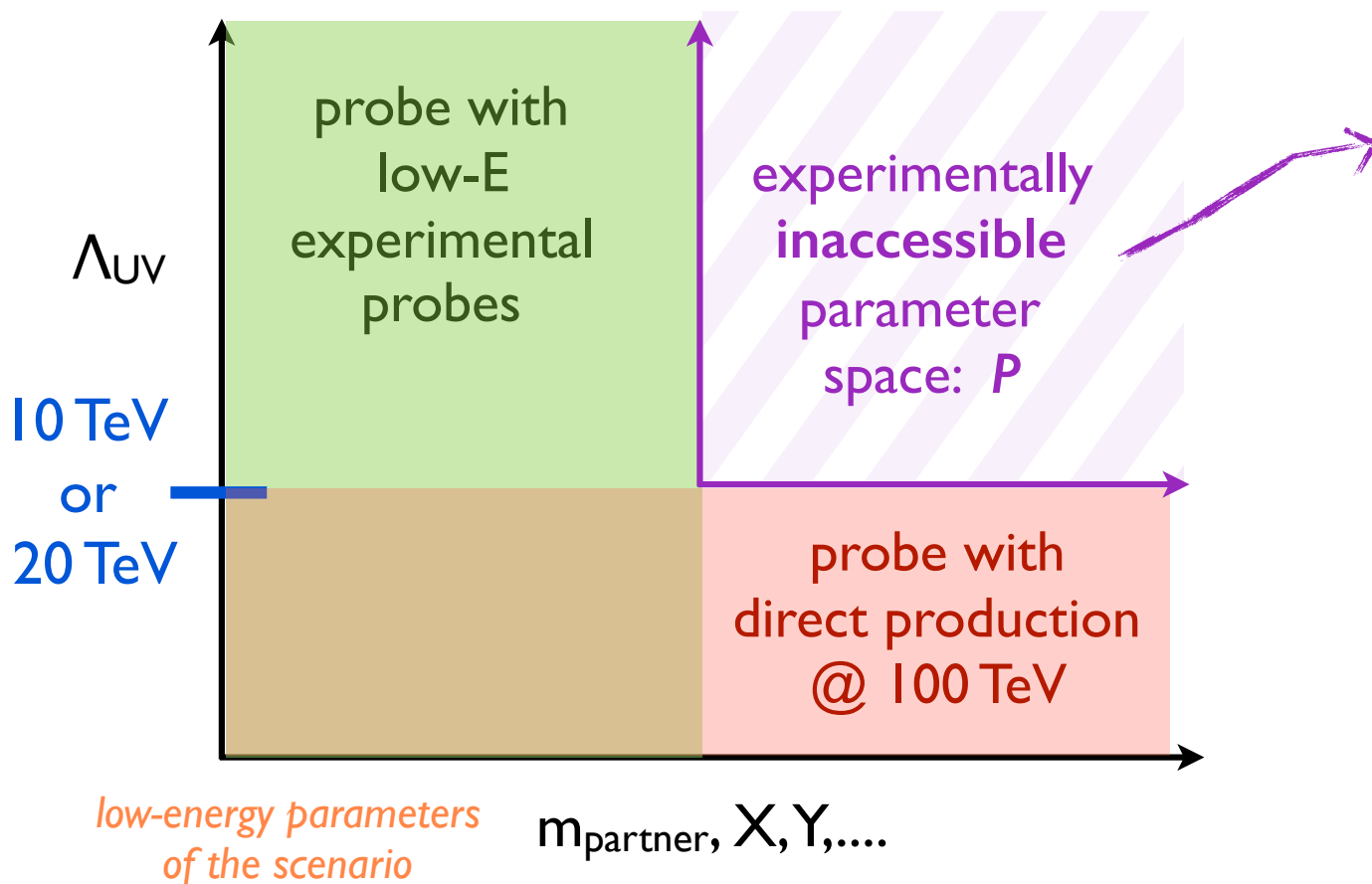
Irreducible tunings  $\{\Delta_i\}$  of loop vs tree suffered by scenario  $\Rightarrow \Delta_{\text{tot}} = f(\Delta_i)$

These will relate to UV completion scale  $\Lambda_{\text{UV}}$ .

Existing UV completions & symmetry arguments suggest SM-charged BSM states at this scale  
 $\rightarrow$  **Assume** production at 100 TeV collider!

# Strategy

For each scenario:



Find the LEAST TUNED the theory can be while escaping experimental detection:

$$\Delta_{\text{tot}}^{\min} = \text{Max}_{\{P\}} f(\Delta_i)$$

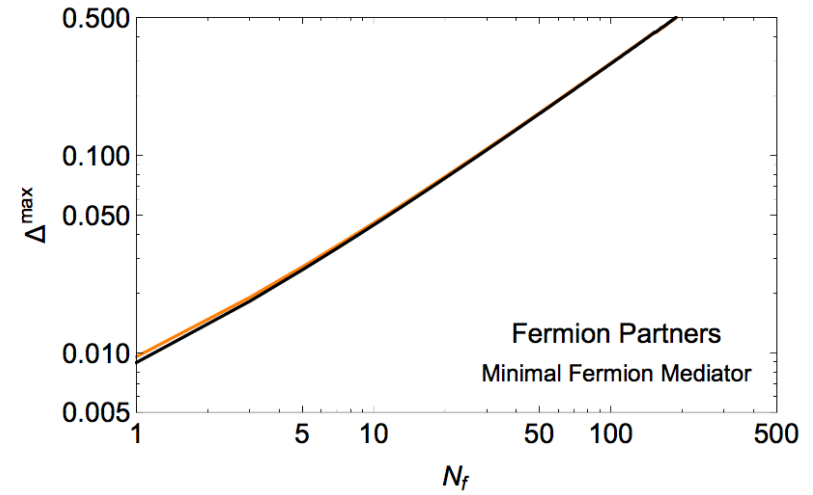
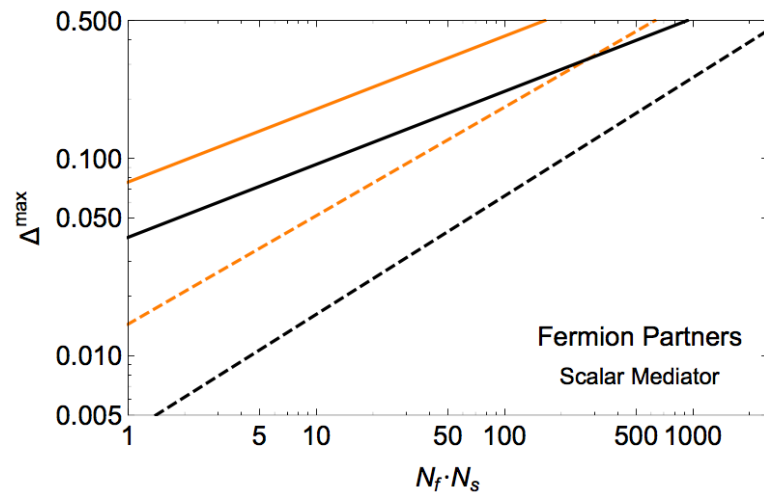
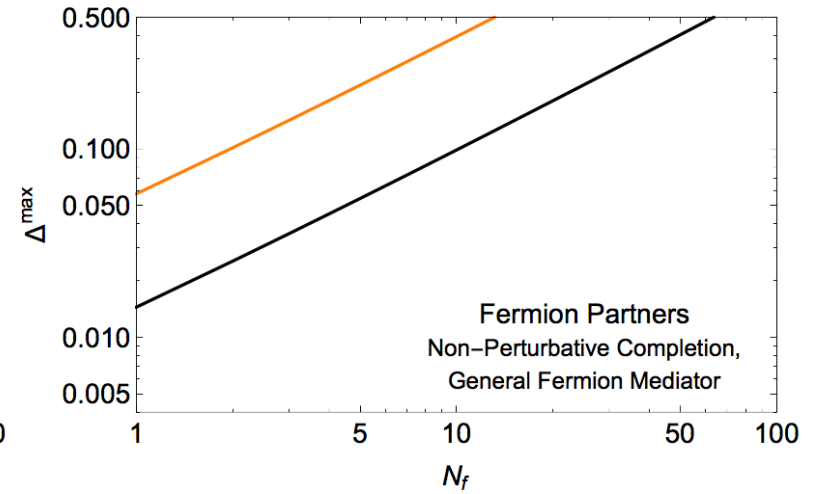
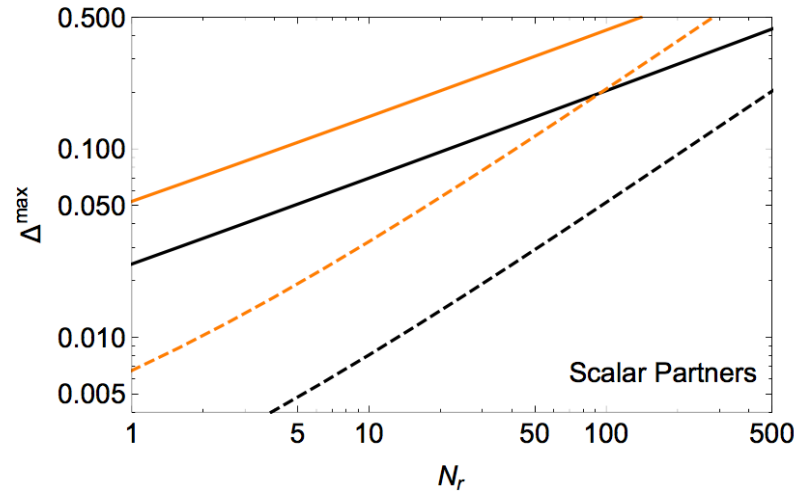
This will allow us to determine how natural an “undiscoverable” theory could be...

# Preview of Results

$\Lambda_{UV}^{\text{reach}} = 10 \text{ TeV} \quad 20 \text{ TeV}$

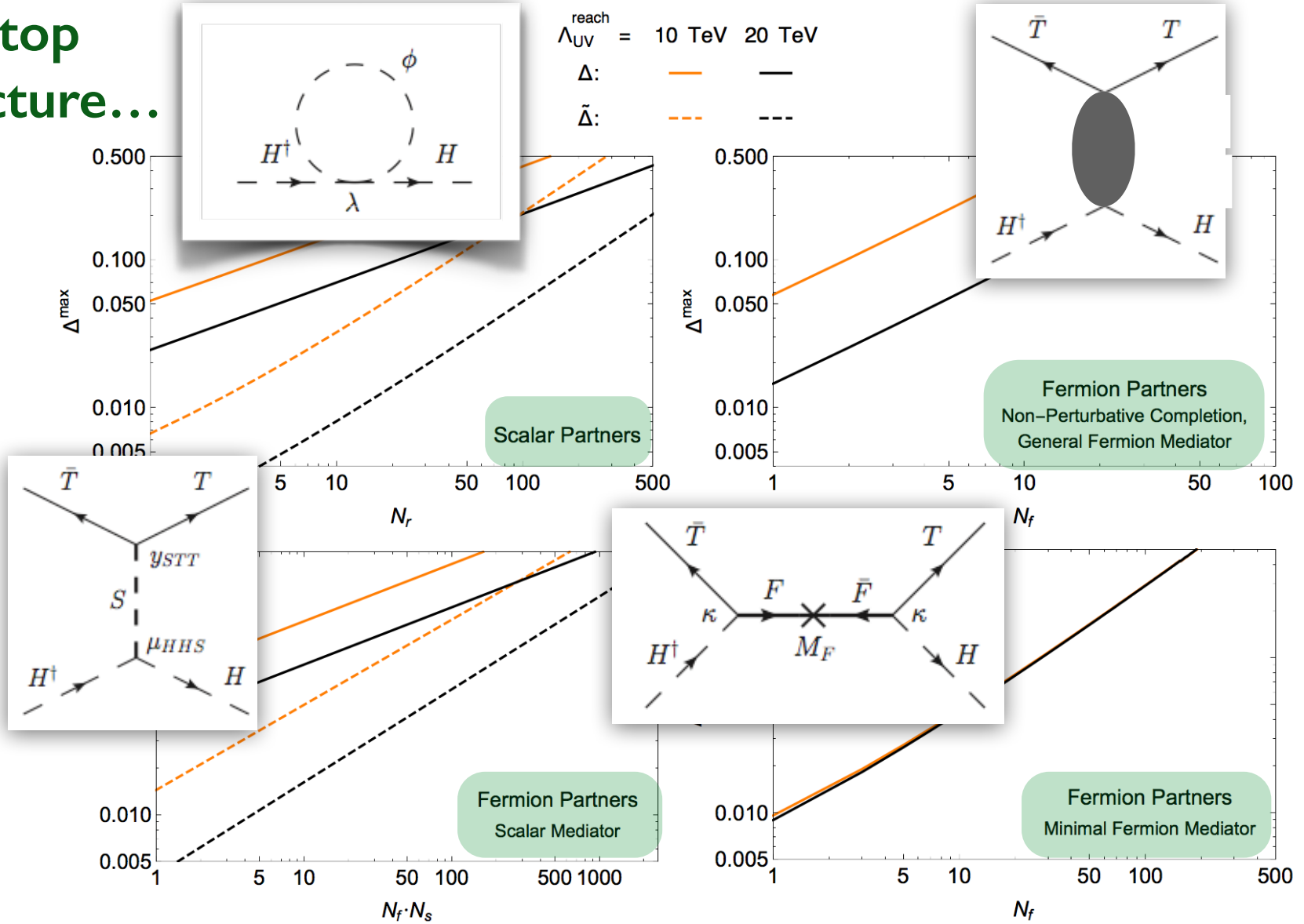
$\Delta$ : — (orange) — (black)

$\tilde{\Delta}$ : - - - (orange) - - - (black)



# Preview of Results

For each top partner structure...

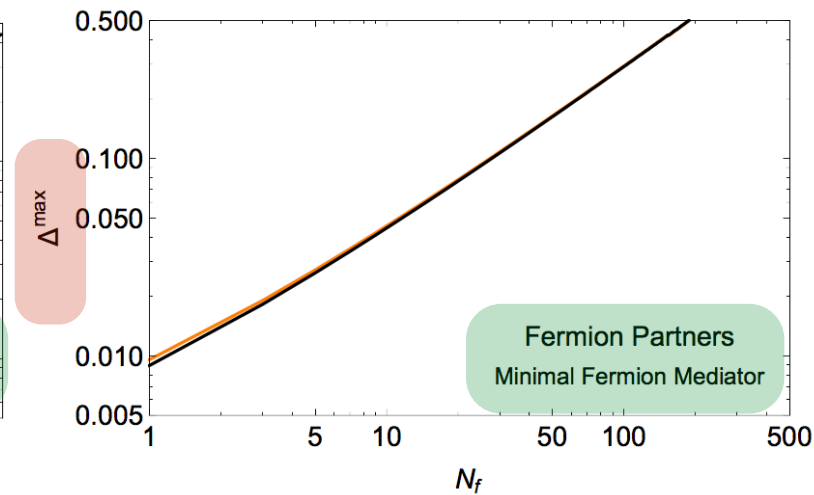
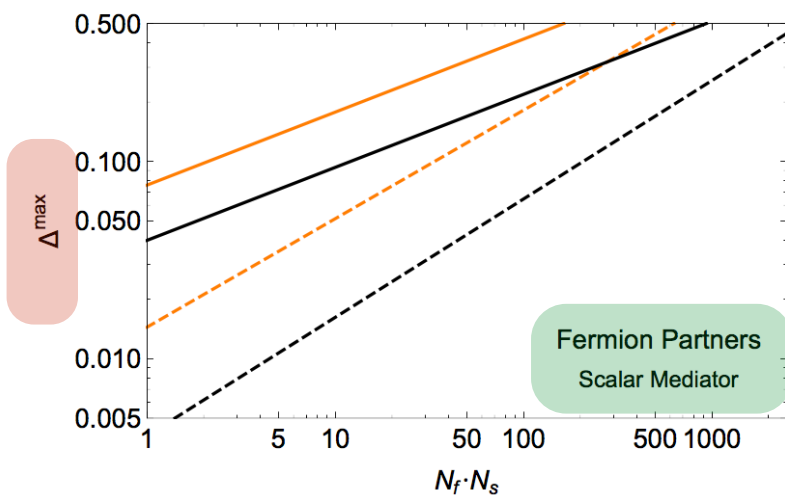
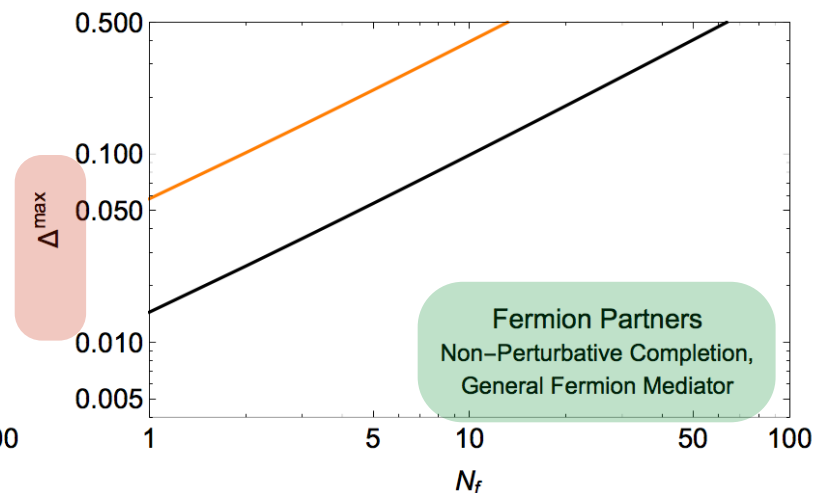
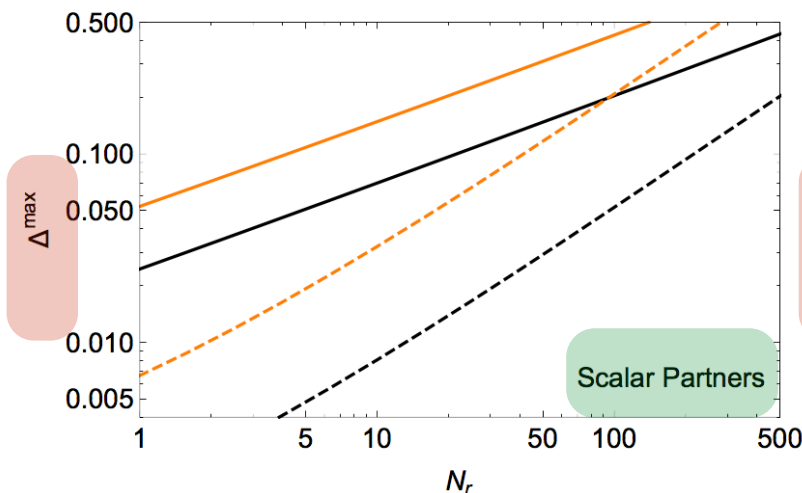


# Preview of Results

For each top partner structure...

$\Lambda_{UV}^{\text{reach}} = 10 \text{ TeV} \quad 20 \text{ TeV}$   
 $\Delta$ : — —  
 $\tilde{\Delta}$ : - - - -

.. we find the “tuning price” you have to pay to avoid any signatures @ 100 TeV or lepton colliders...



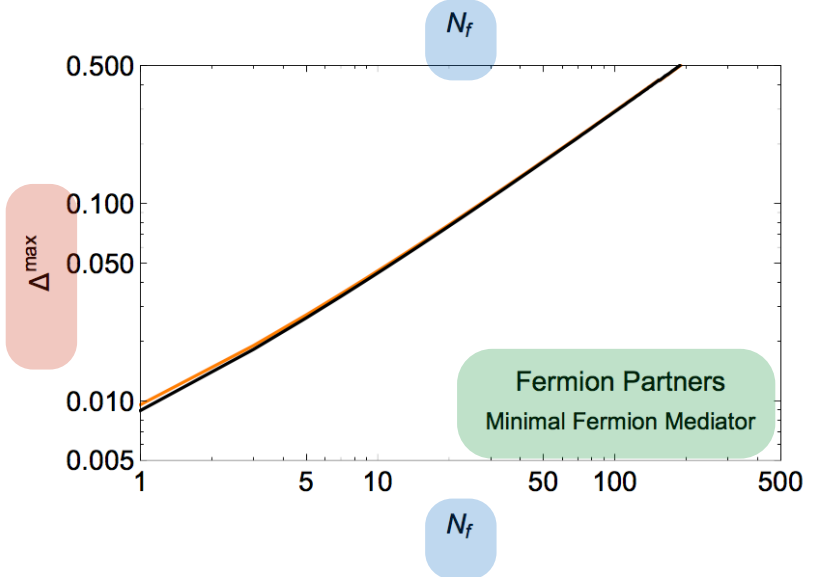
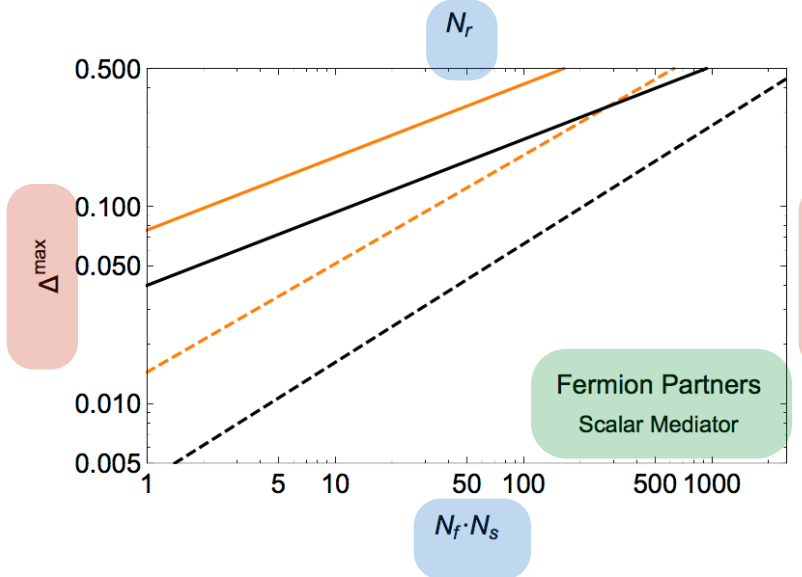
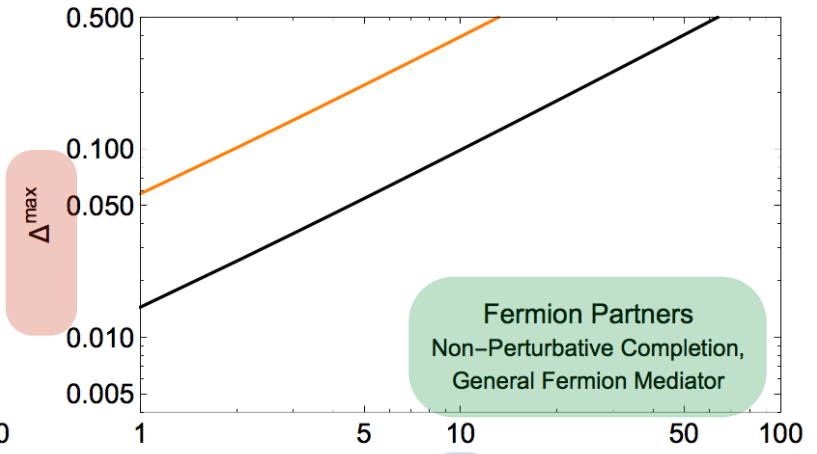
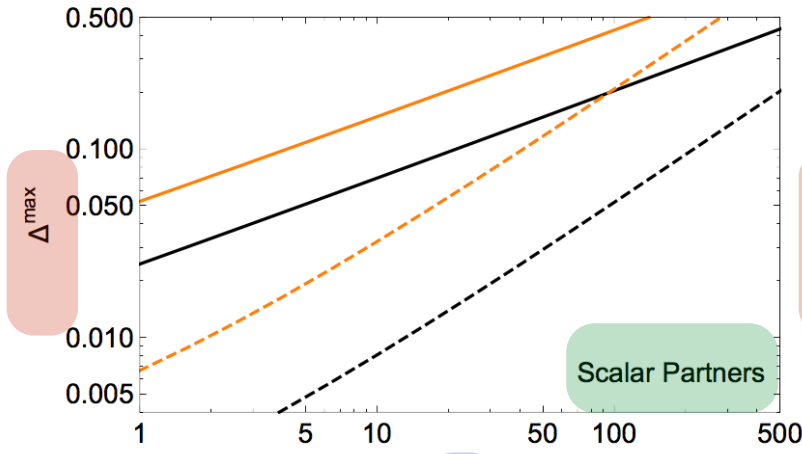
# Preview of Results

For each top

partner structure...

$\Lambda_{UV}^{\text{reach}} = 10 \text{ TeV} \quad 20 \text{ TeV}$   
 $\Delta$ : — —  
 $\tilde{\Delta}$ : - - - -

.. we find the  
 “tuning price”  
 you have to  
 pay to avoid  
 any signatures  
 @ 100 TeV  
 or lepton  
 colliders...



... as a function of the  
 number of top partner dof...

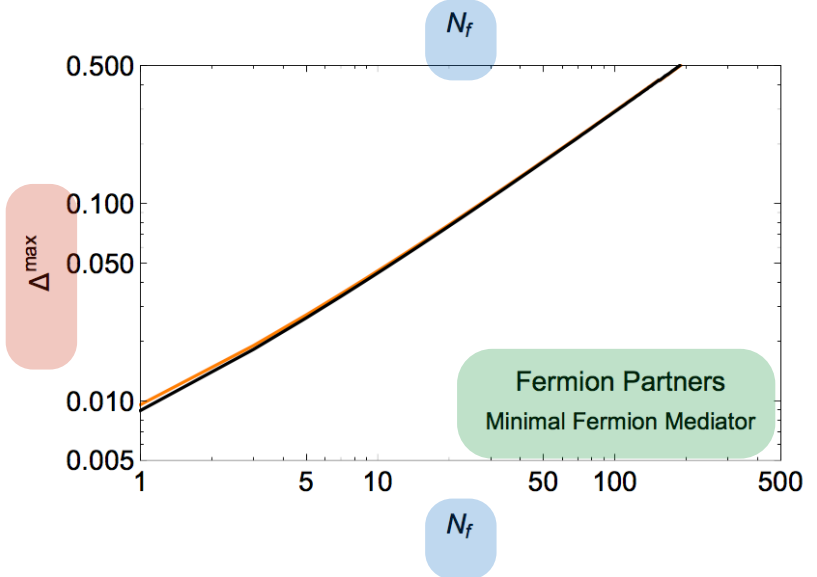
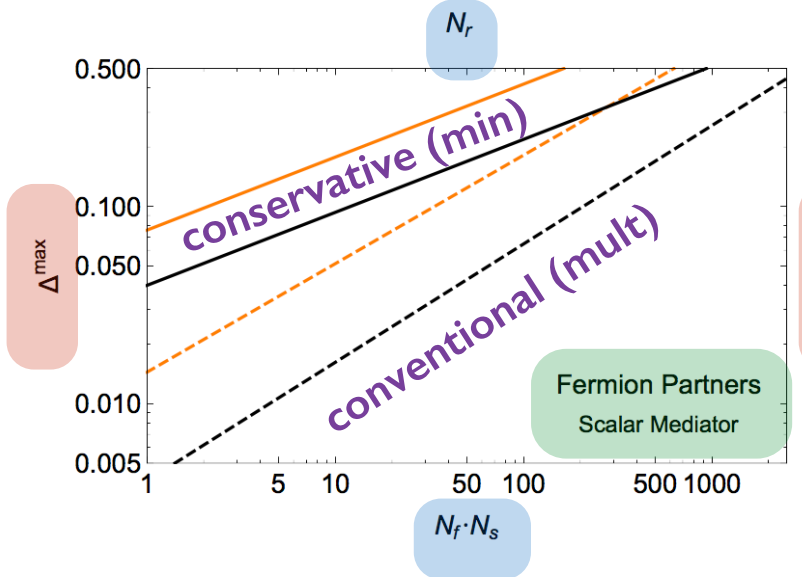
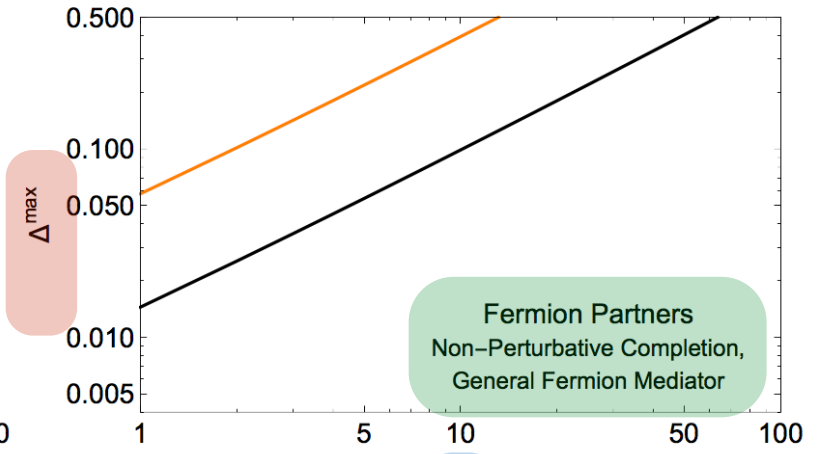
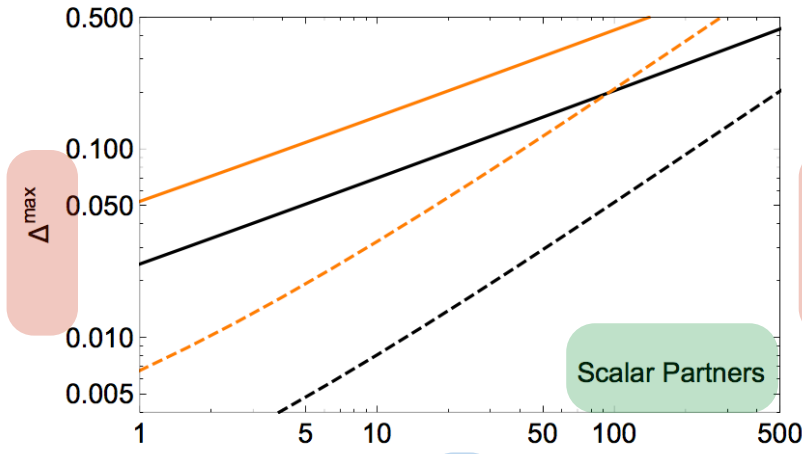
# Preview of Results

... for different ways of combining tunings and assumptions on UV reach.

reach  
 $\Lambda_{UV} = 10 \text{ TeV} \quad 20 \text{ TeV}$   
 $\Delta$ : — —  
 $\tilde{\Delta}$ : - - - -

For each top partner structure...

.. we find the “tuning price” you have to pay to avoid any signatures @ 100 TeV or lepton colliders...



... as a function of the number of top partner dof...



# Preview of Results

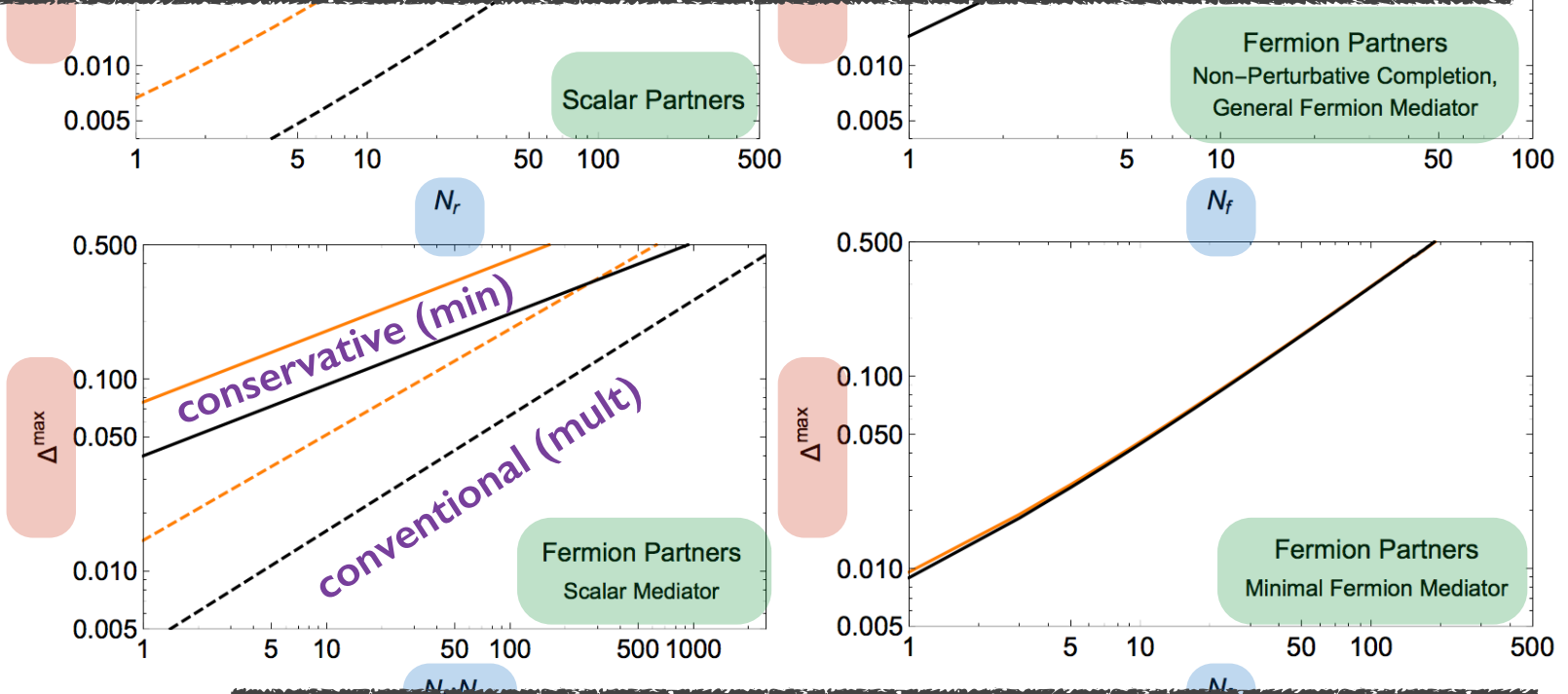
... for different ways of combining tunings and assumptions on UV reach.

reach  
 $\Lambda_{UV} = 10 \text{ TeV} \quad 20 \text{ TeV}$   
 $\Delta:$  — —  
 $\tilde{\Delta}:$  — —

For each top partner structure...

**Very conservative: only top loop etc.  
 Existing theories need UV completion at ~5 TeV  
 Even so....**

.. we find the “tuning price” you have to pay to avoid any signatures @ 100 TeV or lepton colliders...



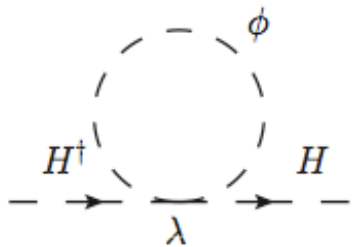
... as a function of number of top partne

**→ need many partners to avoid discovery AND tuning!**

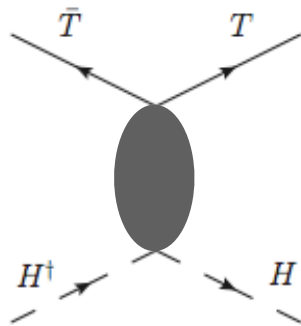
How do we get there?

# Neutral Naturalness Scenarios

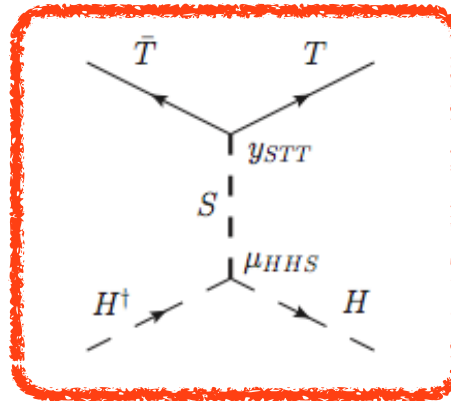
Scalar Partners



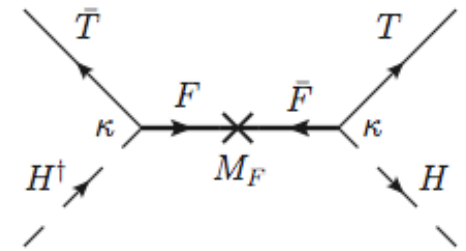
Fermion Partners  
(strong coupling)



Fermion Partners  
(scalar mediator)



Fermion Partners  
(fermion mediator)

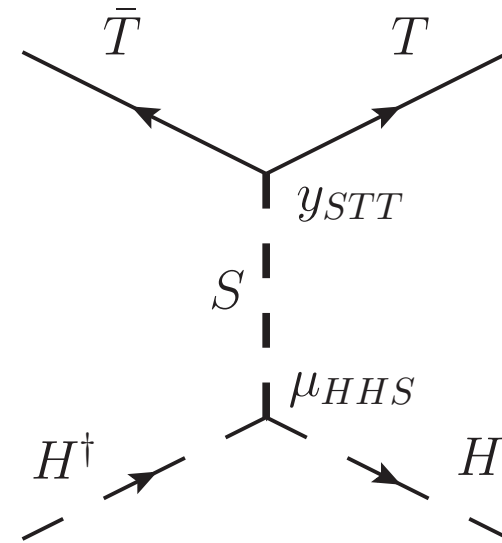


Trickiest/most interesting case  
to analyze in complete generality...

# Fermion Partner - Scalar Mediator

This is the most complicated and important case.

Contains Twin Higgs & Orbifold generalizations,  
but is much more general. 1410.6808, 1411.7393 Craig, Knapen, Longhi



Integrate out mediator(s) to match to natural IR theory:

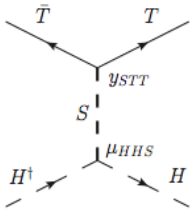
$$\mathcal{L}_T \supset \sum_i T_i \bar{T}_i \left( M_{T_i} - \frac{|H|^2}{2M'_i} \right)$$

low-energy effective Lagrangian  
to cancel top loop

$$N_s \frac{\mu_{HHS} y_{STT}}{m_S^2} = \frac{1}{2M'} = \frac{3}{2N_f} \frac{y_t^2}{M_T}$$

naturalness matching condition

# The Scalar Mediator



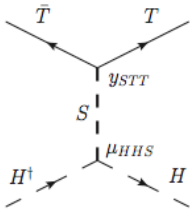
Before we can proceed, we have to know:  
**How heavy is the scalar mediator?**

**Naive expectation:** new scalars can't be light, otherwise we have another hierarchy problem!  
 $\Rightarrow m_S$  should be significantly above weak scale!

**Naive counterargument:** we know of many ways to solve the hierarchy problem! Dress up mediator sector with partners etc...

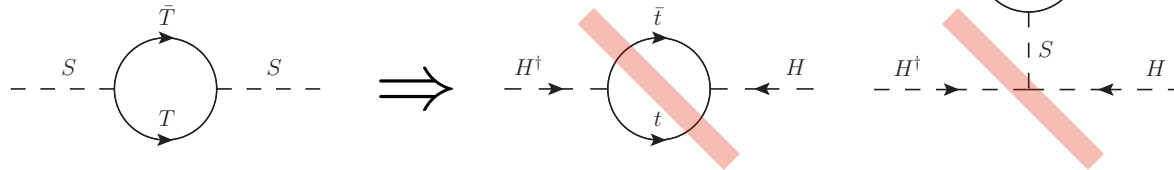
**Nope!**

# The Scalar Mediator



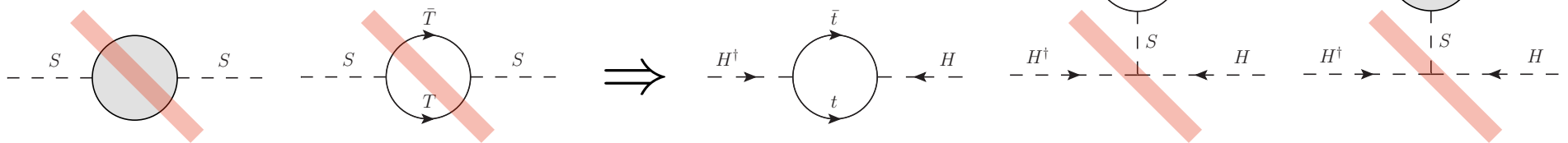
## Sacrificial Scalar Mechanism

$S$  unprotected



$H$  stabilized

$S$  stabilized



$H$  unprotected

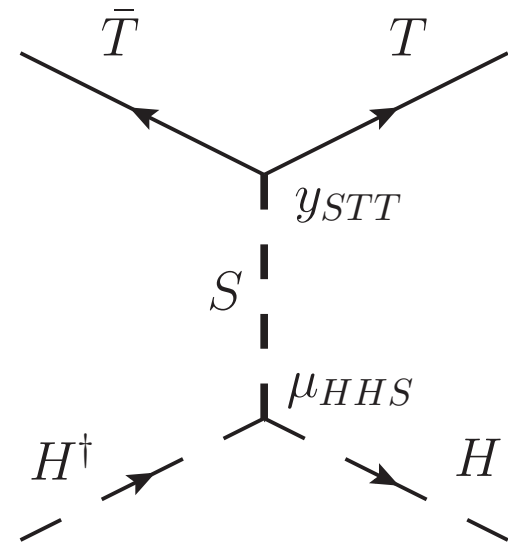
## Consequences:

1. Mass of scalar is tied to UV completion scale!
2.  $m_S \gg m_h$  makes it easy to compute experimental signals.

# Higgs Mixing

Take one scalar mediator  $S$

*(generalizes simply)*



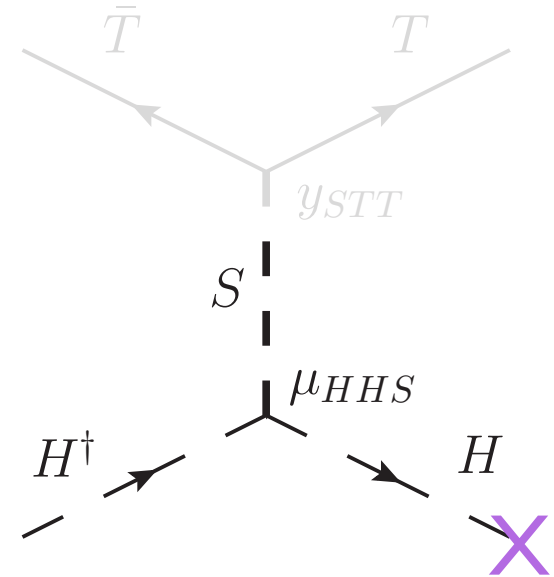
# Higgs Mixing

## Take one scalar mediator $S$

(generalizes simply)

In the  $m_S \gg m_h$  limit,  
mixing angle is simple:

$$s_\theta \approx -\frac{\mu_{HHS}}{m_S^2} v$$





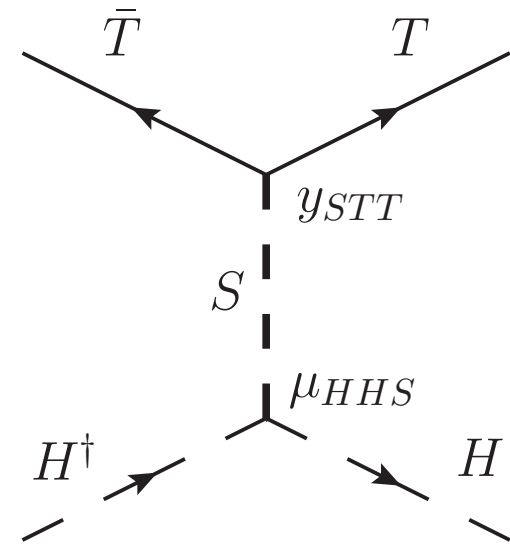
# Computing Observables

## Take one scalar mediator $S$

(generalizes simply)

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mixing angle is simple:

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## Naturalness condition:

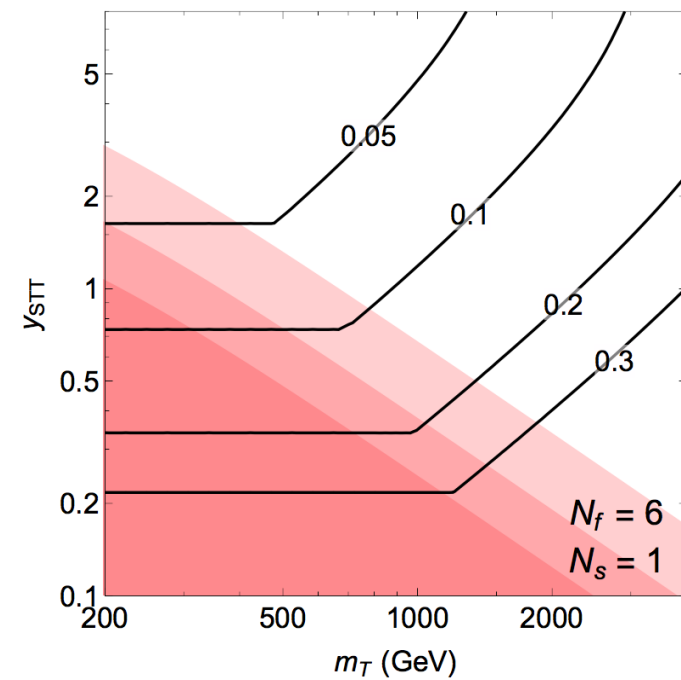
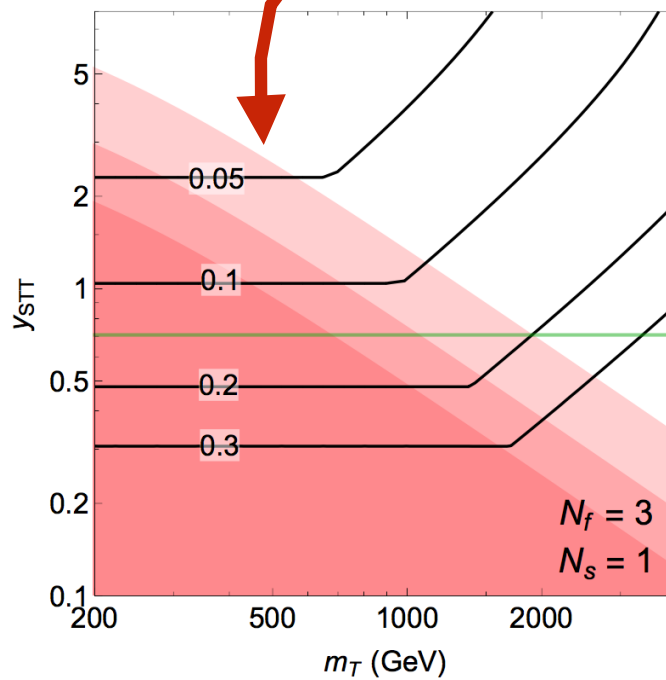
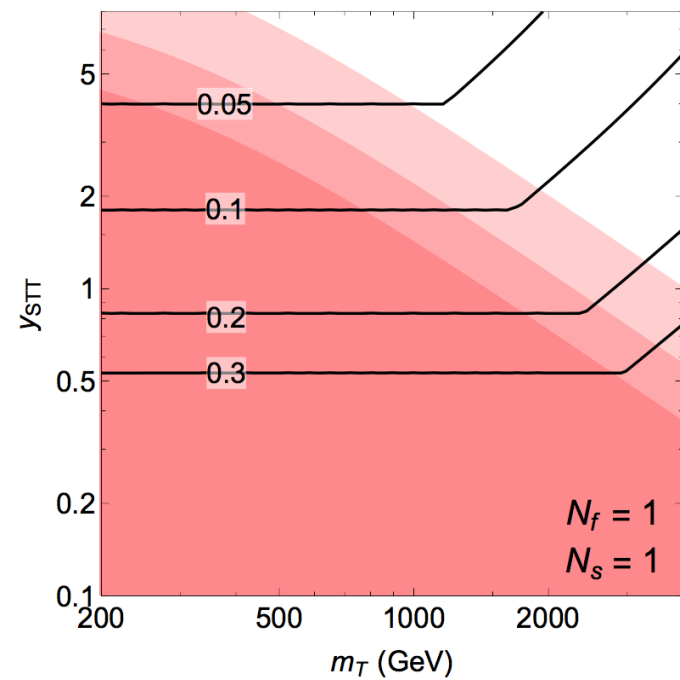
$$\frac{\mu_{HHS} y_{SST}}{m_S^2} = \frac{3}{2N_f} \frac{y_t^2}{M_T} \longrightarrow s_\theta \approx -\frac{3}{2N_f} \frac{y_t^2}{y_{SST}} \frac{v}{M_T}$$

Mediator mass drops out! Only depends on  $(M_T, y_{SST})$

# Higgs Mixing in $(m_T, y_{STT})$ Plane

Lepton colliders have great sensitivity in much of parameter space.

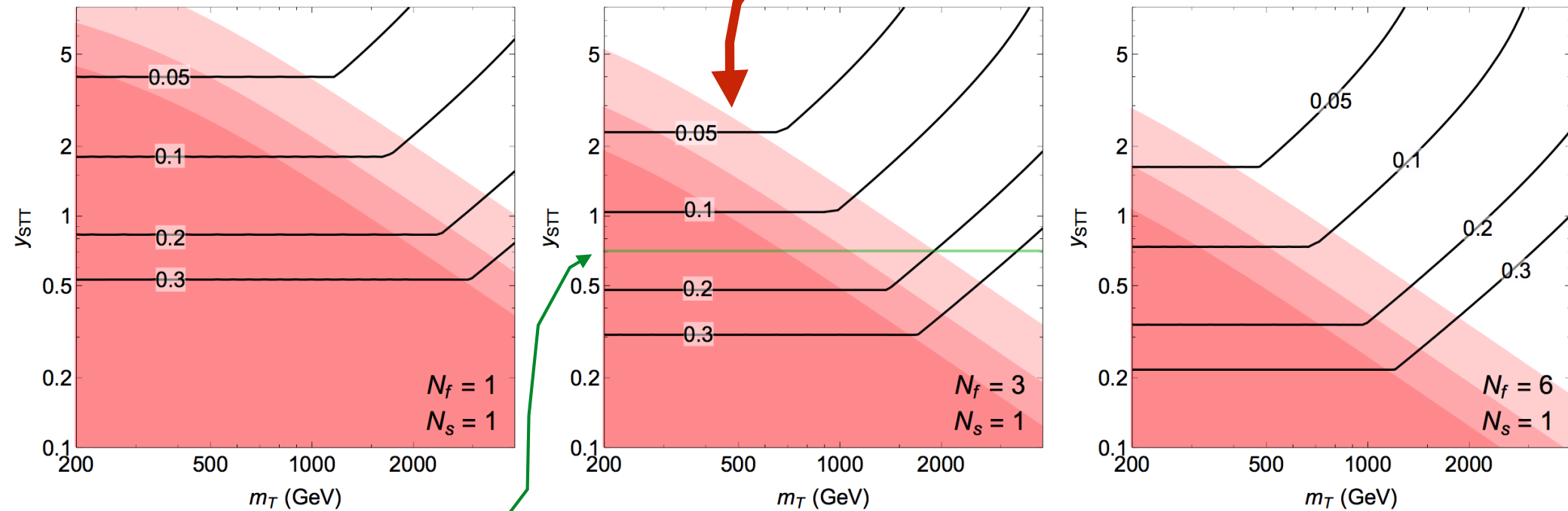
■ ILC250 ( $\delta\sigma_{Zh} > 5.2\%$ )   ■ ILC250 LumiUp ( $\delta\sigma_{Zh} > 2.4\%$ )   ■ FCC-ee ( $\delta\sigma_{Zh} > 0.8\%$ )   —  $\text{Min}_{m_s} (\Delta_{h(s)}, \Delta_{s(h)})$  for  $\Lambda_{UV} = 20 \text{ TeV}$



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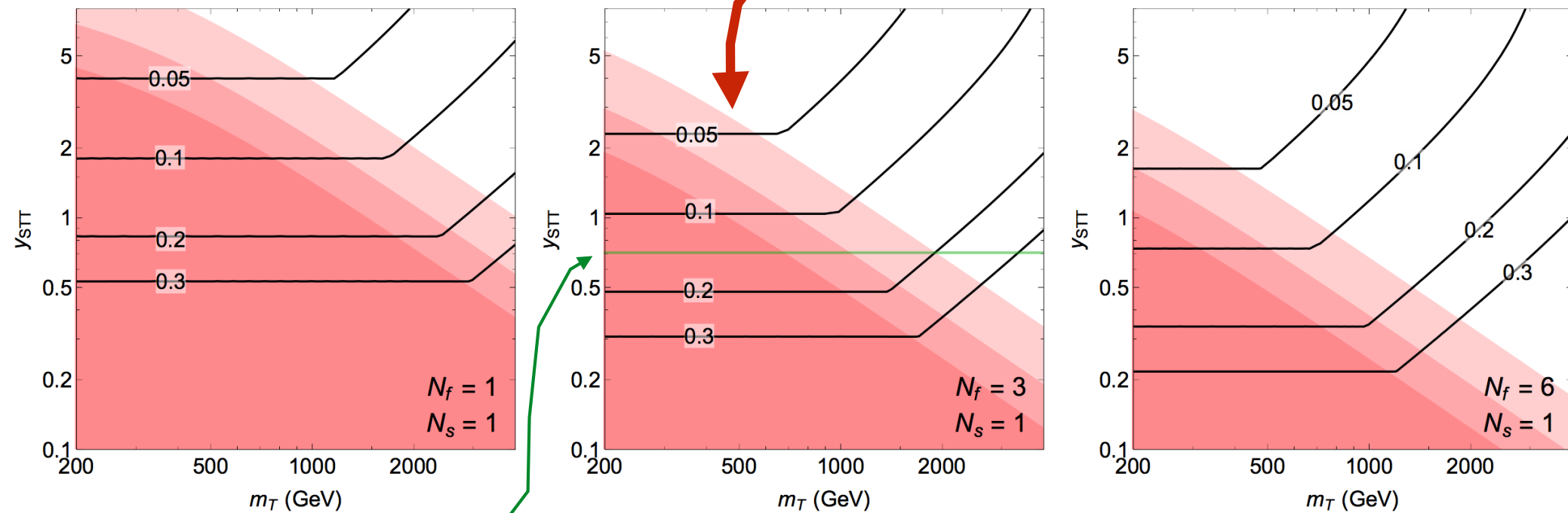


*Twin Higgs models are subspaces (lines) in this more general parameter space.*

# Higgs Mixing in $(m_T, y_{STT})$ Plane

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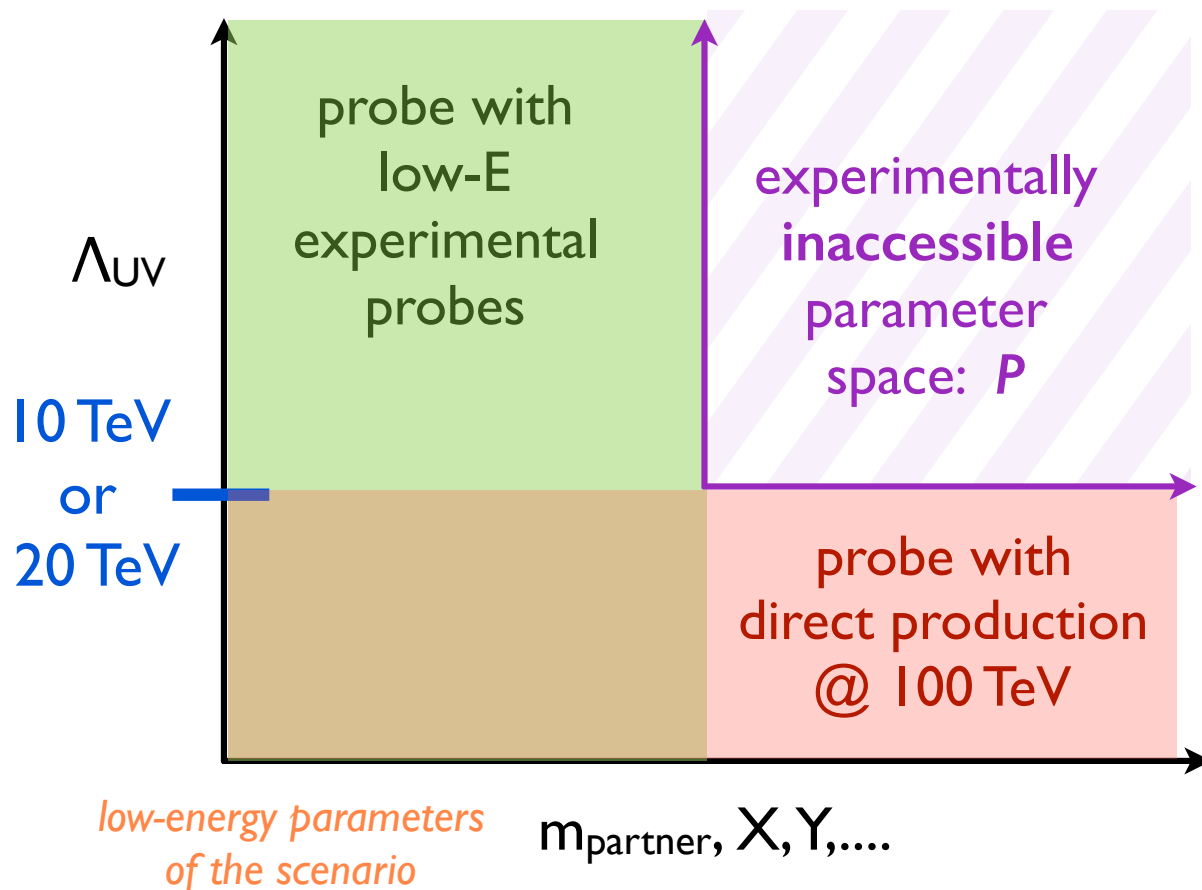
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*Twin Higgs models are subspaces (lines) in this more general parameter space.*

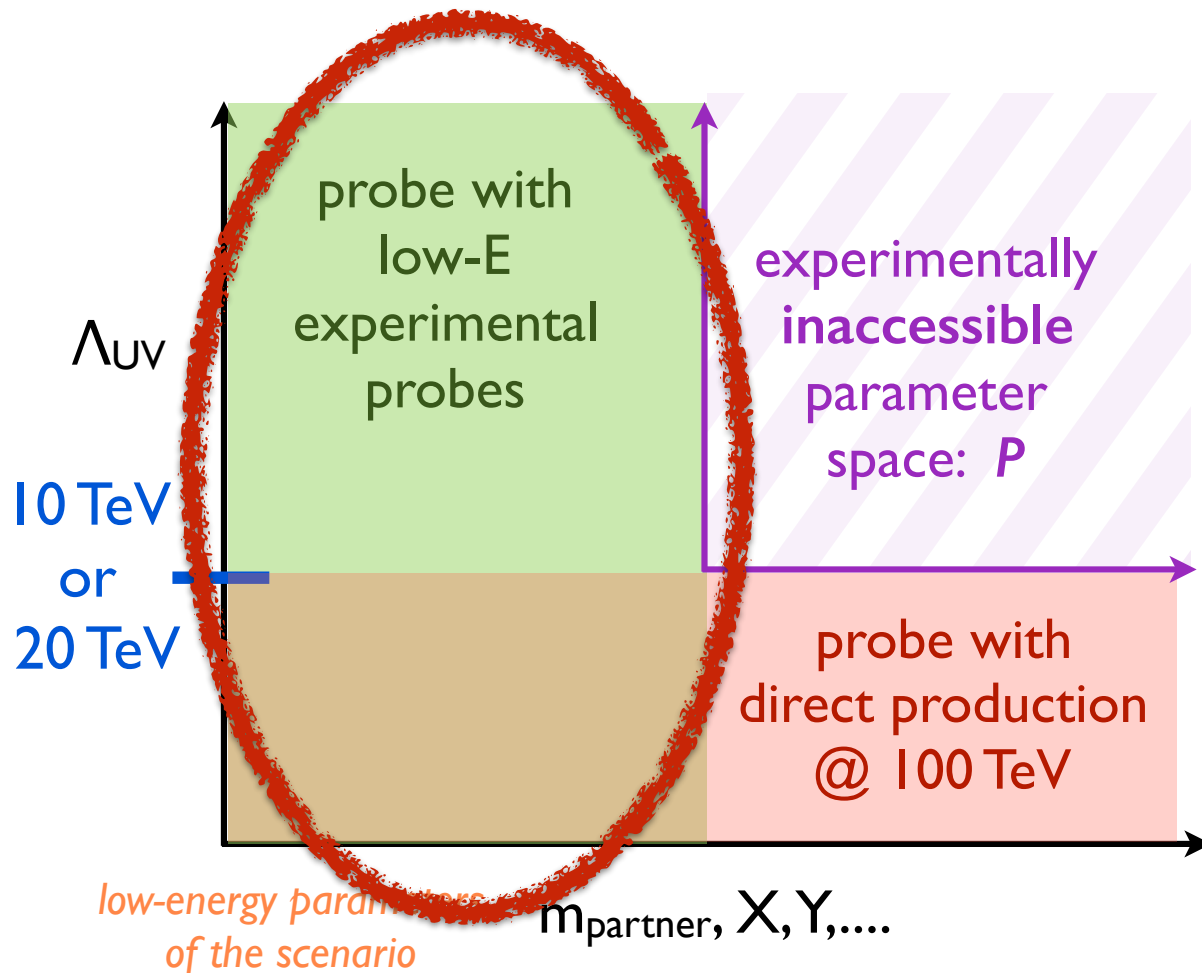
**But what if  $y_{STT}$  is large??**

# Recall our main strategy:



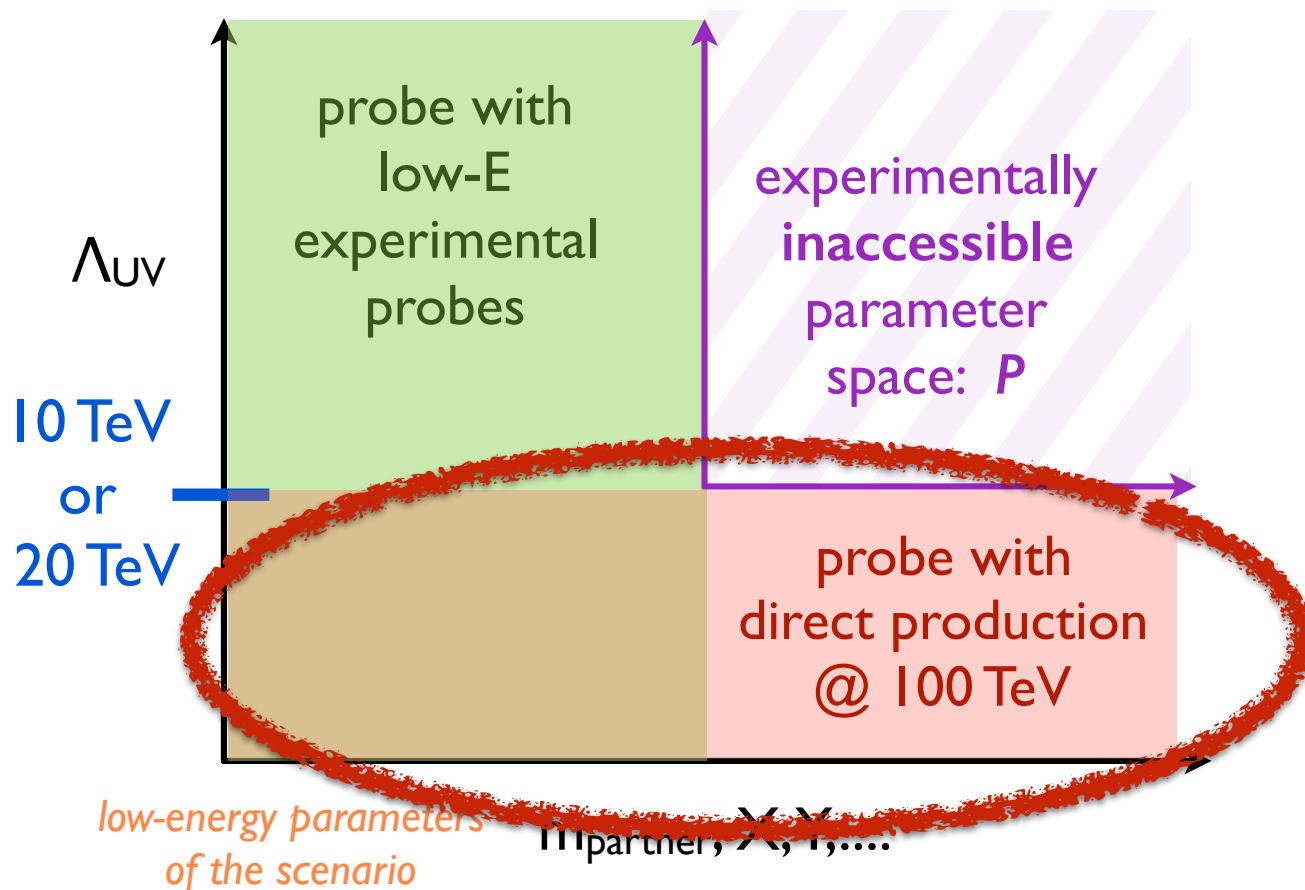
# Recall our main strategy:

We've determined the reach of low-energy observables (higgs mixing).



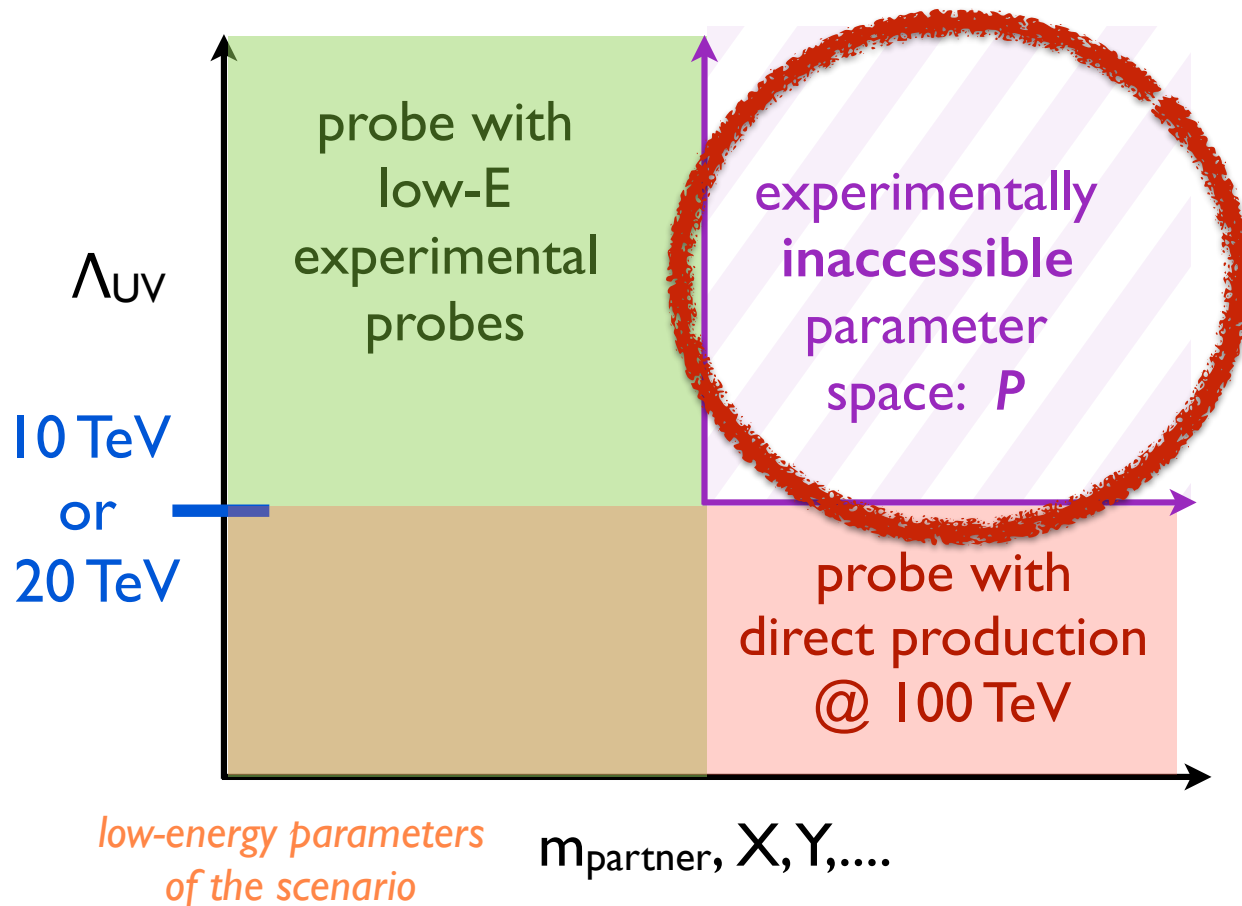
# Recall our main strategy:

Now we exploit the 100 TeV collider's ability to probe the UV scale.



# Recall our main strategy:

Assuming 10 or 20 TeV can be probed, what unavoidable tuning are we stuck with?





# Tunings (I)

$\Delta_{h(S)} = \log$  tuning of  $m_h$  from mediator loops.

*(have to differentiate case where Higgs = PNOB from case without such symmetries...)*

**Gets worse with large  $m_s$ !**

$\Delta_{S(T)} = \log$  tuning from quadratic sensitivity of  $m_s$  to T loops  
(required by Sacrificial Scalar Mechanism!)

**Gets better with large  $m_s$ !**

*Can find conservative tuning estimate by maximizing over (unknown) mediator mass!*

$$\Rightarrow \Delta_{H,S} = \text{Max}_{m_s} f(\Delta_{h(S)}, \Delta_{S(T)})$$

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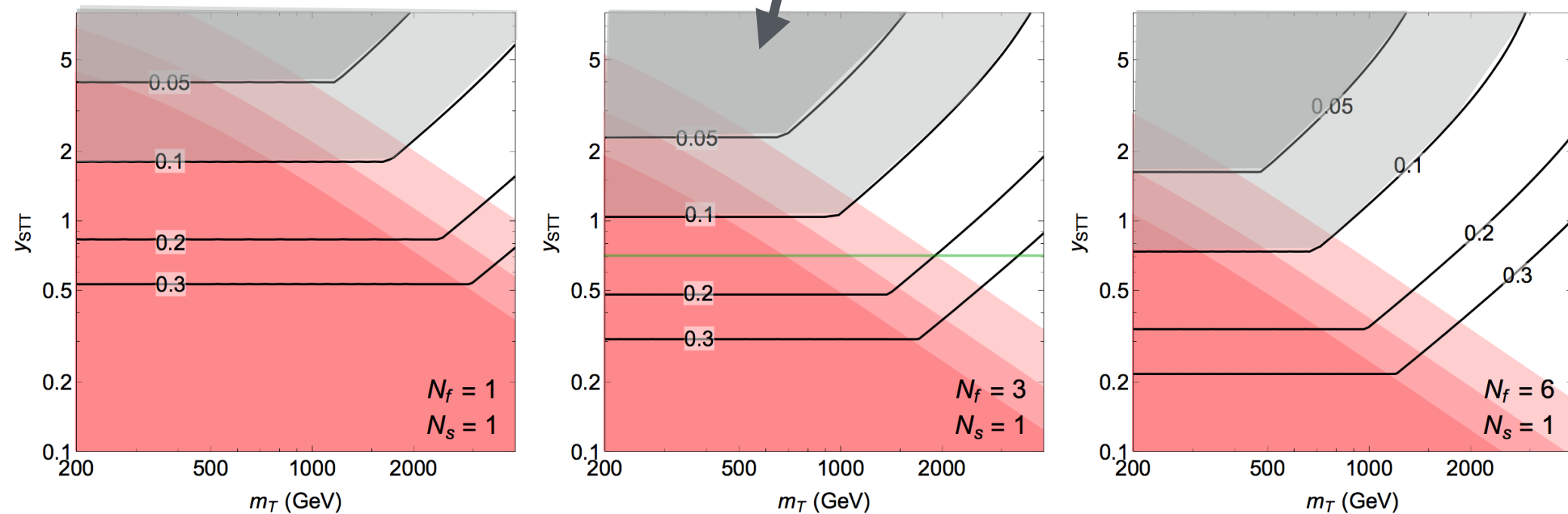
$$\Rightarrow \Delta_{H,S} = \text{Max}_{m_s} f(\Delta_{h(S)}, \Delta_{S(T)})$$

Since we marginalize over  $m_s$ ,  $\Delta_{H,S}$  is uniquely defined in the  $(m_T, y_{STT})$  plane as the tuning from the mediator sector.

# Tuning from Mediator in $(m_T, y_{STT})$ Plane

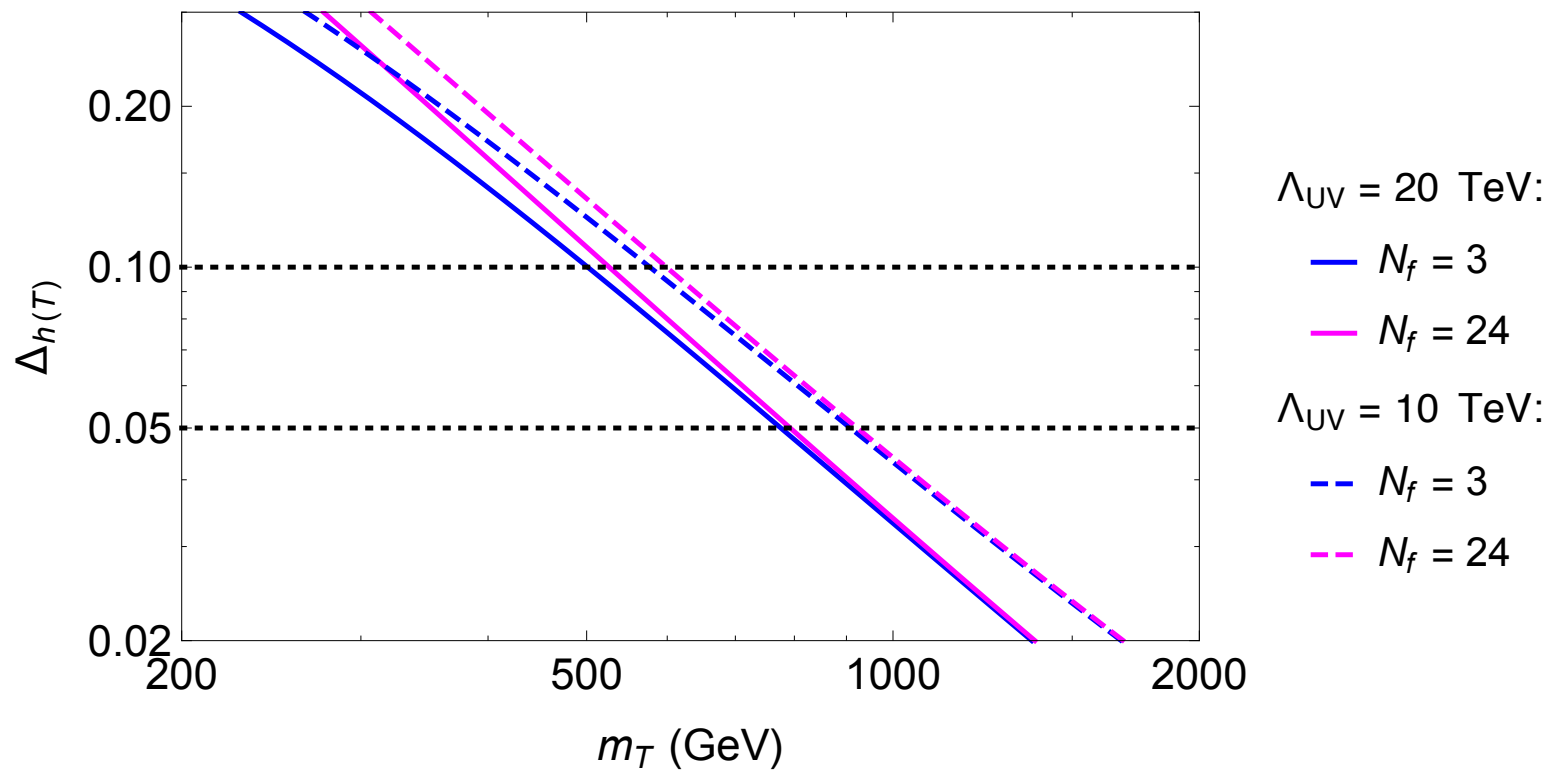
For  $\Lambda_{UV} \geq 20$  TeV (*undetectable by 100 TeV*), high  $y_{STT}$  is badly tuned!

■ ILC250 ( $\delta\sigma_{Zh} > 5.2\%$ )   ■ ILC250 LumiUp ( $\delta\sigma_{Zh} > 2.4\%$ )   ■ FCC-ee ( $\delta\sigma_{Zh} > 0.8\%$ )   —  $\text{Min}_{m_s} (\Delta_{h(s)}, \Delta_{s(h)})$  for  $\Lambda_{UV} = 20$  TeV



# Tunings (2)

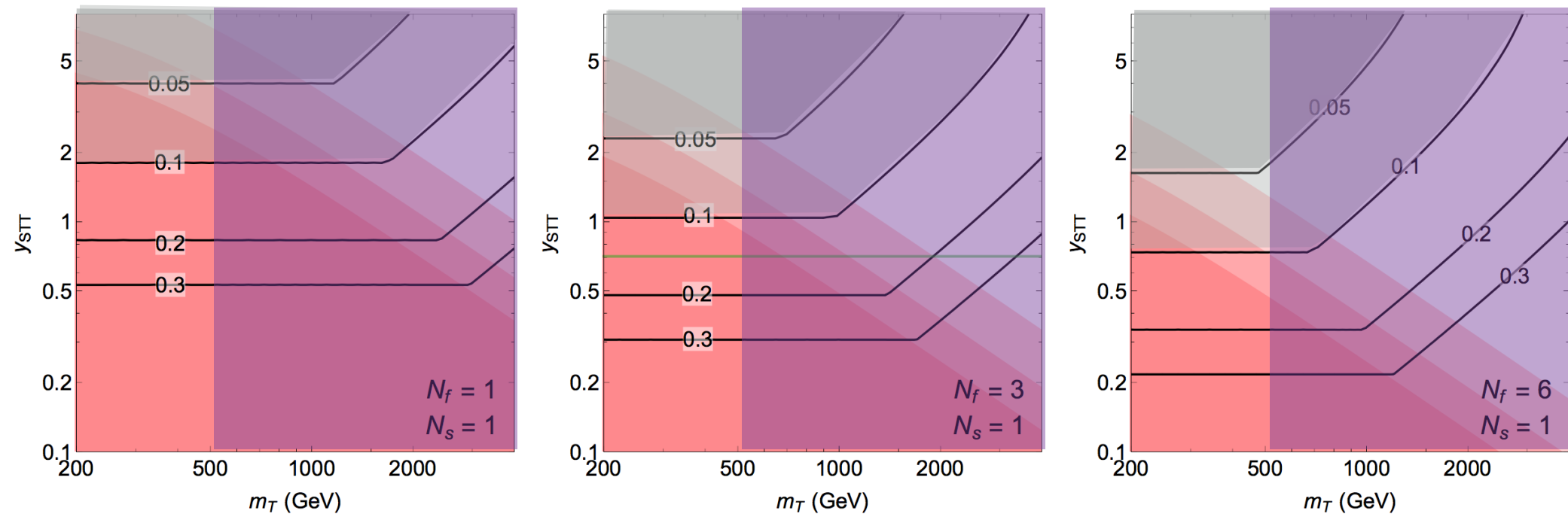
For  $\Lambda_{UV} \geq 20$  TeV (*undetectable by 100 TeV*), top partners heavier than  $\sim 500$  GeV give log-tuning to Higgs mass worse than 10%



# Log tuning from $t$ vs $T$ in $(m_T, y_{STT})$ Plane

For  $\Lambda_{UV} \cong 20 \text{ TeV}$  (*undetectable by 100 TeV*), top partners heavier than  $\sim 500 \text{ GeV}$  give log-tuning to Higgs mass worse than 10%

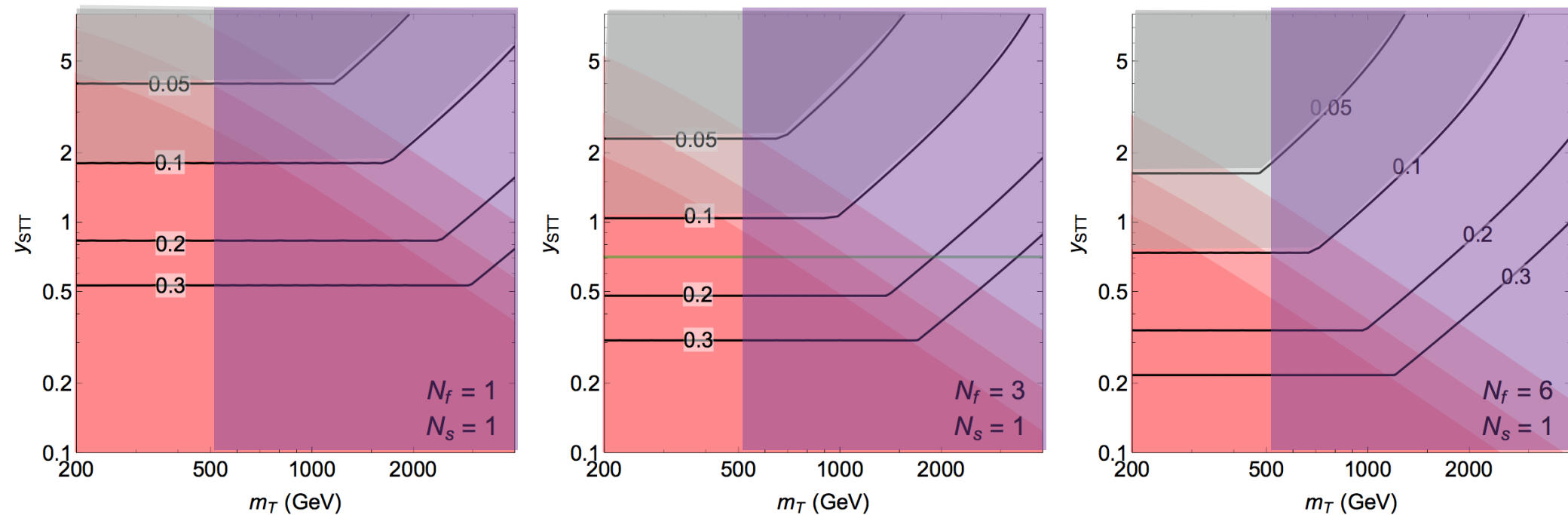
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# Log tuning from $t$ vs $T$ in $(m_T, y_{STT})$ Plane

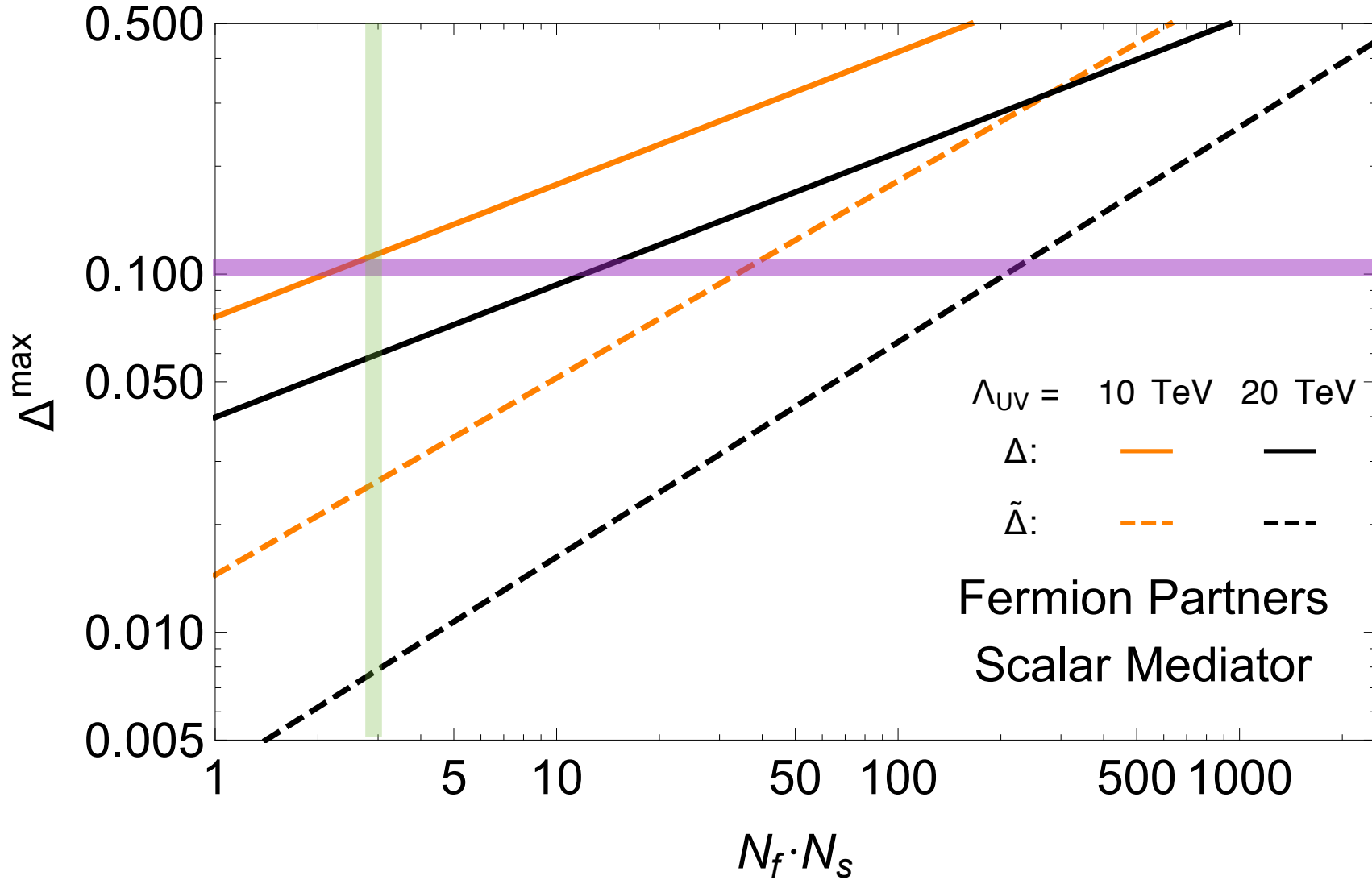
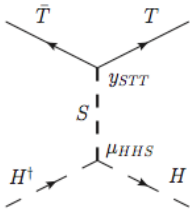
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**No untuned parameter space left for  
 $N_f \times N_s \sim O(\text{SM})!$**

# Fermion Partner - Scalar Mediator



**A natural theory needs to have VERY MANY fermion partners/scalar mediators to possibly escape detection.**

# Need both colliders for full coverage!

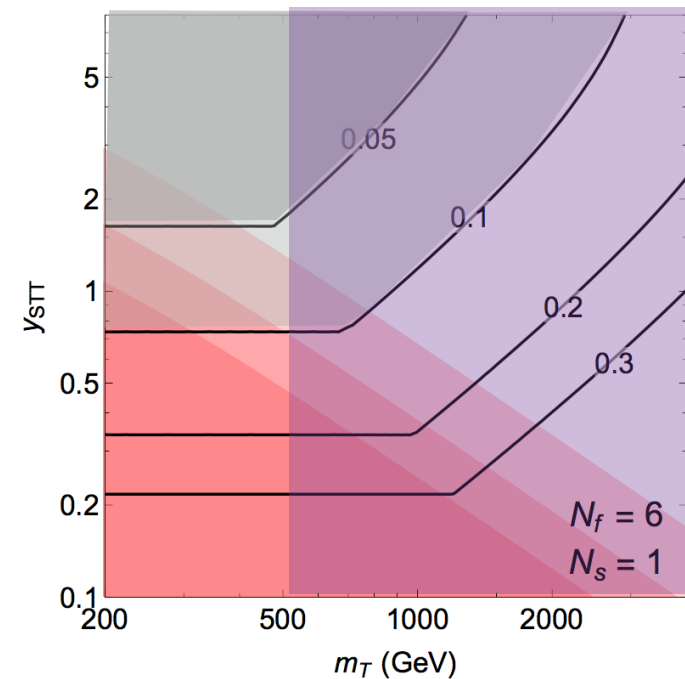
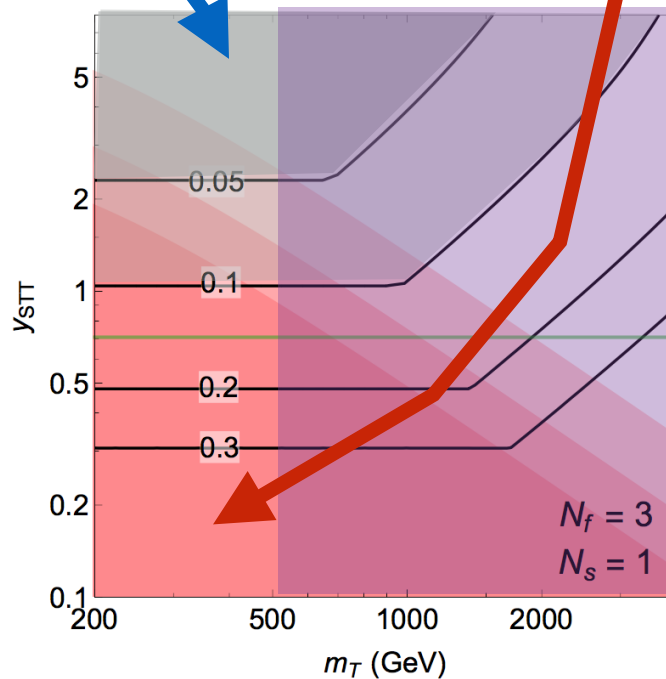
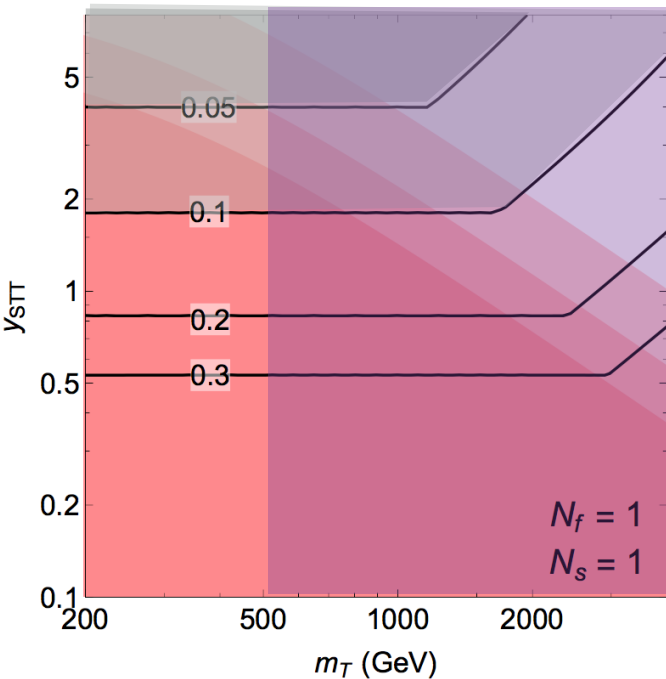
Large hidden sector coupling:  
Higgs mixing is tiny, but need low  $\Lambda_{UV}$ .

No guaranteed signal at lepton collider,  
but slam dunk at 100 TeV!

Small hidden sector coupling:  
theory can be healthy even for very large  $\Lambda_{UV}$ ,  
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No guaranteed 100 TeV signals,  
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# Need both colliders for full coverage!

Large hidden sector coupling:  
Higgs mixing is tiny, but need low  $\Lambda_{UV}$ .

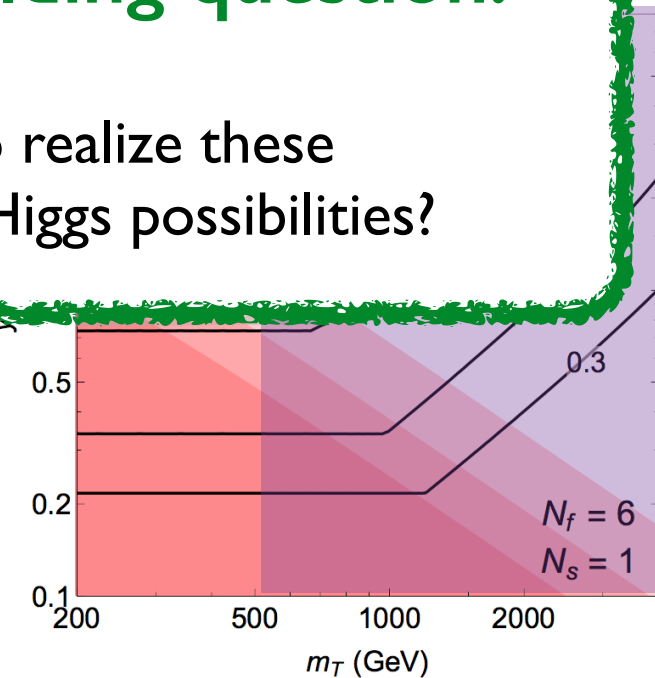
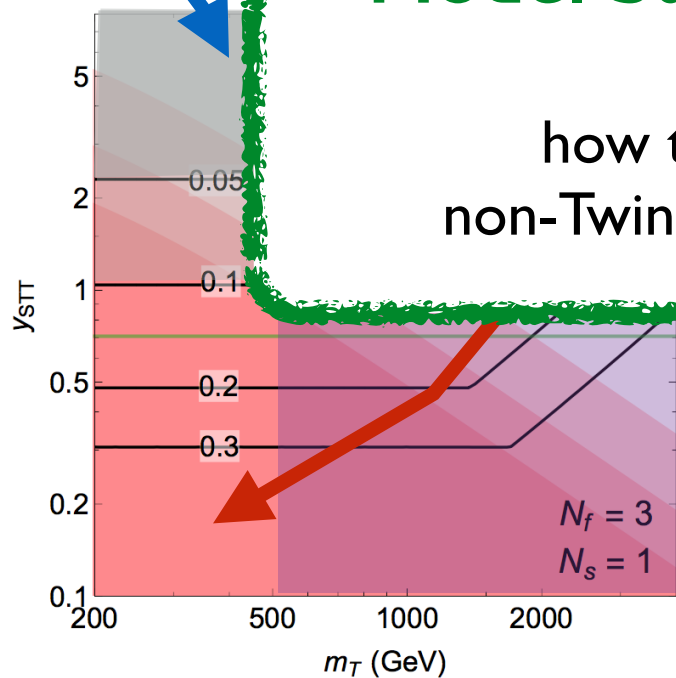
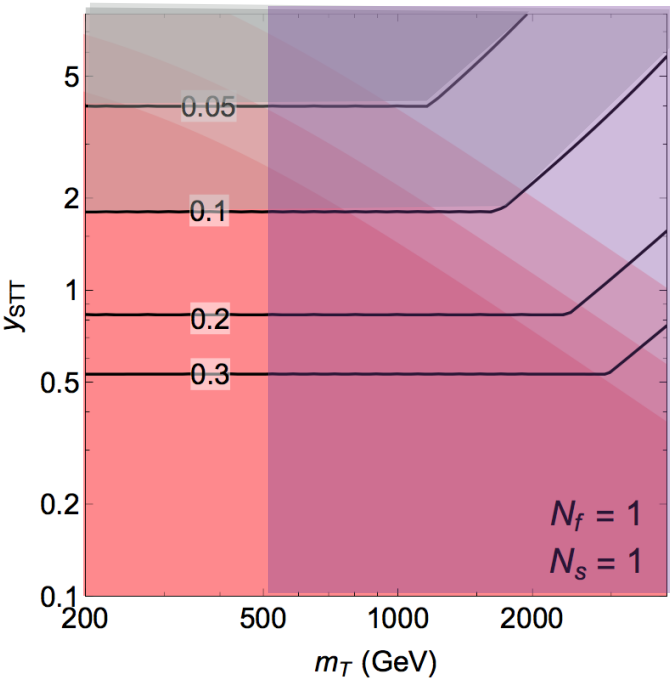
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No guaranteed 100 TeV signals,  
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ILC250 ( $\delta\sigma_{Zh} > 5.2\%$ )    ILC250 Luminosity ( $\delta\sigma_{Zh} > 5.2\%$ )

**Model building question:**  
how to realize these non-Twin-Higgs possibilities?



... go through corresponding derivations  
for the other scenarios, with similar  
conclusions....

**What's the upshot?**

# 1. Great discovery potential TODAY

DC, Verhaaren 1506.06141

Chacko, DC, Verhaaren, 1512.XXXXX

*Long-lived hidden sector states (mirror glueballs, quarkonia) generate spectacular displaced signals that allow the LHC to probe TeV uncolored top partners*

## 2. Implications for LHC searches

*Displaced Vertex searches with just one DV + VBF or lepton are required. Also, need sub-mm decay length reconstruction.*

HXSWG yellow report (soon!)

### 3. No-Lose Theorem:

*Any theory of  $\sim 10\%$  naturalness with  $O(SM)$  top partners will be discovered at a planned lepton collider and/or 100 TeV*

→ *Model-independent (bottom-up) and very conservative (only top loop etc)*

How to avoid this theorem?

Could have **top partner swarms, or neutral top partners without SM charges in UV completion.**

There might also be weird non-perturbative or stringy constructions that don't need top partners?

## 4. Implications for future colliders

*Both lepton collider and 100 TeV have to work in tandem for full coverage of general naturalness*

Without lepton collider:

*could miss theory with large-ish Higgs mixing but small hidden sector couplings  $\rightarrow$  very high UV completion scale out of 100 TeV collider reach*

Without 100 TeV:

*several scenarios give small IR signatures, need to probe UV*

## 5. For full coverage, need to probe UV completion!

*Central assumption of SM-charged BSM states at  $\Lambda_{UV}$  allows us to make these very powerful conclusions.*

This seems very reasonable, and is certainly the case in all currently proposed UV completions.

Can we formally prove this always has to be the case, or construct counter-examples?

# Summary

## 1. Discovery potential TODAY

*Neutral naturalness motivates spectacular displaced signatures that give the LHC TeV-reach for uncolored top partners.*

## 2. Implications for LHC searches

*Need searches with just one DV + lepton or VBF, and sub-mm decay-length reconstruction for full coverage*

## 3. No-Lose Theorem

*Any theory of  $\sim 10\%$  naturalness with  $O(SM)$  top partners will be discovered at a planned lepton collider and/or 100 TeV*

## 4. Implications for future colliders

*Both lepton collider and 100 TeV have to work in tandem for full coverage of general naturalness*

## 5. Probing UV completion is vital!

*Can we formally prove that full that SM-charged BSM states appear at  $\Lambda_{UV}$  in full symmetry-based theories?*

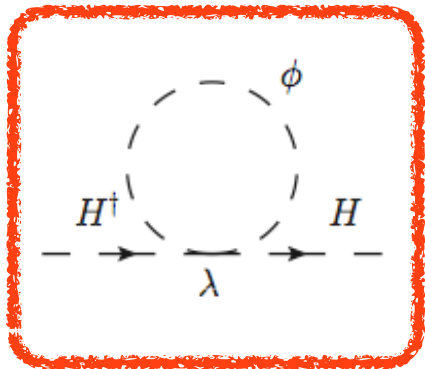
# Thank you!



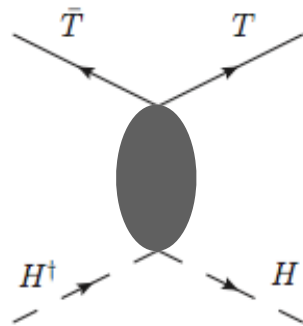
# Backup Slides

# Neutral Naturalness Scenarios

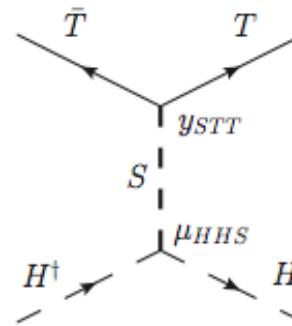
Scalar Partners



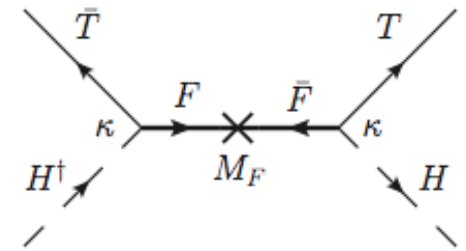
Fermion Partners  
(strong coupling)



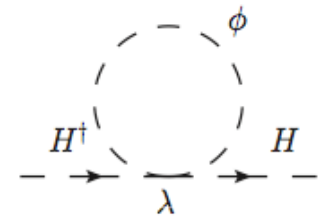
Fermion Partners  
(scalar mediator)



Fermion Partners  
(fermion mediator)

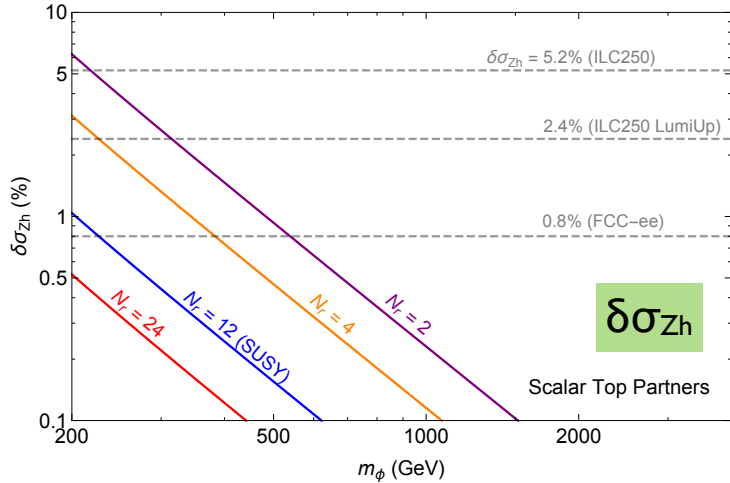


# Scalar Partner



1305.5251 Craig, Englert, McCullough

1409.0005: DC, Meade, Yu  
1412.0258 Craig, Lou, McCullough, Thalappilil



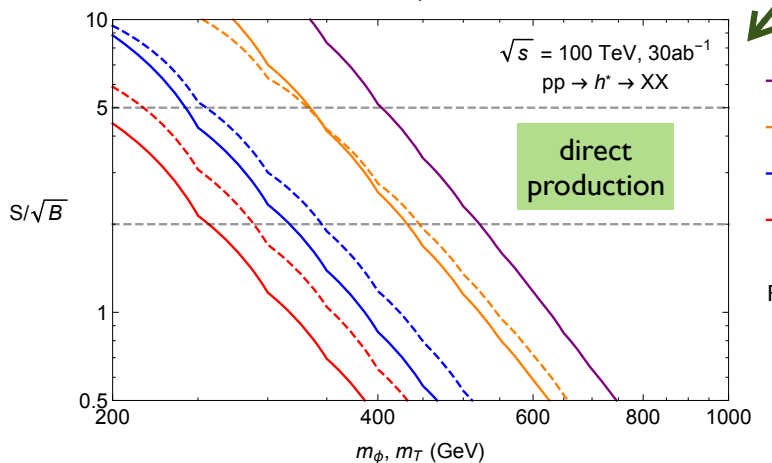
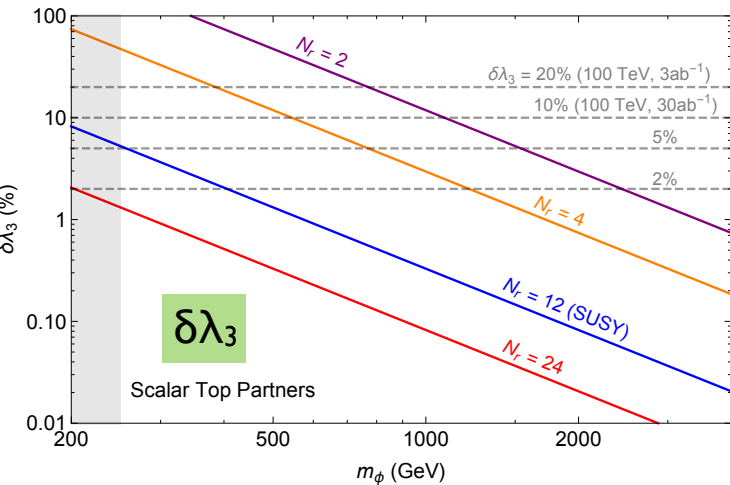
Low-energy probes only have reach of few 100 GeV

Two tunings in theory:

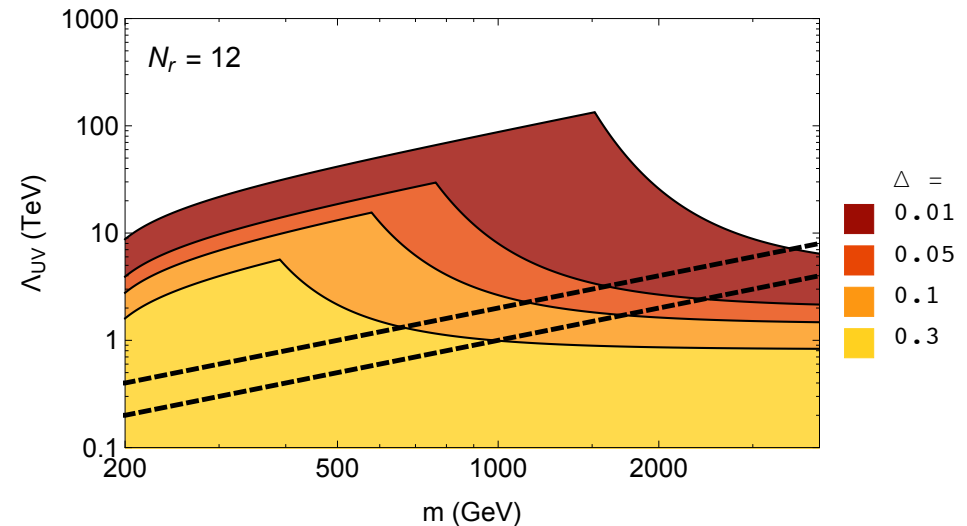
$\Delta_{h(\phi)}$  = log tuning from incomplete t- $\phi$  cancellation

$\Delta_{\phi(h)}$  from quadratically divergent mass contribution due to higgs loops

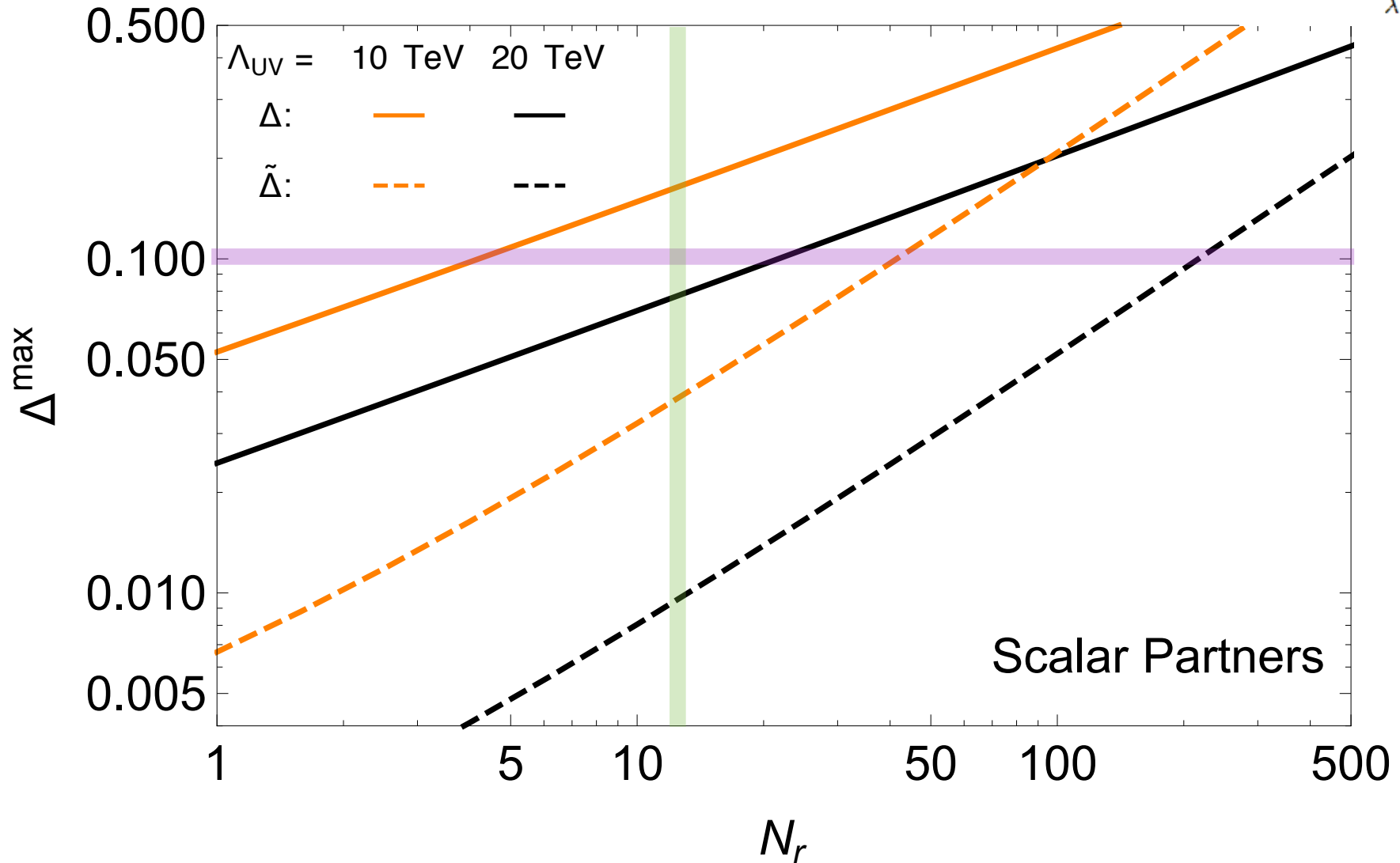
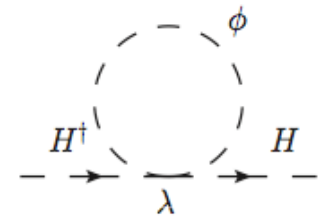
For given  $\Delta_{tot}$ , find largest allowed  $\Lambda_{UV}$ :



- Scalar Partners
- $N_r = 2$
- $N_r = 4$
- $N_r = 12$  (SUSY)
- $N_r = 24$
- Fermion Partners
- -  $N_r = 1$
- -  $N_r = 3$  (TH)
- -  $N_r = 6$



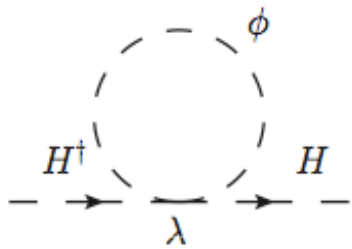
# Scalar Partner



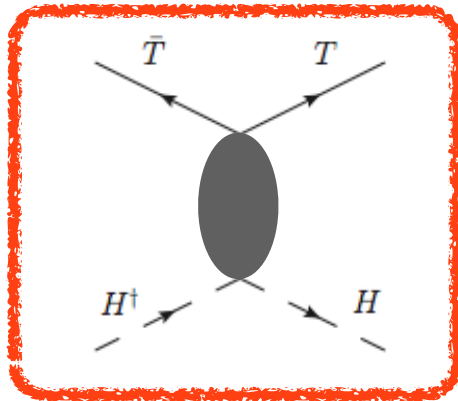
**A natural theory needs to have VERY MANY scalar partners to possibly escape detection.**

# Neutral Naturalness Scenarios

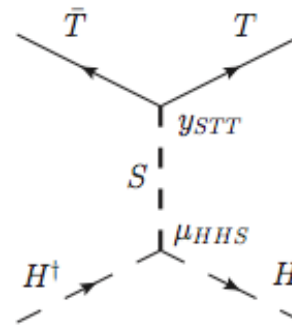
Scalar Partners



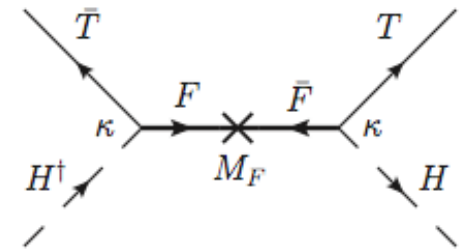
Fermion Partners  
(strong coupling)



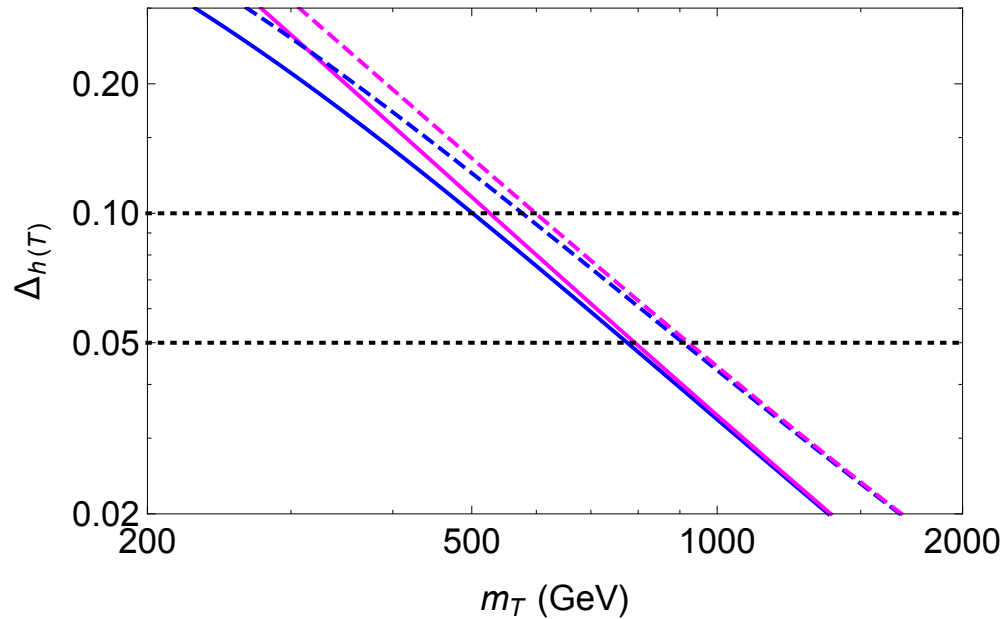
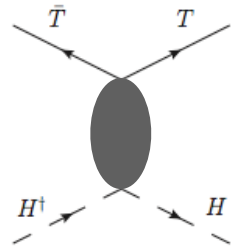
Fermion Partners  
(scalar mediator)



Fermion Partners  
(fermion mediator)



# Fermion Partner - Strong Coupling



$\Lambda_{UV} = 20$  TeV:

—  $N_f = 3$

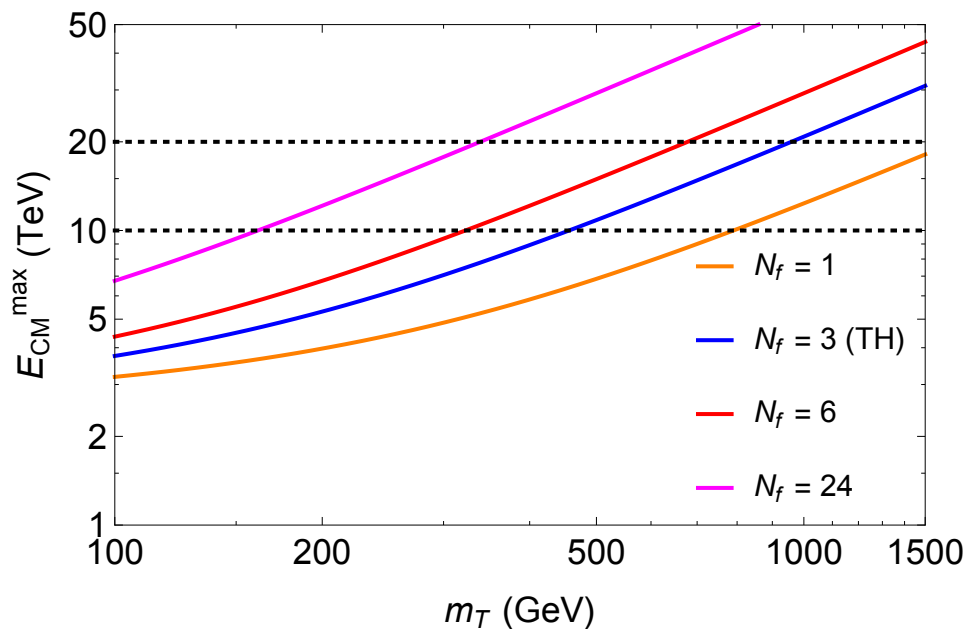
—  $N_f = 24$

$\Lambda_{UV} = 10$  TeV:

- -  $N_f = 3$

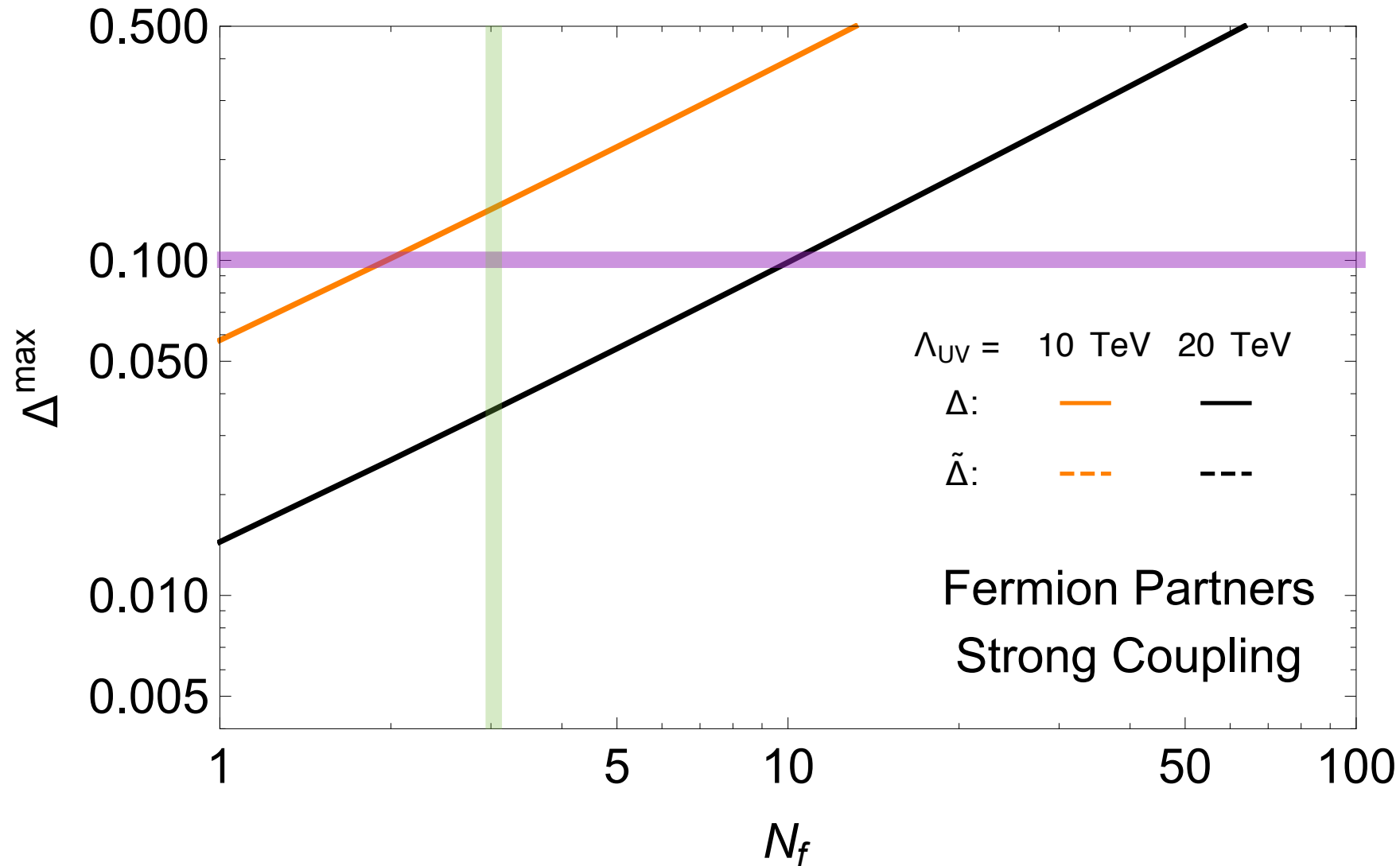
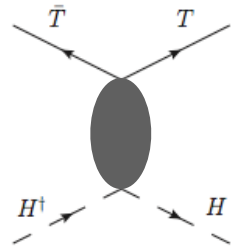
- -  $N_f = 24$

Log tuning of higgs mass:  
for  $\Lambda_{UV} < 10 - 20$  TeV,  
 $m_T \lesssim 500$  GeV  
OR  
tuning worse than 10%.



Unitarity constraints place  
*strict* upper bound on  $\Lambda_{UV}$  where  
new physics must get resolved.

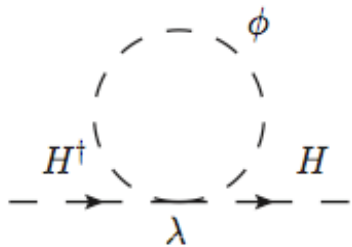
# Fermion Partner - Strong Coupling



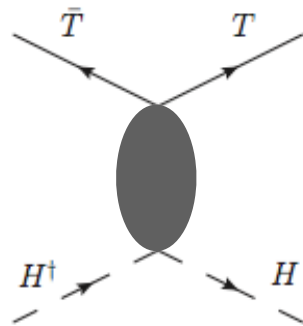
**A natural theory needs to have VERY MANY fermion partners to possibly escape detection.**

# Neutral Naturalness Scenarios

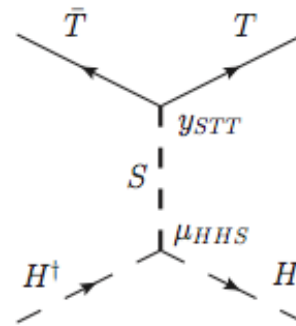
Scalar Partners



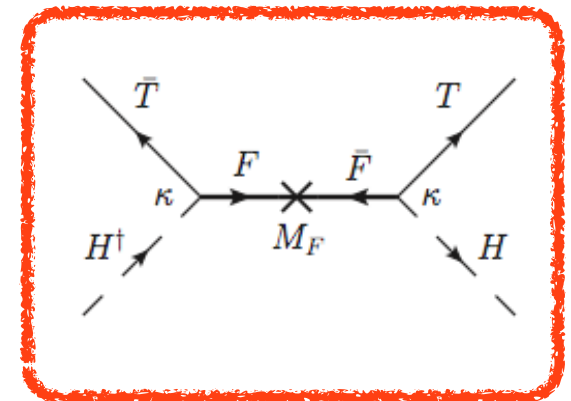
Fermion Partners  
(strong coupling)



Fermion Partners  
(scalar mediator)

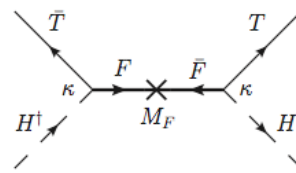


Fermion Partners  
(fermion mediator)



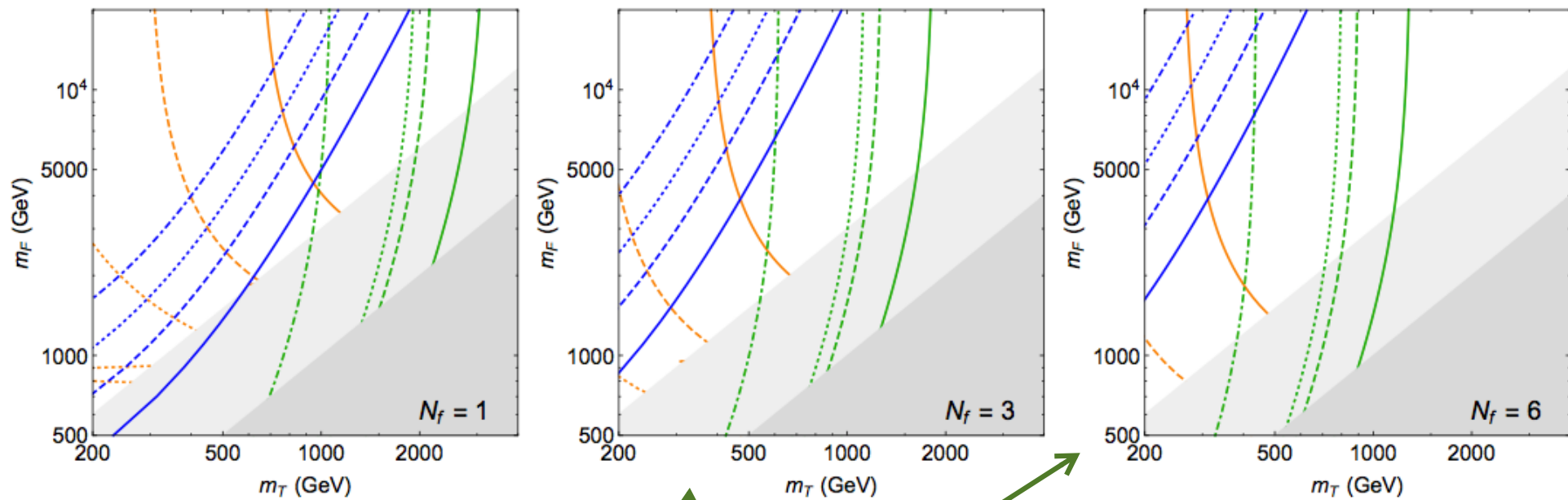


# Fermion Partner - Fermion Mediator



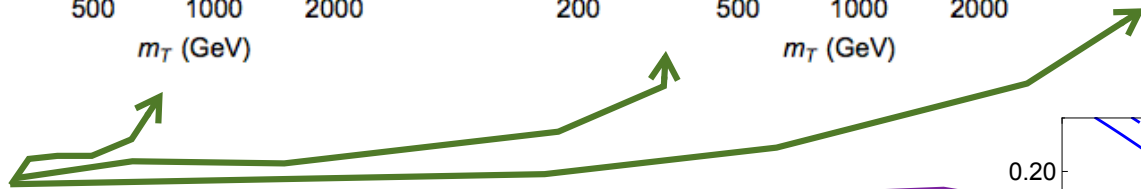
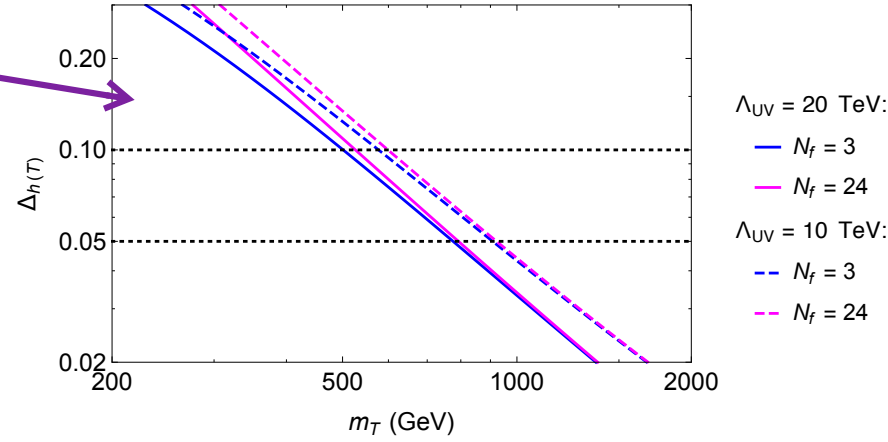
using results from I 506.0546 Fedderke, Lin, Wang

- $\Delta T = 0.076$  (current)
- $\Delta T = 0.024$  (ILC)
- $\Delta T = 0.019$  (FCC-ee-Z)
- $\Delta T = 0.0092$  (FCC-ee-t)
- $\delta\sigma_{Zh} = 5.2\%$  (ILC250)
- $\delta\sigma_{Zh} = 2.4\%$  (ILC250 LumiUp)
- $\delta\sigma_{Zh} = 0.8\%$  (FCC-ee)
- $\delta\lambda_3 = 20\%$  (100 TeV,  $3ab^{-1}$ )
- $\delta\lambda_3 = 10\%$  (100 TeV,  $30ab^{-1}$ )
- $\delta\lambda_3 = 5\%$
- $\delta\lambda_3 = 2\%$

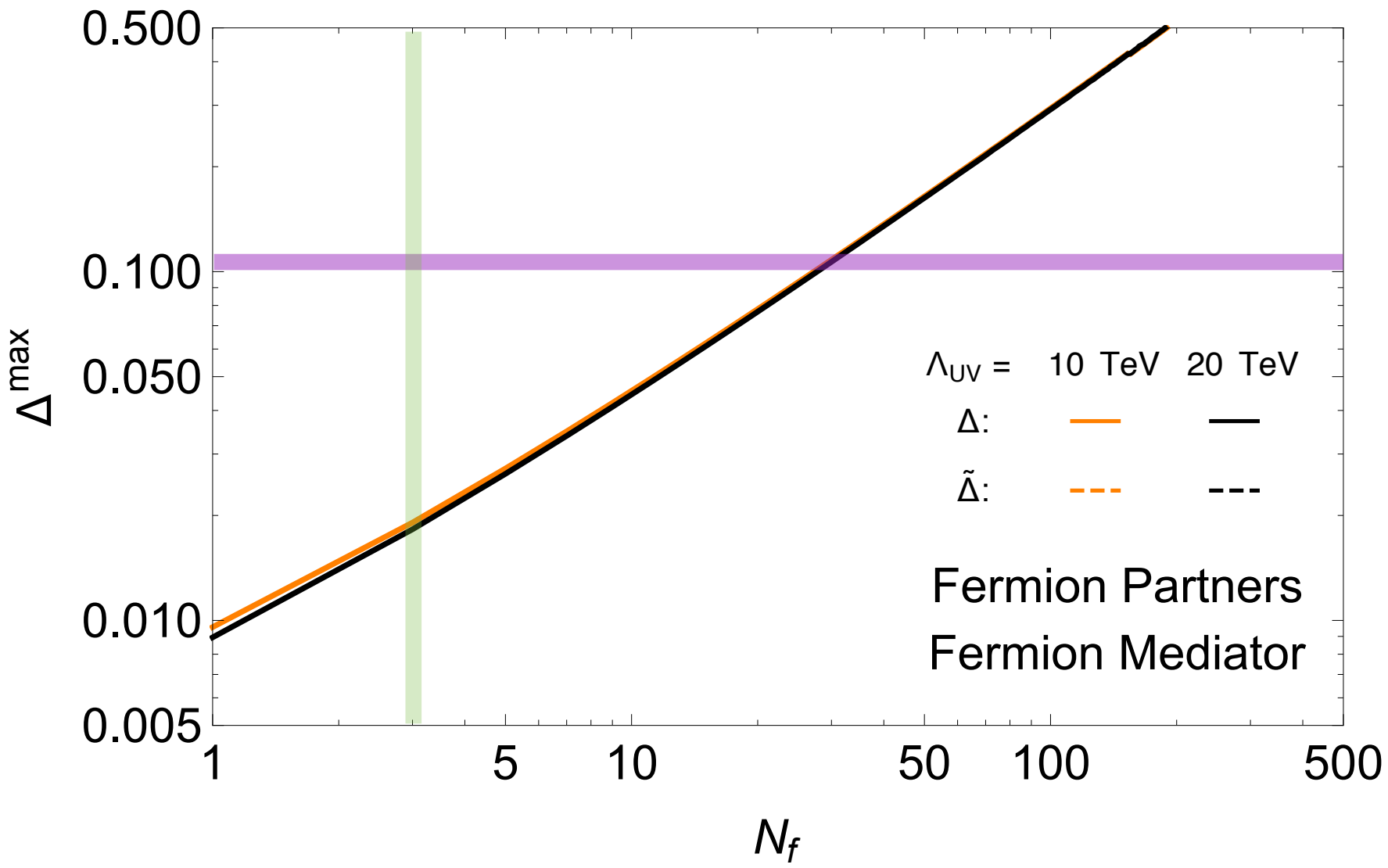
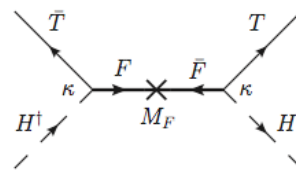


Violation of custodial symmetry  $\rightarrow$  large T parameter deviations!

Again, Higgs log tuning prefers top partners  $< 500$  GeV



# Fermion Partner - Fermion Mediator



**A natural theory needs to have VERY MANY fermion partners to possibly escape detection.**