MEASUREMENTS OF Ω AND Λ FROM 42 HIGH-REDSHIFT SUPERNOVAE

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ABSTRACT

We report measurements of the mass density, Ω_M , and cosmological-constant energy density, Ω_{Λ} , of the universe based on the analysis of 42 type Ia supernovae discovered by the Supernova Cosmology Project. The magnitude-redshift data for these supernovae, at redshifts between 0.18 and 0.83, are fitted jointly with a set of supernovae from the Calán/Tololo Supernova Survey, at redshifts below 0.1, to yield values for the cosmological parameters. All supernova peak magnitudes are standardized using a SN Ia light-curve width-luminosity relation. The measurement yields a joint probability distribution of the cosmological parameters that is approximated by the relation $0.8\Omega_M - 0.6\Omega_\Lambda \approx -0.2 \pm 0.1$ in the region of interest ($\Omega_M \lesssim 1.5$). For a flat ($\Omega_M + \Omega_\Lambda = 1$) cosmology we find $\Omega_M^{\rm flat} = 0.28^{+0.09}_{-0.08}$ (1 σ statistical) $^{+0.05}_{-0.04}$ (identified systematics). The data are strongly inconsistent with a $\Lambda = 0$ flat cosmology, the simplest inflationary universe model. An open, $\Lambda = 0$ cosmology also does not fit the data well: the data indicate that the cosmological constant is nonzero and positive, with a confidence of $P(\Lambda > 0) = 99\%$, including the identified systematic uncertainties. The best-fit age of the universe relative to the Hubble time is $t_0^{\text{flat}} = 14.9^{+1.4}_{-1.1}(0.63/h)$ Gyr for a flat cosmology. The size of our sample allows us to perform a variety of statistical tests to check for possible systematic errors and biases. We find no significant differences in either the host reddening distribution or Malmquist bias between the low-redshift Calán/Tololo sample and our high-redshift sample. Excluding those few supernovae that are outliers in color excess or fit residual does not significantly change the results. The conclusions are also robust whether or not a width-luminosity relation is used to standardize the supernova peak magnitudes. We discuss and constrain, where possible, hypothetical alternatives to a cosmological constant.

Subject headings: cosmology: observations — distance scale — supernovae: general

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1. INTRODUCTION

Since the earliest studies of supernovae, it has been suggested that these luminous events might be used as standard candles for cosmological measurements (Baade 1938). At closer distances they could be used to measure the Hubble constant if an absolute distance scale or magnitude scale could be established, while at higher redshifts they could determine the deceleration parameter (Tammann 1979; Colgate 1979). The Hubble constant measurement became a realistic possibility in the 1980s, when the more homogeneous subclass of type Ia supernovae (SNe Ia) was identified (see Branch 1998). Attempts to measure the deceleration parameter, however, were stymied for lack of high-redshift supernovae. Even after an impressive multivear effort by Nørgaard-Nielsen et al. (1989), it was only possible to follow one SN Ia, at z = 0.31, discovered 18 days past its peak brightness.

The Supernova Cosmology Project was started in 1988 to address this problem. The primary goal of the project is the determination of the cosmological parameters of the universe using the magnitude-redshift relation of type Ia supernovae. In particular, Goobar & Perlmutter (1995) showed the possibility of separating the relative contributions of the mass density, Ω_M , and the cosmological constant, Λ , to changes in the expansion rate by studying supernovae at a range of redshifts. The Project developed techniques, including instrumentation, analysis, and observing strategies, that make it possible to systematically study highredshift supernovae (Perlmutter et al. 1995a). As of 1998 March, more than 75 type Ia supernovae at redshifts z = 0.18-0.86 have been discovered and studied by the Supernova Cosmology Project (Perlmutter et al. 1995b, 1996, 1997a, 1997b, 1997c, 1997d, 1998a).

A first presentation of analysis techniques, identification of possible sources of statistical and systematic errors, and first results based on seven of these supernovae at redshifts $z \sim 0.4$ were given in Perlmutter et al. (1997e; hereafter referred to as P97). These first results yielded a confidence region that was suggestive of a flat, $\Lambda = 0$ universe but with a large range of uncertainty. Perlmutter et al. (1998b) added a z = 0.83 SN Ia to this sample, with observations from the Hubble Space Telescope (HST) and Keck 10 m telescope, providing the first demonstration of the method of separating Ω_M and Λ contributions. This analysis offered preliminary evidence for a low-mass-density universe with a best-fit value of $\Omega_M = 0.2 \pm 0.4$, assuming $\Lambda = 0$. Independent work by Garnavich et al. (1998a), based on three supernovae at $z \sim 0.5$ and one at z = 0.97, also suggested a low mass density, with best-fit $\Omega_M = -0.1 \pm 0.5$ for $\Lambda = 0$.

Perlmutter et al. 1997f presented a preliminary analysis of 33 additional high-redshift supernovae, which gave a confidence region indicating an accelerating universe and barely including a low-mass $\Lambda=0$ cosmology. Recent independent work of Riess et al. (1998), based on 10 high-redshift supernovae added to the Garnavich et al. (1998a) set, reached the same conclusion. Here we report on the complete analysis of 42 supernovae from the Supernova Cosmology Project, including the reanalysis of our previously reported supernovae with improved calibration data and improved photometric and spectroscopic SN Ia templates.

2. BASIC DATA AND PROCEDURES

The new supernovae in this sample of 42 were all dis-

covered while still brightening, using the Cerro Tololo Inter-American Observatory (CTIO) 4 m telescope with the 2048^2 pixel prime-focus CCD camera or the 4×2048^2 pixel Big Throughput Camera.¹⁰ The supernovae were followed with photometry over the peak of their light curves and approximately 2-3 months further ($\sim 40-60$ days rest frame) using the CTIO 4 m, Wisconsin-Indiana-Yale-NOAO (WIYN) 3.6 m, ESO 3.6 m, Isaac Newton Telescope (INT) 2.5 m, and the William Herschel Telescope (WHT) 4.2 m telescopes. (SN 1997ap and other 1998 supernovae have also been followed with HST photometry.) The supernova redshifts and spectral identifications were obtained using the Keck I and II 10 m telescopes with the Low-Resolution Imaging Spectrograph (Oke et al. 1995) and the ESO 3.6 m telescope. The photometry coverage was most complete in Kron-Cousins R-band, with Kron-Cousins I-band photometry coverage ranging from two or three points near peak to relatively complete coverage paralleling the R-band observations.

Almost all of the new supernovae were observed spectroscopically. The confidence of the type Ia classifications based on these spectra taken together with the observed light curves, ranged from "definite" (when Si II features were visible) to "likely" (when the features were consistent with type Ia and inconsistent with most other types). The lower confidence identifications were primarily due to hostgalaxy contamination of the spectra. Fewer than 10% of the original sample of supernova candidates from which these SNe Ia were selected were confirmed to be non-type Ia, i.e., being active galactic nuclei or belonging to another SN subclass; almost all of these non-SNe Ia could also have been identified by their light curves and/or position far from the SN Ia Hubble line. Whenever possible, the redshifts were measured from the narrow host-galaxy lines rather than the broader supernova lines. The light curves and several spectra are shown in Perlmutter et al. (1997e, 1997f, 1998b); complete catalogs and detailed discussions of the photometry and spectroscopy for these supernovae will be presented in forthcoming papers.

The photometric reduction and the analyses of the light curves followed the procedures described in P97. The supernovae were observed with the Kron-Cousins filter that best matched the rest-frame B and V filters at the supernova's redshift, and any remaining mismatch of wavelength coverage was corrected by calculating the expected photometric difference—the "cross-filter K-correction"—using template SN Ia spectra as in Kim, Goobar, & Perlmutter (1996). We have now recalculated these K-corrections (see Nugent et al. 1998) using improved template spectra, based on an extensive database of low-redshift SN Ia spectra recently made available from the Calán/Tololo survey (Phillips et al. 1999). Where available, IUE and HST spectra (Cappellaro, Turatto, & Fernley 1995; Kirshner et al. 1993) were also added to the SN Ia spectra, including those published previously (1972E, 1981B, 1986G, 1990N, 1991T, 1992A, and 1994D: in Kirshner & Oke 1975; Branch et al. 1993; Phillips et al. 1987; Jeffery et al. 1992; Meikle et al. 1996; Patat et al. 1996). In Nugent et al. (1998) we show that the Kcorrections can be calculated accurately for a given day on the supernova light curve and for a given supernova light-

¹⁰ Big Throughput Camera information is provided by G. Bernstein & J. A. Tyson, 1998, at http://www.astro.lsa.umich.edu/btc/user.html.

curve width from the color of the supernova on that day. (Such a calculation of K-correction based on supernova color will also automatically account for any modification of the K-correction due to reddening of the supernova; see Nugent et al. 1998. In the case of insignificant reddening the SN Ia template color curves can be used.) We find that these calculations are robust to mis-estimations of the light-curve width or day on the light curve, giving results correct to within 0.01 mag for light-curve—width errors of $\pm 25\%$ or light-curve phase errors of ± 5 days even at redshifts where filter matching is the worst. Given small additional uncertainties in the colors of supernovae, we take an overall systematic uncertainty of 0.02 mag for the K-correction.

The improved K-corrections have been recalculated for all the supernovae used in this paper, including those previously analyzed and published. Several of the low-redshift supernovae from the Calán/Tololo survey have relatively large changes (as much as 0.1 mag) at times in their Kcorrected light curves. (These and other low-redshift supernovae with new K-corrections are used by several independent groups in constructing SN Ia light-curve templates, so the templates must be updated accordingly.) The K-corrections for several of the high-redshift supernovae analyzed in P97 have also changed by small amounts at the light-curve peak $[\Delta K(t=0) \lesssim 0.02 \text{ mag}]$ and somewhat larger amounts by 20 days past peak $[\Delta K(t = 20) \lesssim 0.1]$ mag]; this primarily affects the measurement of the restframe light-curve width. These K-correction changes balance out among the P97 supernovae, so the final results for these supernovae do not change significantly. (As we discuss below, however, the much larger current data set does affect the interpretation of these results.)

As in P97, the peak magnitudes have been corrected for the light-curve width-luminosity relation of SNe Ia:

$$m_B^{\rm corr} = m_B + \Delta_{\rm corr}(s)$$
, (1)

where the correction term Δ_{corr} is a simple monotonic function of the "stretch factor," s, that stretches or contracts the time axis of a template SN Ia light curve to best fit the observed light curve for each supernova (see P97; Perlmutter et al. 1995a; Kim et al. 1999; Goldhaber et al. 1999; and see Phillips 1993; Riess, Press, & Kirshner 1995, 1996 [hereafter RPK96]). A similar relation corrects the V-band light curve, with the same stretch factor in both bands. For the supernovae discussed in this paper, the template must be time-dilated by a factor 1 + z before fitting to the observed light curves to account for the cosmological lengthening of the supernova timescale (Goldhaber et al. 1995; Leibundgut et al. 1996a; Riess et al. 1997a). P97 calculated $\Delta_{corr}(s)$ by translating from s to Δm_{15} (both describing the timescale of the supernova event) and then using the relation between Δm_{15} and luminosity as determined by Hamuy et al. (1995). The light curves of the Calán/Tololo supernovae have since been published, and we have directly fitted each light curve with the stretched template method to determine its stretch factor s. In this paper, for the lightcurve width-luminosity relation, we therefore directly use the functional form

$$\Delta_{\rm corr}(s) = \alpha(s-1) \tag{2}$$

and determine α simultaneously with our determination of the cosmological parameters. With this functional form, the supernova peak apparent magnitudes are thus all

"corrected" as they would appear if the supernovae had the light-curve width of the template, s = 1.

We use analysis procedures that are designed to be as similar as possible for the low- and high-redshift data sets. Occasionally, this requires not using all of the data available at low redshift, when the corresponding data are not accessible at high redshift. For example, the low-redshift supernova light curves can often be followed with photometry for many months with high signal-to-noise ratios, whereas the high-redshift supernova observations are generally only practical for approximately 60 rest-frame days past maximum light. This period is also the phase of the low-redshift SN Ia light curves that is fitted best by the stretched-template method and that best predicts the luminosity of the supernova at maximum. We therefore fitted only this period for the light curves of the low-redshift supernovae. Similarly, at high redshift the rest-frame B-band photometry is usually much more densely sampled in time than the rest-frame V-band data, so we use the stretch factor that best fits the rest-frame B-band data for both low- and high-redshift supernovae, even though at low-redshift the V-band photometry is equally well sampled.

Each supernova peak magnitude was also corrected for Galactic extinction, A_R , using the extinction law of Cardelli, Clayton, & Mathis (1989), first using the color excess, $E(B-V)_{SF\&D}$, at the supernova's Galactic coordinates provided by Schlegel, Finkbeiner, & Davis (1998) and then for comparison—using the $E(B-V)_{\rm B\&H}$ value provided by D. Burstein & C. Heiles (1998, private communication; see also Burstein & Heiles 1982). Galactic extinction, A_R , was calculated from E(B-V) using a value of the total-to-selective extinction ratio, $\mathcal{R}_R \equiv A_R/E(B-V)$, specific to each supernova. These were calculated using the appropriate redshifted supernova spectrum as it would appear through an R-band filter. These values of \mathcal{R}_R range from 2.56 at z = 0 to 4.88 at z = 0.83. The observed supernova colors were similarly corrected for Galactic extinction. Any extinction in the supernova's host galaxy or between galaxies was not corrected for at this stage but will be analyzed separately in § 4.

All the same corrections for width-luminosity relation, K-corrections, and extinction (but using $\mathcal{R}_B = 4.14$) were applied to the photometry of 18 low-redshift SNe Ia ($z \le 0.1$) from the Calán/Tololo supernova survey (Hamuy et al. 1996) that were discovered earlier than 5 days after peak. The light curves of these 18 supernovae have all been refitted since P97, using the more recently available photometry (Hamuy et al. 1996) and our K-corrections.

Figures 1 and 2a show the Hubble diagram of effective rest-frame B magnitude corrected for the width-luminosity relation,

$$m_R^{\rm eff} = m_R + \Delta_{\rm corr} - K_{BR} - A_R , \qquad (3)$$

as a function of redshift for the 42 Supernova Cosmology Project high-redshift supernovae, along with the 18 Calán/Tololo low-redshift supernovae. (Here K_{BR} is the cross-filter K-correction from observed R band to restframe B band.) Tables 1 and 2 give the corresponding IAU names, redshifts, magnitudes, corrected magnitudes, and their respective uncertainties. As in P97, the inner error bars in Figures 1 and 2 represent the photometric uncertainty, while the outer error bars add in quadrature 0.17 mag of intrinsic dispersion of SN Ia magnitudes that remain after

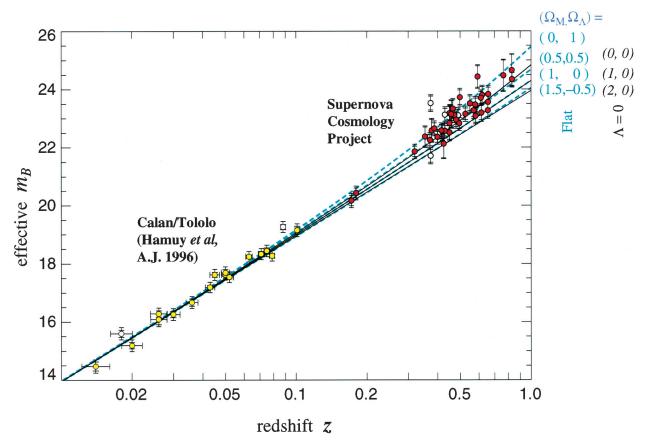


Fig. 1.—Hubble diagram for 42 high-redshift type Ia supernovae from the Supernova Cosmology Project and 18 low-redshift type Ia supernovae from the Calán/Tololo Supernova Survey after correcting both sets for the SN Ia light-curve width-luminosity relation. The inner error bars show the uncertainty due to measurement errors, while the outer error bars show the total uncertainty when the intrinsic luminosity dispersion, 0.17 mag, of light-curve-width-corrected type Ia supernovae is added in quadrature. The unfilled circles indicate supernovae not included in fit C. The horizontal error bars represent the assigned peculiar velocity uncertainty of 300 km s⁻¹. The solid curves are the theoretical $m_B^{\rm eff}(z)$ for a range of cosmological models with zero cosmological constant: $(\Omega_M, \Omega_\Lambda) = (0, 0)$ on top, (1, 0) in middle, and (2, 0) on bottom. The dashed curves are for a range of flat cosmological models: $(\Omega_M, \Omega_\Lambda) = (0, 1)$ on top, (0.5, 0.5) second from top, (1, 0) third from top, and (1.5, -0.5) on bottom.

applying the width-luminosity correction. For these plots, the slope of the width-brightness relation was taken to be $\alpha=0.6$, the best-fit value of fit C discussed below. (Since both the low- and high-redshift supernova light-curve widths are clustered rather closely around s=1, as shown in Fig. 4, the exact choice of α does not change the Hubble diagram significantly.) The theoretical curves for a universe with no cosmological constant are shown as solid lines for a range of mass density, $\Omega_M=0$, 1, 2. The dashed lines represent alternative flat cosmologies, for which the total mass energy density $\Omega_M+\Omega_\Lambda=1$ (where $\Omega_\Lambda\equiv\Lambda/3H_0^2$). The range of models shown are for $(\Omega_M,\Omega_\Lambda)=(0,1)$, (0.5,0.5), (1,0), which is covered by the matching solid line, and (1.5,-0.5).

3. FITS TO $\Omega_{\rm m}$ AND Ω_{Λ}

The combined low- and high-redshift supernova data sets of Figure 1 are fitted to the Friedman-Robertson-Walker (FRW) magnitude-redshift relation, expressed as in P97:

$$\begin{split} m_B^{\text{eff}} &\equiv m_R + \alpha(s-1) - K_{BR} - A_R \\ &= \mathcal{M}_B + 5\log \mathcal{D}_L(z; \, \Omega_M, \, \Omega_\Lambda) \;, \end{split} \tag{4}$$

where $\mathcal{D}_L \equiv H_0 d_L$ is the "Hubble-constant-free" luminosity distance and $\mathcal{M}_B \equiv M_B - 5 \log H_0 + 25$ is the "Hubble-constant-free" *B*-band absolute magnitude at maximum of a SN Ia with width s = 1. (These quantities

are, respectively, calculated from theory or fitted from apparent magnitudes and redshifts, both without any need for H_0 . The cosmological-parameter results are thus also completely independent of H_0 .) The details of the fitting procedure as presented in P97 were followed, except that both the low- and high-redshift supernovae were fitted simultaneously, so that \mathcal{M}_B and α , the slope of the width-luminosity relation, could also be fitted in addition to the cosmological parameters Ω_M and Ω_Λ . For most of the analyses in this paper, \mathcal{M}_B and α are statistical "nuisance" parameters; we calculate two-dimensional confidence regions and single-parameter uncertainties for the cosmological parameters by integrating over these parameters, i.e., $\mathcal{P}(\Omega_M, \Omega_\Lambda) = \iint \mathcal{P}(\Omega_M, \Omega_\Lambda, \mathcal{M}_B, \alpha) d\mathcal{M}_B d\alpha$.

As in P97, the small correlations between the photometric uncertainties of the high-redshift supernovae, due to shared calibration data, have been accounted for by fitting with a correlation matrix of uncertainties. 11 The low-redshift supernova photometry is more likely to be uncorrelated in its calibration, since these supernovae were not discovered in batches. However, we take a 0.01 mag systematic uncertainty in the comparison of the low-redshift B-band photometry and the high-redshift R-band photometry. The stretch-factor uncertainty is propagated with a fixed width-luminosity slope (taken from the low-redshift

¹¹ The data are available at http://www-supernova.lbl.gov.

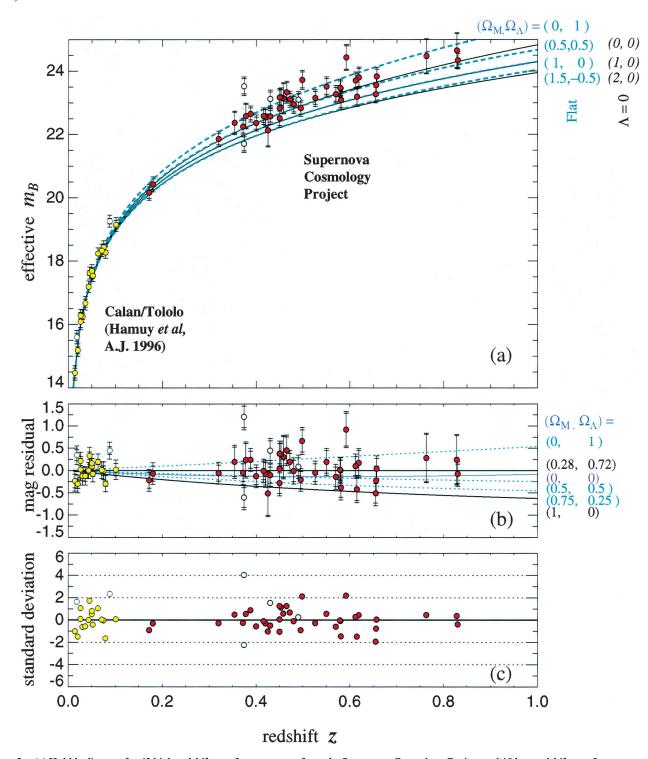


Fig. 2.—(a) Hubble diagram for 42 high-redshift type Ia supernovae from the Supernova Cosmology Project and 18 low-redshift type Ia supernovae from the Calán/Tololo Supernova Survey, plotted on a linear redshift scale to display details at high redshift. The symbols and curves are as in Fig. 1. (b) Magnitude residuals from the best-fit flat cosmology for the fit C supernova subset, $(\Omega_M, \Omega_\Lambda) = (0.28, 0.72)$. The dashed curves are for a range of flat cosmological models: $(\Omega_M, \Omega_\Lambda) = (0, 1)$ on top, (0.5, 0.5) third from bottom, (0.75, 0.25) second from bottom, and (1, 0) is the solid curve on bottom. The middle solid curve is for $(\Omega_M, \Omega_\Lambda) = (0, 0)$. Note that this plot is practically identical to the magnitude residual plot for the best-fit unconstrained cosmology of fit C, with $(\Omega_M, \Omega_\Lambda) = (0.73, 1.32)$. (c) Uncertainty-normalized residuals from the best-fit flat cosmology for the fit C supernova subset, $(\Omega_M, \Omega_\Lambda) = (0.28, 0.72)$.

supernovae; cf. P97) and checked for consistency after the fit.

We have compared the results of Bayesian and classical, "frequentist," fitting procedures. For the Bayesian fits, we have assumed a "prior" probability distribution that has zero probability for $\Omega_{\rm M} < 0$ but otherwise has uniform

probability in the four parameters Ω_M , Ω_Λ , α , and M_B . For the frequentist fits, we have followed the classical statistical procedures described by Feldman & Cousins (1998) to guarantee frequentist coverage of our confidence regions in the physically allowed part of parameter space. Note that throughout the previous cosmology literature, completely

TABLE 1 SCP SNE IA DATA

| SN | z | σ_z | $m_X^{ m peak}$ | $\sigma_X^{ m peak}$ | A_X | K_{BX} | $m_B^{ m peak}$ | $m_B^{ m eff}$ | $\sigma_{m_R^{ m eff}}$ | Notes |
|--------|-------|------------|-----------------|----------------------|-------|----------|-----------------|----------------|-------------------------|-----------|
| (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) |
| 1992bi | 0.458 | 0.001 | 22.12 | 0.10 | 0.03 | -0.72 | 22.81 | 23.11 | 0.46 | Е-Н |
| 1994F | 0.354 | 0.001 | 22.08 | 0.10 | 0.11 | -0.58 | 22.55 | 22.38 | 0.33 | E-H |
| 1994G | 0.425 | 0.001 | 21.52 | 0.21 | 0.03 | -0.68 | 22.17 | 22.13 | 0.49 | |
| 1994H | 0.374 | 0.001 | 21.28 | 0.06 | 0.10 | -0.61 | 21.79 | 21.72 | 0.22 | B–L |
| 1994al | 0.420 | 0.001 | 22.37 | 0.06 | 0.42 | -0.68 | 22.63 | 22.55 | 0.25 | E–H |
| 1994am | 0.372 | 0.001 | 21.82 | 0.07 | 0.10 | -0.61 | 22.32 | 22.26 | 0.20 | E-H |
| 1994an | 0.378 | 0.001 | 22.14 | 0.08 | 0.21 | -0.62 | 22.55 | 22.58 | 0.37 | E–H |
| 1995aq | 0.453 | 0.001 | 22.60 | 0.07 | 0.07 | -0.71 | 23.24 | 23.17 | 0.25 | |
| 1995ar | 0.465 | 0.005 | 22.71 | 0.04 | 0.07 | -0.71 | 23.35 | 23.33 | 0.30 | Н |
| 1995as | 0.498 | 0.001 | 23.02 | 0.07 | 0.07 | -0.71 | 23.66 | 23.71 | 0.25 | Н |
| 1995at | 0.655 | 0.001 | 22.62 | 0.03 | 0.07 | -0.66 | 23.21 | 23.27 | 0.21 | Н |
| 1995aw | 0.400 | 0.030 | 21.75 | 0.03 | 0.12 | -0.65 | 22.27 | 22.36 | 0.19 | |
| 1995ax | 0.615 | 0.001 | 22.53 | 0.07 | 0.11 | -0.67 | 23.10 | 23.19 | 0.25 | |
| 1995ay | 0.480 | 0.001 | 22.64 | 0.04 | 0.35 | -0.72 | 23.00 | 22.96 | 0.24 | |
| 1995az | 0.450 | 0.001 | 22.44 | 0.07 | 0.61 | -0.71 | 22.53 | 22.51 | 0.23 | |
| 1995ba | 0.388 | 0.001 | 22.08 | 0.04 | 0.06 | -0.63 | 22.66 | 22.65 | 0.20 | |
| 1996cf | 0.570 | 0.010 | 22.70 | 0.03 | 0.13 | -0.68 | 23.25 | 23.27 | 0.22 | |
| 1996cg | 0.490 | 0.010 | 22.46 | 0.03 | 0.11 | -0.72 | 23.06 | 23.10 | 0.20 | C, D, G-L |
| 1996ci | 0.495 | 0.001 | 22.19 | 0.03 | 0.09 | -0.71 | 22.82 | 22.83 | 0.19 | |
| 1996ck | 0.656 | 0.001 | 23.08 | 0.07 | 0.13 | -0.66 | 23.62 | 23.57 | 0.28 | |
| 1996cl | 0.828 | 0.001 | 23.53 | 0.10 | 0.18 | -1.22 | 24.58 | 24.65 | 0.54 | |
| 1996cm | 0.450 | 0.010 | 22.66 | 0.07 | 0.15 | -0.71 | 23.22 | 23.17 | 0.23 | |
| 1996cn | 0.430 | 0.010 | 22.58 | 0.03 | 0.08 | -0.69 | 23.19 | 23.13 | 0.22 | C, D, G-L |
| 1997F | 0.580 | 0.001 | 22.90 | 0.06 | 0.13 | -0.68 | 23.45 | 23.46 | 0.23 | H |
| 1997G | 0.763 | 0.001 | 23.56 | 0.41 | 0.20 | -1.13 | 24.49 | 24.47 | 0.53 | |
| 1997H | 0.526 | 0.001 | 22.68 | 0.05 | 0.16 | -0.70 | 23.21 | 23.15 | 0.20 | H |
| 1997I | 0.172 | 0.001 | 20.04 | 0.02 | 0.16 | -0.33 | 20.20 | 20.17 | 0.18 | |
| 1997J | 0.619 | 0.001 | 23.25 | 0.08 | 0.13 | -0.67 | 23.80 | 23.80 | 0.28 | |
| 1997K | 0.592 | 0.001 | 23.73 | 0.10 | 0.07 | -0.67 | 24.33 | 24.42 | 0.37 | H |
| 1997L | 0.550 | 0.010 | 22.93 | 0.05 | 0.08 | -0.69 | 23.53 | 23.51 | 0.25 | |
| 1997N | 0.180 | 0.001 | 20.19 | 0.01 | 0.10 | -0.34 | 20.42 | 20.43 | 0.17 | H |
| 1997O | 0.374 | 0.001 | 22.97 | 0.07 | 0.09 | -0.61 | 23.50 | 23.52 | 0.24 | B–L |
| 1997P | 0.472 | 0.001 | 22.52 | 0.04 | 0.10 | -0.72 | 23.14 | 23.11 | 0.19 | |
| 1997Q | 0.430 | 0.010 | 22.01 | 0.03 | 0.09 | -0.69 | 22.60 | 22.57 | 0.18 | |
| 1997R | 0.657 | 0.001 | 23.28 | 0.05 | 0.11 | -0.66 | 23.83 | 23.83 | 0.23 | |
| 1997S | 0.612 | 0.001 | 23.03 | 0.05 | 0.11 | -0.67 | 23.59 | 23.69 | 0.21 | |
| 1997ac | 0.320 | 0.010 | 21.38 | 0.03 | 0.09 | -0.55 | 21.83 | 21.86 | 0.18 | |
| 1997af | 0.579 | 0.001 | 22.96 | 0.07 | 0.09 | -0.68 | 23.54 | 23.48 | 0.22 | |
| 1997ai | 0.450 | 0.010 | 22.25 | 0.05 | 0.14 | -0.71 | 22.81 | 22.83 | 0.30 | Н |
| 1997aj | 0.581 | 0.001 | 22.55 | 0.06 | 0.11 | -0.68 | 23.12 | 23.09 | 0.22 | |
| 1997am | 0.416 | 0.001 | 21.97 | 0.03 | 0.11 | -0.67 | 22.52 | 22.57 | 0.20 | |
| 1997ap | 0.830 | 0.010 | 23.20 | 0.07 | 0.13 | -1.23 | 24.30 | 24.32 | 0.22 | H |

Note.—Col. (1): IAU Name assigned to SCP supernova.

Col. (2): Geocentric redshift of supernova or host galaxy.

Col. (3): Redshift uncertainty.

Col. (4): Peak magnitude from light-curve fit in observed band corresponding to rest-frame B-band (i.e., $m_X^{\text{peak}} \equiv m_R^{\text{peak}}$ or m_Y^{peak}).

Col. (5): Uncertainty in fit peak magnitude.

Col. (6): Galactic extinction in observed band corresponding to rest-frame B-band (i.e., $A_X \equiv A_R$ or A_I); an uncertainty of 10% is assumed.

Col. (7): Representative K-correction (at peak) from observed band to B-band (i.e., $K_{BX} \equiv K_{BR}$ or K_{BI}); an uncertainty of 2% is assumed.

Col. (8): B-band peak magnitude.

Col. (9): Stretch luminosity—corrected effective *B*-band peak magnitude: $m_B^{\text{eff}} \equiv m_X^{\text{peak}} + \alpha(s-1) - K_{BX} - A_X$. Col. (10): Total uncertainty in corrected *B*-band peak magnitude. This includes uncertainties due to the intrinsic

luminosity dispersion of SNe Ia of 0.17 mag, 10% of the Galactic extinction correction, 0.01 mag for K-corrections, 300 km s⁻¹ to account for peculiar velocities, in addition to propagated uncertainties from the light-curve fits.

Col. (11): Fits from which given supernova was excluded.

unconstrained fits have generally been used that can (and do) lead to confidence regions that include the part of parameter space with negative values for Ω_M . The differences between the confidence regions that result from Bayesian and classical analyses are small. We present the Bayesian confidence regions in the figures, since they are

somewhat more conservative; i.e., they have larger confidence regions in the vicinity of particular interest near $\Lambda=0$.

The residual dispersion in SN Ia peak magnitude after correcting for the width-luminosity relation is small, about 0.17 mag, before applying any color-correction. This was

TABLE 2
CALÁN/TOLOLO SNE IA DATA

| SN (1) | z (2) | σ_z (3) | m _{obs} (4) | $\sigma_{\mathrm{obs}}^{\mathrm{peak}}$ (5) | A _B (6) | К _{вв} (7) | m _B ^{peak} (8) | m _B ^{corr} (9) | $\sigma_{m_B^{\rm corr}}$ (10) | Notes (11) |
|--------|----------|----------------|----------------------|---|--------------------|---------------------|------------------------------------|------------------------------------|--------------------------------|---------------|
| 1990O | 0.030 | 0.002 | 16.62 | 0.03 | 0.39 | -0.00 | 16.23 | 16.26 | 0.20 | |
| 1990af | 0.050 | 0.002 | 17.92 | 0.01 | 0.16 | +0.01 | 17.75 | 17.63 | 0.18 | |
| 1992P | 0.026 | 0.002 | 16.13 | 0.03 | 0.12 | -0.01 | 16.02 | 16.08 | 0.24 | |
| 1992ae | 0.075 | 0.002 | 18.61 | 0.12 | 0.15 | +0.03 | 18.43 | 18.43 | 0.20 | |
| 1992ag | 0.026 | 0.002 | 16.59 | 0.04 | 0.38 | -0.01 | 16.22 | 16.28 | 0.20 | |
| 1992al | 0.014 | 0.002 | 14.60 | 0.01 | 0.13 | -0.01 | 14.48 | 14.47 | 0.23 | |
| 1992aq | 0.101 | 0.002 | 19.29 | 0.12 | 0.05 | +0.05 | 19.19 | 19.16 | 0.23 | |
| 1992bc | 0.020 | 0.002 | 15.20 | 0.01 | 0.07 | -0.01 | 15.13 | 15.18 | 0.20 | |
| 1992bg | 0.036 | 0.002 | 17.41 | 0.07 | 0.77 | +0.00 | 16.63 | 16.66 | 0.21 | |
| 1992bh | 0.045 | 0.002 | 17.67 | 0.04 | 0.10 | +0.01 | 17.56 | 17.61 | 0.19 | |
| 1992Ы | 0.043 | 0.002 | 17.31 | 0.07 | 0.04 | +0.01 | 17.26 | 17.19 | 0.18 | |
| 1992bo | 0.018 | 0.002 | 15.85 | 0.02 | 0.11 | -0.01 | 15.75 | 15.61 | 0.21 | B-L |
| 1992bp | 0.079 | 0.002 | 18.55 | 0.02 | 0.21 | +0.04 | 18.30 | 18.27 | 0.18 | |
| 1992br | 0.088 | 0.002 | 19.71 | 0.07 | 0.12 | +0.04 | 19.54 | 19.28 | 0.18 | B-L |
| 1992bs | 0.063 | 0.002 | 18.36 | 0.05 | 0.09 | +0.03 | 18.24 | 18.24 | 0.18 | |
| 1993B | 0.071 | 0.002 | 18.68 | 0.08 | 0.31 | +0.03 | 18.34 | 18.33 | 0.20 | |
| 1993O | 0.052 | 0.002 | 17.83 | 0.01 | 0.25 | +0.01 | 17.58 | 17.54 | 0.18 | |
| 1993ag | 0.050 | 0.002 | 18.29 | 0.02 | 0.56 | +0.01 | 17.71 | 17.69 | 0.20 | |

Note.—Col. (1): IAU name assigned to Calán/Tololo supernova.

Col. (2): Redshift of supernova or host galaxy in Local Group rest-frame.

Col. (3): Redshift uncertainty.

Col. (4): Peak magnitude from light-curve fit in observed B-band. Note that the template light curve used in the fit is not identical to the template light curve used by Hamuy et al. (1995), so the best-fit peak magnitude may differ slightly.

Col. (5): Uncertainty in fit peak magnitude.

Col. (6): Galactic extinction in observed B-band; an uncertainty of 10% is assumed.

Col. (7): Representative K-correction from observed B-band to rest-frame B-band; an uncertainty of 2% is assumed.

Col. (8): B-band peak magnitude.

Col. (9): Stretch-luminosity corrected B-band peak magnitude.

Col. (10): Total uncertainty in corrected B-band peak magnitude. This includes uncertainties due to the intrinsic luminosity dispersion of SNe Ia of 0.17 mag, 10% of the Galactic extinction correction, 0.01 mag for K-corrections, 300 km s⁻¹ to account for peculiar velocities, in addition to propagated uncertainties from the light-curve fits.

Col. (11): Fits from which given supernova was excluded.

reported in Hamuy et al. (1996) for the low-redshift Calán/ Tololo supernovae, and it is striking that the same residual is most consistent with the current 42 high-redshift supernovae (see § 5). It is not clear from the current data sets, however, whether this dispersion is best modeled as a normal distribution (a Gaussian in flux space) or a lognormal distribution (a Gaussian in magnitude space). We have therefore performed the fits in two ways: minimizing χ^2 measured using either magnitude residuals or flux residuals. The results are generally in excellent agreement, but since the magnitude fits yield slightly larger confidence regions, we have again chosen this more conservative alternative to report in this paper.

We have analyzed the total set of 60 low- plus high-redshift supernovae in several ways, with the results of each fit presented as a row of Table 3. The most inclusive analyses are presented in the first two rows: Fit A is a fit to the entire data set, while fit B excludes two supernovae that are the most significant outliers from the average light-curve width, s=1, and two of the remaining supernovae that are the largest residuals from fit A. Figure 4 shows that the remaining low- and high-redshift supernovae are well matched in their light-curve width (the error-weighted means are $\langle s \rangle_{\text{Hamuy}} = 0.99 \pm 0.01$ and $\langle s \rangle_{\text{SCP}} = 1.00 \pm 0.01$) making the results robust with respect to the width-luminosity-relation correction (see § 4.5). Our primary analysis, fit C, further excludes two supernovae

that are likely to be reddened, and is discussed in the following section.

Fits A and B give very similar results. Removing the two large-residual supernovae from fit A yields indistinguishable results, while Figure 5a shows that the 68% and 90% joint confidence regions for Ω_M and Ω_Λ still change very little after also removing the two supernovae with outlier light-curve widths. The best-fit mass-density in a flat universe for fit A is, within a fraction of the uncertainty, the same value as for fit B, $\Omega_M^{\rm flat} = 0.26^{+0.09}_{-0.08}$ (see Table 3). The main difference between the fits is the goodness-of-fit: the larger χ^2 per degree of freedom for fit A, $\chi^2_{\rm v} = 1.76$, indicates that the outlier supernovae included in this fit are probably not part of a Gaussian distribution and thus will not be appropriately weighted in a χ^2 fit. The χ^2 per degree of freedom for fit B, $\chi^2_{\rm v} = 1.16$, is over 300 times more probable than that of fit A and indicates that the remaining 56 supernovae are a reasonable fit to the model, with no large statistical errors remaining unaccounted for.

Of the two large-residual supernovae excluded from the fits after fit A, one is fainter than the best-fit prediction and one is brighter. The photometric color excess (see § 4.1) for the fainter supernova, SN 1997O, has an uncertainty that is too large to determine conclusively whether it is reddened. The brighter supernova, SN 1994H, is one of the first seven high-redshift supernovae originally analyzed in P97 and is one of the few supernovae without a spectrum to confirm its

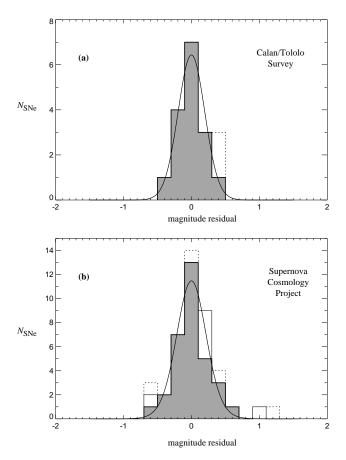


FIG. 3.—Distribution of rest-frame *B*-band magnitude residuals from the best-fit flat cosmology for the fit C supernova subset, for (a) 18 Calán/Tololo supernovae, at redshifts $z \le 0.1$ and (b) 42 supernovae from the Supernova Cosmology Project, at redshifts between 0.18 and 0.83. The darker shading indicates those residuals with uncertainties less than 0.35 mag, unshaded boxes indicate uncertainties greater than 0.35 mag, and dashed boxes indicate the supernovae that are excluded from fit C. The curves show the expected magnitude residual distributions if they are drawn from normal distributions given the measurement uncertainties and 0.17 mag of intrinsic SN Ia dispersion. The low-redshift expected distribution matches a Gaussian with $\sigma = 0.20$ mag (with error on the mean of 0.05 mag), while the high-redshift expected distribution matches a Gaussian with $\sigma = 0.22$ mag (with error on the mean of 0.04 mag).

classification as a SN Ia. After reanalysis with additional calibration data and improved K-corrections, it remains the brightest outlier in the current sample, but it affects the final cosmological fits much less as one of 42 supernovae, rather than 1 of 5 supernovae in the primary P97 analysis.

4. SYSTEMATIC UNCERTAINTIES AND CROSS-CHECKS

With our large sample of 42 high-redshift supernovae, it is not only possible to obtain good statistical uncertainties on the measured parameters but also to quantify several possible sources of systematic uncertainties. As discussed in P97, the primary approach is to examine subsets of our data that will be affected to lesser extents by the systematic uncertainty being considered. The high-redshift sample is now large enough that these subsets each contain enough supernovae to yield results of high statistical significance.

4.1. Extragalactic Extinction 4.1.1. Color-Excess Distributions

Although we have accounted for extinction due to our Galaxy, it is still probable that some supernovae are

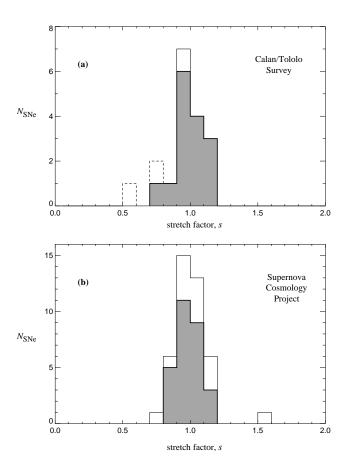


Fig. 4.—Distribution of light-curve widths for (a) 18 Calán/Tololo supernovae at redshifts $z \le 0.1$ and (b) 42 supernovae from the Supernova Cosmology Project at redshifts between 0.18 and 0.83. The light-curve widths are characterized by the "stretch factor," s, that stretches or contracts the time axis of a template SN Ia light curve to best fit the observed light curve for each supernova (see Perlmutter et al. 1995a, 1997e; Kim et al. 1999; Goldhaber et al. 1999). The template has been time-dilated by a factor 1 + z before fitting to the observed light curves to account for the cosmological lengthening of the supernova timescale (Goldhaber et al. 1995; Leibundgut et al. 1996a). The shading indicates those measurements of s with uncertainties less than 0.1, and the dashed lines indicate the two supernovae that are removed from the fits after fit A. These two excluded supernovae are the most significant deviations from s = 1 (the highest stretch supernova in panel b has an uncertainty of ± 0.23 and hence is not a significant outlier from s = 1); the remaining low- and high-redshift distributions have almost exactly the same error-weighted means: $\langle s \rangle_{\text{Hamuy}} = 0.99 \pm 0.01$ and $\langle s \rangle_{\text{SCP}} = 1.00 \pm 0.01$.

dimmed by host galaxy dust or intergalactic dust. For a standard dust extinction law (Cardelli et al. 1989) the color, B-V, of a supernova will become redder as the amount of extinction, A_B , increases. We thus can look for any extinction differences between the low- and high-redshift supernovae by comparing their rest-frame colors. Since there is a small dependence of intrinsic color on the light-curve width, supernova colors can only be compared for the same stretch factor; for a more convenient analysis, we subtract out the intrinsic colors so that the remaining color excesses can be compared simultaneously for all stretch factors. To determine the rest-frame color excess E(B-V) for each supernova, we fitted the rest-frame B and V photometry to the Band V SN Ia light-curve templates, with one of the fitting parameters representing the magnitude difference between the two bands at their respective peaks. Note that these light-curve peaks are ~2 days apart, so the resulting $B_{\rm max} - V_{\rm max}$ color parameter, which is frequently used to

TABLE 3
FIT RESULTS

| T::4 | NT | 2 | DOE | Oflat | P(O - 0) | Best Fit | Fit Description |
|-------------|-------|-------|------------|------------------------|---------------------------|----------------------------------|--|
| Fit | IN | χΞ | DOF | $\Omega_M^{ m flat}$ | $P(\Omega_{\Lambda} > 0)$ | $(\Omega_{M}, \Omega_{\Lambda})$ | Fit Description |
| Inclusive I | its: | | | | | | |
| A | 60 | 98 | 56 | $0.29^{+0.09}_{-0.08}$ | 0.9984 | 0.83, 1.42 | All supernovae |
| В | 56 | 60 | 52 | $0.26^{+0.09}_{-0.08}$ | 0.9992 | 0.85, 1.54 | Fit A, but excluding two residual outliers and two stretch outliers |
| D.: 6 | 4. | | | | | | |
| Primary fi | | | 5 0 | 0.20+0.09 | 0.0050 | 0.50 1.00 | T'(D 1 (1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 |
| C | 54 | 50 | 50 | $0.28^{+0.09}_{-0.08}$ | 0.9979 | 0.73, 1.32 | Fit B, but also excluding two likely reddened |
| Compariso | n Aı | alys | is Techr | niques: | | | |
| D | 54 | 53 | 51 | $0.25^{+0.10}_{-0.09}$ | 0.9972 | 0.76, 1.48 | No stretch correction ^a |
| E | 53 | 62 | 49 | $0.29^{+0.12}_{-0.10}$ | 0.9894 | 0.35, 0.76 | Bayesian one-sided extinction corrected ^b |
| Effect of R | edde | st Su | pernova | | | | |
| F | | | | $0.26^{+0.09}_{-0.08}$ | 0.9991 | 0.85, 1.54 | Fit B supernovae with colors measured |
| G | 49 | 56 | 45 | $0.28^{+0.09}_{-0.08}$ | 0.9974 | 0.73, 1.32 | Fit C supernovae with colors measured |
| Н | 40 | 33 | 36 | $0.31^{+0.11}_{-0.09}$ | 0.9857 | 0.16, 0.50 | Fit G, but excluding seven next reddest and two next faintest high-redshift supernovae |
| Systematic | Unc | ertai | nty Lin | | | | |
| I | 54 | 56 | 50 | $0.24^{+0.09}_{-0.08}$ | 0.9994 | 0.80, 1.52 | Fit C with +0.03 mag systematic offset |
| J | 54 | 57 | 50 | $0.33^{+0.10}_{-0.09}$ | 0.9912 | 0.72, 1.20 | Fit C with -0.04 mag systematic offset |
| Clumped 1 | Matte | er M | etrics: | 0.09 | | | • • |
| K | | | 50 | $0.35^{+0.12}_{-0.10}$ | 0.9984 | 2.90, 2.64 | Empty beam metric ^c |
| L | 54 | 56 | 50 | $0.34^{+0.10}_{-0.09}$ | 0.9974 | 0.94, 1.46 | Partially filled beam metric |

^a A 0.24 mag intrinsic SNe Ia luminosity dispersion is assumed.

describe supernova colors, is not a color measurement on a particular day. The difference of this color parameter from the $B_{\rm max}-V_{\rm max}$ found for a sample of low-redshift supernovae for the same light-curve stretch-factor (Tripp 1998; Kim et al. 1999; M. M. Phillips 1998, private communication) does yield the rest-frame E(B-V) color excess for the fitted supernova.

For the high-redshift supernovae at 0.3 < z < 0.7, the matching R- and I-band measurements take the place of the rest-frame B and V measurements, and the fit B and V light-curve templates are K-corrected from the appropriate matching filters, e.g., $R(t) = B(t) + K_{BR}(t)$ (Kim et al. 1996; Nugent et al. 1998). For the three supernovae at z > 0.75, the observed R - I corresponds more closely to a rest-frame U - B color than to a B - V color, so E(B - V) is calculated from rest-frame E(U - B) using the extinction law of Cardelli et al. (1989). Similarly, for the two SNe Ia at $z \sim 0.18$, E(B - V) is calculated from rest-frame E(V - R).

Figure 6 shows the color excess distributions for both the low- and high-redshift supernovae after removing the color excess due to our Galaxy. Six high-redshift supernovae are not shown on this E(B-V) plot, because six of the first seven high-redshift supernovae discovered were not observed in both R and I bands. The color of one lowredshift supernova, SN 1992bc, is poorly determined by the V-band template fit and has also been excluded. Two supernovae in the high-redshift sample are $>3 \sigma$ red-and-faint outliers from the mean in the joint probability distribution of E(B-V) color excess and magnitude residual from fit B. These two, SNe 1996cg and 1996cn (Fig. 6; light shading), are very likely reddened supernovae. To obtain a more robust fit of the cosmological parameters, in fit C we remove these supernovae from the sample. As can be seen from the fit-C 68% confidence region of Figure 5a, these likely reddened supernovae do not significantly affect any of our results. The main distribution of 38 high-redshift supernovae thus is barely affected by a few reddened events. We find identical results if we exclude the six supernovae without color measurements (fit G in Table 3). We take fit C to be our primary analysis for this paper, and in Figure 7 we show a more extensive range of confidence regions for this fit.

4.1.2. Cross-Checks on Extinction

The color-excess distributions of the fit C data set (with the most significant measurements highlighted by dark shading in Fig. 6) show no significant difference between the low- and high-redshift means. The dashed curve drawn over the high-redshift distribution of Figure 6 shows the expected distribution if the low-redshift distribution had the measurement uncertainties of the high-redshift supernovae indicated by the dark shading. This shows that the reddening distribution for the high-redshift supernovae is consistent with the reddening distribution for the lowredshift supernovae, within the measurement uncertainties. The error-weighted means of the low- and high-redshift distributions are almost identical: $\langle E(B-V) \rangle_{\text{Hamuy}} = 0.033$ \pm 0.014 mag and $\langle E(B-V)\rangle_{\text{SCP}}=0.035\pm0.022$ mag. We also find no significant correlation between the color excess and the statistical weight or redshift of the supernovae within these two redshift ranges.

To test the effect of any remaining high-redshift reddening on the fit C measurement of the cosmological parameters, we have constructed a fit H subset of the high-redshift supernovae that is intentionally biased to be bluer than the low-redshift sample. We exclude the error-weighted reddest 25% of the high-redshift supernovae; this excludes nine high-redshift supernovae with the highest error-weighted E(B-V). We further exclude two supernovae that have large uncertainties in E(B-V) but are significantly faint in their residual from fit C. This is a somewhat conservative cut, since it removes the faintest of the high-redshift supernovae, but it does ensure that the error-weighted E(B-V) mean of the remaining supernova

^b Bayesian method of RPK96 with conservative prior (see text and Appendix) and 0.10 mag intrinsic SNe Ia luminosity dispersion.

^c Assumes additional Bayesian prior of $\Omega_M < 3$, $\Omega_{\Lambda} < 3$.

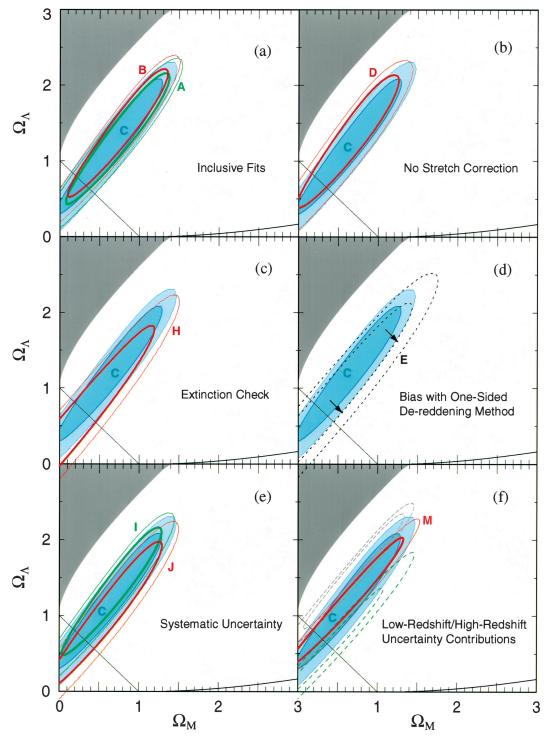


Fig. 5.—Comparison of best-fit confidence regions in the Ω_M - Ω_Λ plane. Each panel shows the result of fit C (shaded regions) compared with fits to different subsets of supernovae, or variant analyses for the same subset of supernovae, to test the robustness of the fit C result. Unless otherwise indicated, the 68% and 90% confidence regions in the Ω_M - Ω_Λ plane are shown after integrating the four-dimensional fits over the other two variables, \mathcal{M}_B and α . The "no-big-bang" shaded region at the upper left, the flat-universe diagonal line, and the infinite expansion line are shown as in Fig. 7 for ease of comparison. The panels are described as follows: (a) Fit A of all 60 supernovae and fit B of 56 supernovae, excluding the two outliers from the light-curve width distribution and the two remaining statistical outliers. Fit C further excludes the two likely reddened high-redshift supernovae. (b) Fit D of the same 54-supernova subset as in fit C, but with no correction for the light-curve width-luminosity relation. (c) Fit H of the subset of supernovae with color measurements, after excluding the reddest 25% (nine high-redshift supernovae) and the two faint high-redshift supernovae with large uncertainties in their color measurements. The close match to the confidence regions of fit C indicates that any extinction of these supernovae is quite small and not significant in the fits of the cosmological parameters. (d) 68% confidence region for Fit E of the 53 supernovae with color measurements from the fit B data set, but following the Bayesian reddening-correction method of RPK96. This method, when used with any reasonably conservative prior (i.e., somewhat broader than the likely true extinction distribution; see text), can produce a result that is biased, with an approximate bias direction and worst-case amount indicated by the arrows. (e) Fits I and J. These are identical to fit C but with 0.03 or 0.04 mag added or subtracted from each of the high-redshift supernova measurements to account for the full range of identified systematic uncertainty in each direction. Other hypothetical sources of systematic uncertainty (see Table 4B) are not included. (f) Fit M. This is a separate two-parameter $(\Omega_M$ and $\Omega_{\Lambda})$ fit of just the high-redshift supernovae, using the values of \mathcal{M}_B and α found from the low-redshift supernovae. The dashed confidence regions show the approximate range of uncertainty from these two low-redshift-derived parameters added to the systematic errors of fit J. Future well-observed low-redshift supernovae can constrain this dashed-line range of uncertainty.

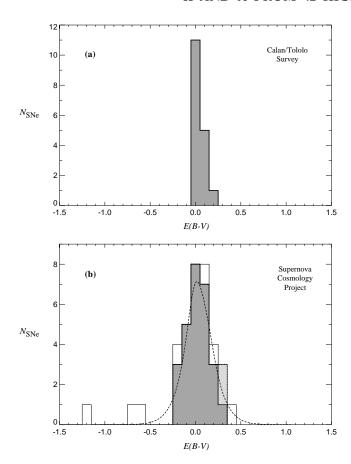


FIG. 6.—(a) Rest-frame B-V color excess distribution for 17 of 18 Calán/Tololo supernovae (see text), corrected for Galactic extinction using values from Schlegel et al. (1998). (b) Rest-frame B-V color excess for the 36 high-redshift supernovae for which rest-frame B-V colors were measured, also corrected for Galactic extinction. The darker shading indicates those E(B-V) measurements with uncertainties less than 0.3 mag, unshaded boxes indicate uncertainties greater than 0.3 mag, and the light shading indicates the two supernovae that are likely to be reddened based on their joint probability in color excess and magnitude residual from fit B. The dashed curve shows the expected high-redshift E(B-V) distribution if the low-redshift distribution had the measurement uncertainties of the high-redshift supernovae indicated by the dark shading. Note that most of the color-excess dispersion for the high-redshift supernovae is due to the rest-frame V-band measurement uncertainties, since the rest-frame B-band uncertainties are usually smaller.

subset is a good indicator of any reddening that could affect the cosmological parameters. The probability that the highredshift subset of fit H is redder in the mean than the lowredshift supernovae is less than 5%; This subset is thus very unlikely to be biased to fainter magnitudes by high-redshift reddening. Even with nonstandard, "grayer" dust that does not cause as much reddening for the same amount of extinction, a conservative estimate of the probability that the high-redshift subset of fit H is redder in the mean than the low-redshift supernovae is still less than $\sim 17\%$ for any high-redshift value of $\mathcal{R}_B \equiv A_B/E(B-V)$ less than twice the low-redshift value. [These same confidence levels are obtained whether using Gaussian statistics, assuming a normal distribution of E(B-V) measurements, or using bootstrap resampling statistics, based on the observed distribution.] The confidence regions of Figure 5c and the $\Omega_{M}^{\rm flat}$ results in Table 3 show that the cosmological parameters found for fit H differ by less than half of a standard deviation from those for fit C. We take the difference of these fits, 0.03 in Ω_M^{flat} (which corresponds to less than 0.025 in

magnitudes) as a ~ 1 σ upper bound on the systematic uncertainty due to extinction by dust that reddens.

Note that the modes of both distributions appear to be at zero reddening, and similarly the medians of the distributions are quite close to zero reddening: $\langle E(B-V) \rangle_{\rm Hamuy}^{\rm median} = 0.01$ mag and $\langle E(B-V) \rangle_{\rm SCP}^{\rm median} = 0.00$ mag. This should be taken as suggestive rather than conclusive, since the zero point of the relationship between true color and stretch is not tightly constrained by the current low-redshift SN Ia data set. This apparent strong clustering of SNe Ia about zero reddening has been noted in the past for low-redshift supernova samples. Proposed explanations have been given based on the relative spatial distributions of the SNe Ia and the dust: Modeling by Hatano, Branch, & Deaton (1998) of the expected extinction of SN Ia disk and bulge populations viewed at random orientations shows an extinction distribution with a strong spiked peak near zero extinction along with a broad, lower probability wing to higher extinction. This wing will be further suppressed by the observational selection against more reddened supernovae, since they are dimmer. (For a flux-limited survey this suppression factor is $10^{-a_R[\mathcal{R}_BE(B-V)-\alpha(s-1)]} \approx 10^{-1.6E(B-V)}$, where a_R is the slope of the supernova number counts.) We also note that the high-redshift supernovae for which we have accurate measurements of apparent separation between SN and host position (generally, those with HST imaging) appear to be relatively far from the host center, despite our high search sensitivity to supernovae in front of the host galaxy core (see Pain et al. 1996 for search efficiency studies; also cf. Wang, Höflich, & Wheeler 1997). If generally true for the entire sample, this would be consistent with little extinction.

Our results, however, do not depend on the low- and high-redshift color-excess distributions being consistent with zero reddening. It is only important that the reddening distributions for the low-redshift and high-redshift data sets are statistically the same and that there is no correlation between reddening and statistical weight in the fit of the cosmological parameters. With both of these conditions satisfied, we find that our measurement of the cosmological parameters is unaffected (to within the statistical error) by any small remaining extinction among the supernovae in the two data sets.

4.1.3. Analysis with Reddening Correction of Individual Supernovae

We have also performed fits using rest-frame B-band magnitudes individually corrected for host galaxy extinction using $A_B = \mathcal{R}_B E(B-V)$ (implicitly assuming that the extragalactic extinction is all at the redshift of the host galaxy). As a direct comparison between the treatment of host galaxy extinction described above and an alternative Bayesian method (RPK96), we applied it to the 53 SNe Ia with color measurements in our fit C data set. We find that our cosmological parameter results are robust with respect to this change, although this method can introduce a bias into the extinction corrections and hence the cosmological parameters. In brief, in this method the Gaussian extinction probability distribution implied by the measured colorexcess and its error is multiplied by an assumed a priori probability distribution (the Bayesian prior) for the intrinsic distribution of host extinctions. The most probable value of the resulting renormalized probability distribution is taken as the extinction, and following A. Riess (1998, private communication) the second-moment is taken as the uncertainty. For this analysis, we choose a conservative prior (as given in RPK96) that does not assume that the supernovae are unextinguished but rather is somewhat broader than the true extinction distribution where the majority of the previously observed supernovae apparently suffer very little reddening. (If one alternatively assumes that the current data's extinction distribution is quite as narrow as that of previously observed supernovae, one can choose a less conservative but more realistic narrow prior probability distribution, such as that of Hatano et al. 1998. This turns out to be quite similar to our previous analysis in § 4.1.1, since a distribution like that of Hatano et al. 1998 has zero extinction for most supernovae.)

This Bayesian method with a conservative prior will only brighten supernovae, never make them fainter, since it only affects the supernovae with redder measurements than the zero-extinction E(B-V) value, leaving unchanged those measured to be bluer than this. The resulting slight difference between the assumed and true reddening distributions would make no difference in the cosmology measurements if its size were the same at low and high redshifts. However, since the uncertainties, $\sigma_{E(B-V)}^{high-z}$, in the high-redshift data set E(B-V) measurements are larger on average than those of the low-redshift data set, $\sigma_{E(B-V)}^{low-z}$, this method can overcorrect the high-redshift supernovae on average relative to the low-redshift supernovae. Fortunately, as shown in the Appendix, even an extreme case with a true distribution all at zero extinction and a conservative prior would introduce a bias in extinction A_B only of order 0.1 mag at worst for our current low- and high-redshift measurement uncertainties. The results of fit E are shown in Table 3 and as the dashed contour in Figure 5d, where it can be seen that compared to fit C this approach moves the best-fit value much less than this and in the direction expected for this effect (Fig. 5d; arrows). The fact that Ω_M^{flat} changes so little from case C, even with the possible bias, gives further confidence in the cosmological results.

We can eliminate any such small bias of this method by assuming no Bayesian prior on the host-galaxy extinction, allowing extinction corrections to be negative in the case of supernovae measured to be bluer than the zero-extinction E(B-V) value. As expected, we recover the unbiased results within error but with larger uncertainties, since the Bayesian prior also narrows the error bars in the method of RPK96. However, there remains a potential source of bias when correcting for reddening: the effective ratio of total to selective extinction, \mathcal{R}_B , could vary for several reasons. First, the extinction could be due to host galaxy dust at the supernova's redshift or intergalactic dust at lower redshifts, where it will redden the supernova less, since it is acting on a redshifted spectrum. Second, \mathcal{R}_B may be sensitive to dust density, as indicated by variations in the dust extinction laws between various sight lines in the Galaxy (Clayton & Cardelli 1988; Gordon & Clayton 1998). Changes in metallicity might be expected to be a third possible cause of \mathcal{R}_B evolution, since metallicity is one dust-related quantity known to evolve with redshift (Pettini et al. 1997), but fortunately it appears not to significantly alter \mathcal{R}_B , as evidenced by the similarity of the optical portions of the extinction curves of the Galaxy, the LMC, and the SMC (Pei 1992; Gordon & Clayton 1998). Three-filter photometry of highredshift supernovae currently in progress with the HST will help test for such differences in \mathcal{R}_B .

To avoid these sources of bias, we consider it important to use and compare both analysis approaches: the rejection of reddened supernovae and the correction of reddened supernovae. We do find consistency in the results calculated both ways. The advantages of the analyses with reddening corrections applied to individual supernovae (with or without a Bayesian prior on host-galaxy extinction) are outweighed by the disadvantages for our sample of highredshift supernovae; although, in principle, by applying reddening corrections the intrinsic magnitude dispersion of SNe Ia can be reduced from an observed dispersion of 0.17 mag to approximately 0.12 mag, in practice the net improvement for our sample is not significant, since uncertainties in the color measurements often dominate. We have therefore chosen for our primary analysis to follow the first procedure discussed above, removing the likely reddened supernovae (fit C) and then comparing color-excess means. The systematic difference for fit H, which rejects the reddest and the faintest high-redshift supernovae, is already quite small, and we avoid introducing additional actual and possible biases. Of course, neither approach avoids biases if \mathcal{R}_B at high redshift is so large $[> 2\mathcal{R}_B(z=0)]$ that dust does not redden the supernovae enough to be distinguished and this dust makes more than a few supernovae faint.

4.2. Malmquist Bias and Other Luminosity Biases

In the fit of the cosmological parameters to the magnitude-redshift relation, the low-redshift supernova magnitudes primarily determine \mathcal{M}_B and the widthluminosity slope α , and then the comparison with the highredshift supernova magnitudes primarily determines Ω_{M} and Ω_{Λ} . Both low- and high-redshift supernova samples can be biased toward selecting the brighter tail of any distribution in supernova detection magnitude for supernovae found near the detection threshold of the search (classical Malmquist bias; Malmquist 1924, 1936). A widthluminosity relation fit to such a biased population would have a slope that is slightly too shallow and a zero point slightly too bright. A second bias is also acting on the supernova samples, selecting against supernovae on the narrowlight-curve side of the width-luminosity relation, since such supernovae are detectable for a shorter period of time. Since this bias removes the narrowest/faintest supernova light curves preferentially, it culls out the part of the widthbrightness distribution most subject to Malmquist bias and moves the resulting best-fit slope and zero point closer to their correct values.

If the Malmquist bias is the same in both data sets, then it is completely absorbed by \mathcal{M}_B , and α and does not affect the cosmological parameters. Thus our principal concern is that there could be a difference in the amount of bias between the low- and high-redshift samples. Note that effects peculiar to photographic supernovae searches, such as saturation in galaxy cores, that might in principle select slightly different SNe Ia subpopulations should not be important in determining luminosity bias, because light-curve stretch compensates for any such differences. Moreover, Figure 4 shows that the high-redshift SNe Ia we have discovered have a stretch distribution entirely consistent with those discovered in the Calán/Tololo search.

To estimate the Malmquist bias of the high-redshift-supernova sample, we first determined the completeness of our high-redshift searches as a function of magnitude, through an extensive series of tests inserting artificial supernovae into our images (see Pain et al. 1996). We find that roughly 30% of our high-redshift supernovae were detected within twice the SN Ia intrinsic luminosity dispersion of the 50% completeness limit, where the above biases might be important. This is consistent with a simple model where the

supernova number counts follow a power-law slope of 0.4 mag⁻¹, similar to that seen for comparably distant galaxies (Smail et al. 1995). For a flux-limited survey of standard candles having the light-curve width-corrected luminosity dispersion for SNe Ia of ~ 0.17 mag and this number-count power-law slope, we can calculate that the classical Malmquist bias should be 0.03 mag (see, e.g., Mihalas & Binney 1981 for a derivation of the classical Malmquist bias). (Note that this estimate is much smaller than the Malmquist bias affecting other cosmological distance indicators because of the much smaller intrinsic luminosity dispersion of SNe Ia.) These high-redshift supernovae, however, are typically detected before maximum, and their detection magnitudes and peak magnitudes have a correlation coefficient of only 0.35, so the effects of classical Malmquist bias should be diluted. Applying the formalism of Willick (1994) we estimate that the decorrelation between detection magnitude and peak magnitude reduces the classical Malmquist bias in the high-redshift sample to only 0.01 mag. The redshift and stretch distributions of the high-redshift supernovae that are near the 50% completeness limit track those of the overall high-redshift sample, again suggesting that Malmquist biases are small for our data set.

We cannot make an exactly parallel estimate of Malmquist bias for the low-redshift-supernova sample, because we do not have information for the Calán/Tololo data set concerning the number of supernovae found near the detection limit. However, the amount of classical Malmquist bias should be similar for the Calán/Tololo supernovae, since the amount of bias is dominated by the intrinsic luminosity dispersion of SNe Ia, which we find to be the same for the low-redshift and high-redshift samples (see § 5). Figure 4 shows that the stretch distributions for the high- and lowredshift samples are very similar, so that the compensating effects of stretch bias should also be similar in the two data sets. The major source of difference in the bias is expected to be due to the close correlation between the detection magnitude and the peak magnitude for the low-redshift supernova search, since this search tended not to find the supernovae as early before peak as the high-redshift search. In addition, the number-counts at low-redshift should be somewhat steeper (Maddox et al. 1990). We thus expect the Calán/Tololo supernovae to have a bias closer to that obtained by direct application of the classical Malmquist bias formula, 0.04 mag. One might also expect "inhomogeneous Malmquist bias" to be more important for the low-redshift supernovae, since in smaller volumes of space inhomogeneities in the host galaxy distribution might by chance put more supernovae near the detection limit than would be expected for a homogeneous distribution. However, after averaging over all the Calán/Tololo supernova-search fields, the total low-redshift volume searched is large enough that we expect galaxy count fluctuations of only $\sim 4\%$, so the classical Malmquist bias is still a good approximation.

We believe that both these low- and high-redshift biases may be smaller and even closer to each other, because of the mitigating effect of the bias against detection of low-stretch supernovae, discussed above. However, to be conservative we take the classical Malmquist bias of 0.04 mag for the low-redshift data set and the least biased value of 0.01 mag for the high-redshift data set, and we consider systematic uncertainty from this source to be the difference, 0.03 mag, in the direction of low-redshift supernovae more biased than high-redshift. In the other direction, i.e., for high-

redshift supernovae more biased than low-redshift, we consider the extreme case of a fortuitously unbiased low-redshift sample and take the systematic uncertainty bound to be the 0.01 mag bias of the high-redshift sample. (In this direction any systematic error is less relevant to the question of the existence of a cosmological constant.)

4.3. Gravitational Lensing

As discussed in P97, the clumping of mass in the universe could leave the line-of-sight to most of the supernovae underdense, while occasional supernovae may be seen through overdense regions. The latter supernovae could be significantly brightened by gravitational lensing, while the former supernovae would appear somewhat fainter. With enough supernovae, this effect will average out (for inclusive fits such as fit A, which include outliers), but the most overdense lines of sight may be so rare that a set of 42 supernovae may only sample a slightly biased (fainter) set. The probability distribution of these amplifications and deamplifications has previously been studied both analytically and by Monte Carlo simulations. Given the acceptance window of our supernova search, we can integrate the probability distributions from these studies to estimate the bias due to amplified or deamplified supernovae that may be rejected as outliers. This average (de)amplification bias is less than 1% at the redshifts of our supernovae for simulations based on isothermal spheres the size of typical galaxies (Holz & Wald 1998), N-body simulations using realistic mass power spectra (Wambsganss, Cen, & Ostriker 1998), and the analytic models of Frieman (1996).

It is also possible that the small-scale clumping of matter is more extreme, for example, if significant amounts of mass were in the form of compact objects such as MACHOs. This could lead to many supernova sight lines that are not just underdense but nearly empty. Once again, only the very rare line of sight would have a compact object in it, amplifying the supernova signal. To first approximation, with 42 supernovae we would see only the nearly empty beams and thus only deamplifications. The appropriate luminositydistance formula in this case is not the Friedmann-Robertson-Walker (FRW) formula but rather the "partially filled beam" formula with a mass filling factor, $\eta \approx 0$ (see Kantowski 1998 and references therein). We present the results of the fit of our data (fit K) with this luminositydistance formula (as calculated using the code of Kayser, Helbig, & Schramm 1996) in Figure 8. A more realistic limit on this pointlike mass density can be estimated, because we would expect such pointlike masses to collect into the gravitational potential wells already marked by galaxies and clusters. Fukugita, Hogan, & Peebles (1998) estimate an upper limit of $\Omega_M < 0.25$ on the mass that is clustered like galaxies. In Figure 8, we also show the confidence region from fit L, assuming that only the mass density contribution up to $\Omega_M = 0.25$ is pointlike, with filling factor $\eta = 0$, and that η rises to 0.75 at $\Omega_M = 1$. We see that at low mass density, the FRW fit is already very close to the nearly empty-beam $(\eta \approx 0)$ scenario, so the results are quite similar. At high mass density, the results diverge, although only minimally for fit L; the best fit in a flat universe is $\Omega_M^{\text{flat}} = 0.34^{+0.10}_{-0.09}.$

4.4. Supernova Evolution and Progenitor Environment Evolution

The spectrum of a SN Ia on any given point in its light curve reflects the complex physical state of the supernova

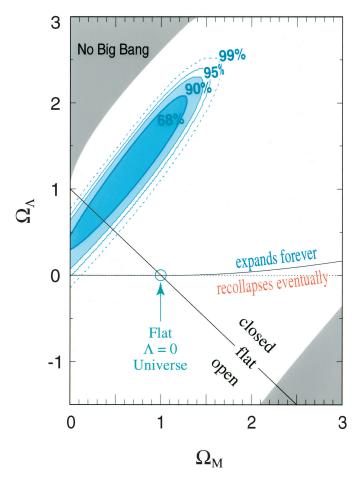


Fig. 7.—Best-fit confidence regions in the Ω_M - Ω_Λ plane for our primary analysis, fit C. The 68%, 90%, 95%, and 99% statistical confidence regions in the $\Omega_M \! - \! \Omega_\Lambda$ plane are shown, after integrating the four-dimensional fit over \mathcal{M}_B and α . (See footnote 11 for a link to the table of this twodimensional probability distribution.) See Fig. 5e for limits on the small shifts in these contours due to identified systematic uncertainties. Note that the spatial curvature of the universe—open, flat, or closed—is not determinative of the future of the universe's expansion, indicated by the nearhorizontal solid line. In cosmologies above this near-horizontal line the universe will expand forever, while below this line the expansion of the universe will eventually come to a halt and recollapse. This line is not quite horizontal, because at very high mass density there is a region where the mass density can bring the expansion to a halt before the scale of the universe is big enough that the mass density is dilute with respect to the cosmological constant energy density. The upper-left shaded region, labeled "no big bang," represents "bouncing universe" cosmologies with no big bang in the past (see Carroll et al. 1992). The lower right shaded region corresponds to a universe that is younger than the oldest heavy elements (Schramm 1990) for any value of $H_0 \ge 50 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

on that day: the distribution, abundances, excitations, and velocities of the elements that the photons encounter as they leave the expanding photosphere all imprint on the spectra. So far, the high-redshift supernovae that have been studied have light-curve shapes just like those of low-redshift supernovae (see Goldhaber et al. 1999), and their spectra show the same features on the same day of the light curve as their low-redshift counterparts having comparable light-curve width. This is true all the way out to the z=0.83 limit of the current sample (Perlmutter et al. 1998b). We take this as a strong indication that the physical parameters of the supernova explosions are not evolving significantly over this time span.

Theoretically, evolutionary effects might be caused by changes in progenitor populations or environments. For

example, lower metallicity and more massive SN Iaprogenitor binary systems should be found in younger stellar populations. For the redshifts that we are considering, z < 0.85, the change in average progenitor masses may be small (Ruiz-Lapuente, Canal, & Burkert 1997; Ruiz-Lapuente 1998). However, such progenitor mass differences or differences in typical progenitor metallicity are expected to lead to differences in the final C/O ratio in the exploding white dwarf and hence affect the energetics of the explosion. The primary concern here would be if this changed the zero-point of the width-luminosity relation. We can look for such changes by comparing light curve rise times between low- and high-redshift supernova samples, since this is a sensitive indicator of explosion energetics. Preliminary indications suggest that no significant rise-time change is seen, with an upper limit of $\lesssim 1$ day for our sample (see forthcoming high-redshift studies of Goldhaber et al. 1999 and Nugent et al. 1998 and low-redshift bounds from Vacca & Leibundgut 1996, Leibundgut et al. 1996b, and Marvin & Perlmutter 1989). This tight a constraint on rise-time change would theoretically limit the zero-point change to less than ~ 0.1 mag (see Nugent et al. 1995; Höflich, Wheeler, & Thielemann 1998).

A change in typical C/O ratio can also affect the ignition density of the explosion and the propagation characteristics of the burning front. Such changes would be expected to appear as differences in light-curve timescales before and after maximum (Höflich & Khokhlov 1996). Preliminary indications of consistency between such low- and high-redshift light-curve timescales suggest that this is probably not a major effect for our supernova samples (Goldhaber et al. 1999).

Changes in typical progenitor metallicity should also directly cause some differences in SN Ia spectral features (Höflich et al. 1998). Spectral differences big enough to affect the *B*- and *V*-band light curves (see, e.g., the extreme mixing models presented in Fig. 9 of Höflich et al. 1998) should be clearly visible for the best signal-to-noise ratio spectra we have obtained for our distant supernovae, yet they are not seen (Filippenko et al. 1998; Hook et al. 1998). The consistency of slopes in the light-curve width-luminosity relation for the low- and high-redshift supernovae can also constrain the possibility of a strong metallicity effect of the type that Höflich et al. (1998) describes.

An additional concern might be that even small changes in spectral features with metallicity could in turn affect the calculations of K-corrections and reddening corrections. This effect, too, is very small, less than 0.01 mag, for photometric observations of SNe Ia conducted in the rest-frame B or V bands (see Figs. 8 and 10 of Höflich et al. 1998), as is the case for almost all of our supernovae. (Only two of our supernovae have primary observations that are sensitive to the rest-frame U band, where the magnitude can change by ~ 0.05 mag, and these are the two supernovae with the lowest weights in our fits, as shown by the error bars of Fig. 2. In general the I-band observations, which are mostly sensitive to the rest-frame B band, provide the primary light curve at redshifts above 0.7.)

The above analyses constrain only the effect of progenitor-environment evolution on SN Ia intrinsic luminosity; however, the extinction of the supernova light could also be affected, if the amount or character of the dust evolves, e.g., with host galaxy age. In § 4.1, we limited the

size of this extinction evolution for dust that reddens, but evolution of "gray" dust grains larger than $\sim 0.1~\mu m$, which would cause more color-neutral optical extinction, can evade these color measurements. The following two analysis approaches can constrain both evolution effects, intrinsic SN Ia luminosity evolution and extinction evolution. They take advantage of the fact that galaxy properties such as formation age, star formation history, and metallicity are not monotonic functions of redshift, so even the low-redshift SNe Ia are found in galaxies with a wide range of ages and metallicities. It is a shift in the distribution of relevant host-galaxy properties occurring between $z \sim 0$ and $z \sim 0.5$ that could cause any evolutionary effects.

Width-luminosity relation across low-redshift environments: To the extent that low-redshift SNe Ia arise from progenitors with a range of metallicities and ages, the lightcurve width-luminosity relation discovered for these supernovae can already account for these effects (cf. Hamuy et al. 1995, 1996). When corrected for the width-luminosity relation, the peak magnitudes of low-redshift SNe Ia exhibit a very narrow magnitude dispersion about the Hubble line, with no evidence of a significant progenitor-environment difference in the residuals from this fit. It therefore does not matter if the population of progenitors evolves such that the measured light-curve widths change, since the widthluminosity relation apparently is able to correct for these changes. It will be important to continue to study further nearby SNe Ia to test this conclusion with as wide a range of host-galaxy ages and metallicities as possible.

Matching low- and high-redshift environments: Galaxies with different morphological classifications result from different evolutionary histories. To the extent that galaxies with similar classifications have similar histories, we can also check for evolutionary effects by using supernovae in our cosmology measurements with matching host galaxy classifications. If the same cosmological results are found for each measurement based on a subset of low- and highredshift supernovae sharing a given host-galaxy classification, we can rule out many evolutionary scenarios. In the simplest such test, we compare the cosmological parameters measured from low- and high-redshift elliptical host galaxies with those measured from low- and high-redshift spiral host galaxies. Without high-resolution host-galaxy images for most of our high-redshift sample, we currently can only approximate this test for the smaller number of supernovae for which the host-galaxy spectrum gives a strong indication of galaxy classification. The resulting sets of nine elliptical-host and eight spiral-host high-redshift supernovae are matched to the four elliptical-host and 10 spiral-host low-redshift supernovae (based on the morphological classifications listed in Hamuy et al. 1996 and excluding two with SB0 hosts). We find no significant change in the best-fit cosmology for the elliptical hostgalaxy subset (with both the low- and high-redshift subsets about 1 σ brighter than the mean of the full sets) and a small $(<1 \sigma)$ shift lower in $\Omega_M^{\rm flat}$ for the spiral host-galaxy subset. Although the consistency of these subset results is encourthe uncertainties are still large (approximately twice the fit C uncertainties) that this test will need to await the host-galaxy classification of the full set of high-redshift supernovae and a larger low-redshift supernova sample.

4.5. Further Cross-Checks

We have checked several other possible effects that might

bias our results by fitting different supernova subsets and using alternative analyses:

Sensitivity to width-luminosity correction: Although the light-curve width correction provides some insurance against supernova evolution biasing our results, Figure 4 shows that almost all of the fit C supernovae at both low and high redshift are clustered tightly around the most probable value of s = 1, the standard width for a B-band Leibundgut SN Ia template light curve. Our results are therefore rather robust with respect to the actual choice of width-luminosity relation. We have tested this sensitivity by refitting the supernovae of fit C but with no widthluminosity correction. The results (fit D), as shown in Figure 5b and listed in Table 3, are in extremely close agreement with those of the light-curve-width-corrected fit C. The statistical uncertainties are also quite close; the lightcurve width correction does not significantly improve the statistical dispersion for the magnitude residuals because of the uncertainty in s, the measured light-curve width. It is clear that the best-fit cosmology does not depend strongly on the extra degree of freedom allowed by including the width-luminosity relation in the fit.

Sensitivity to non–SN Ia contamination: We have tested for the possibility of contamination by non–SN Ia events masquerading as SNe Ia in our sample by performing a fit after excluding any supernovae with less certain SN Ia spectroscopic and photometric identification. This selection removes the large statistical outliers from the sample. In part, this may be because the host-galaxy contamination that can make it difficult to identify the supernova spectrum can also increase the odds of extinction or other systematic uncertainties in photometry. For this more "pure" sample of 43 supernovae, we find $\Omega_{-0.09}^{\rm flat} = 0.33^{+0.10}_{-0.09}$, just over half of a standard deviation from fit C.

Sensitivity to galactic extinction model: Finally, we have tested the effect of the choice of Galactic extinction model, with a fit using the model of Burstein & Heiles (1982), rather than Schlegel et al. (1998). We find no significant difference in the best-fit cosmological parameters, although we note that the extinction near the Galactic pole is somewhat larger in the Schlegel et al. model and that this leads to a ~ 0.03 mag larger average offset between the low-redshift supernova B-band observations and the high-redshift supernovae R-band observations.

5. RESULTS AND ERROR BUDGET

From Table 3 and Figure 5a, it is clear that the results of fits A, B, and C are quite close to each other, so we can conclude that our measurement is robust with respect to the choice of these supernova subsets. The inclusive fits A and B are the fits with the least subjective selection of the data. They already indicate the main cosmological results from this data set. However, to make our results robust with respect to host-galaxy reddening, we use fit C as our primary fit in this paper. For fit C, we find $\Omega_M^{\rm flat} = 0.28^{+0.09}_{-0.08}$ in a flat universe. Cosmologies with $\Omega_{\Lambda} = 0$ are a poor fit to the data at the 99.8% confidence level. The contours of Figure 7 more fully characterize the best-fit confidence regions. 12

The residual plots of Figures 2b and 2c indicate that the best-fit $\Omega_M^{\rm flat}$ in a flat universe is consistent across the redshift range of the high-redshift supernovae. Figure 2c shows

¹² The data are available at http://www-supernova.lbl.gov.

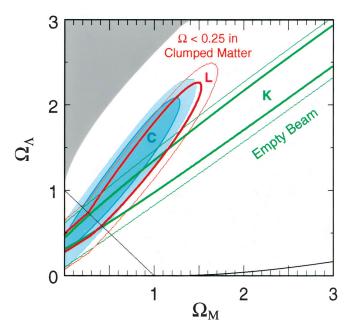


FIG. 8.—Best-fit 68% and 90% confidence regions in the Ω_M - Ω_Λ plane for cosmological models with small scale clumping of matter (e.g., in the form of MACHOs) compared with the FRW model of fit C, with smooth small-scale matter distribution. The shaded contours (fit C) are the confidence regions fit to a FRW magnitude-redshift relation. The extended confidence strips (fit K) are for a fit of the fit C supernova set to an "empty beam" cosmology, using the "partially filled beam" magnitude-redshift relation with a filling factor $\eta=0$, representing an extreme case in which all mass is in compact objects. The fit L unshaded contours represent a somewhat more realistic partially filled-beam fit, with clumped matter $(\eta=0)$ only accounting for up to $\Omega_M=0.25$ of the critical mass density and any matter beyond that amount smoothly distributed (i.e., η rising to 0.75 at $\Omega_M=1$).

the residuals normalized by uncertainties; their scatter can be seen to be typical of a normal-distributed variable, with the exception of the two outlier supernovae that are removed from all fits after fit A, as discussed above. Figure 3 compares the magnitude-residual distributions (the projections of Fig. 2b) to the Gaussian distributions expected given the measurement uncertainties and an intrinsic dispersion of 0.17 mag. Both the low- and high-redshift distributions are consistent with the expected distributions; the formal calculation of the SN Ia intrinsic-dispersion component of the observed magnitude dispersion $(\sigma_{\text{intrinsic}}^2 = \sigma_{\text{observed}}^2 - \sigma_{\text{measurement}}^2)$ yields $\sigma_{\text{intrinsic}} = 0.154 \pm 0.04$ for the low-redshift distribution and $\sigma_{\text{intrinsic}} = 0.036$ for the low-redshift distribution and $\sigma_{\text{intrinsic}} = 0.036$ for the low-redshift distribution. 0.157 ± 0.025 for the high-redshift distribution. The χ^2 per degree of freedom for this fit, $\chi^2_{\nu} = 1.12$, also indicates that the fit model is a reasonable description of the data. The narrow intrinsic dispersion—which does not increase at high redshift-provides additional evidence against an increase in extinction with redshift. Even if there is gray dust that dims the supernovae without reddening them, the dispersion would increase, unless the dust is distributed very uniformly.

A flat, $\Omega_{\Lambda} = 0$ cosmology is a quite poor fit to the data. The $(\Omega_M, \Omega_{\Lambda}) = (1, 0)$ line on Figure 2b shows that 38 out of 42 high-redshift supernovae are fainter than predicted for this model. These supernovae would have to be over 0.4 mag brighter than measured (or the low-redshift supernovae 0.4 mag fainter) for this model to fit the data.

The $(\Omega_M, \Omega_{\Lambda}) = (0, 0)$ upper solid line on Figure 2a shows that the data are still not a good fit to an "empty universe," with zero mass density and cosmological constant. The

high-redshift supernovae are as a group fainter than predicted for this cosmology; in this case, these supernovae would have to be almost 0.15 mag brighter for this empty cosmology to fit the data, and the discrepancy is even larger for $\Omega_M > 0$. This is reflected in the high probability (99.8%) of $\Omega_{\Lambda} > 0$.

As discussed in Goobar & Perlmutter (1995), the slope of the contours in Figure 7 is a function of the supernova redshift distribution; since most of the supernovae reported here are near $z \sim 0.5$, the confidence region is approximately fitted by $0.8\Omega_M - 0.6\Omega_\Lambda \approx -0.2 \pm 0.1$. (The orthogonal linear combination, which is poorly constrained, is fitted by $0.6\Omega_M + 0.8\Omega_\Lambda \approx 1.5 \pm 0.7$.) In P97 we emphasized that the well-constrained linear combination is not parallel to any contour of constant current-deceleration-parameter, $q_0 \equiv \Omega_M/2 - \Omega_\Lambda$; the accelerating/decelerating universe line of Figure 9 shows one such contour at $q_0 = 0$. Note that with almost all of the confidence region above this line, only currently accelerating universes fit the data well. As more of our highest redshift supernovae are analyzed, the long dimension of the confidence region will shorten.

5.1. Error Budget

Most of the sources of statistical error contribute a statistical uncertainty to each supernova individually and are included in the uncertainties listed in Tables 1 and 2, with small correlations between these uncertainties given in the correlated-error matrices. 13 These supernova-specific statistical uncertainties include the measurement errors on SN peak magnitude, light-curve stretch factor, and absolute photometric calibration. The two sources of statistical error that are common to all the supernovae are the intrinsic dispersion of SN Ia luminosities after correcting for the width-luminosity relation, taken as 0.17 mag, and the redshift uncertainty due to peculiar velocities, which are taken as 300 km s⁻¹. Note that the statistical error in \mathcal{M}_B and α are derived quantities from our four-parameter fits. By integrating the four-dimensional probability distributions over these two variables, their uncertainties are included in the final statistical errors.

All uncertainties that are not included in the statistical error budget are treated as systematic errors for the purposes of this paper. In §§ 2 and 4, we have identified and bounded four potentially significant sources of systematic uncertainty: (1) the extinction uncertainty for dust that reddens, bounded at < 0.025 mag, the maximal effect of the nine reddest and two faintest of the high-redshift supernovae; (2) the difference between the Malmquist bias of the low- and high-redshift supernovae, bounded at ≤ 0.03 mag for low-redshift supernovae biased intrinsically brighter than high-redshift supernovae and at < 0.01 mag for highredshift supernovae biased brighter than low-redshift supernovae; (3) the cross-filter K-correction uncertainty of < 0.02mag; and (4) the <0.01 mag uncertainty in K-corrections and reddening corrections due to the effect of progenitor metallicity evolution on the rest-frame B-band spectral features. We take the total identified systematic uncertainty to be the quadrature sum of the sources: +0.04 mag in the direction of spuriously fainter high-redshift or brighter lowredshift supernovae and -0.03 mag in the opposite direc-

Note that we treat the possibility of gravitational lensing

¹³ The data are available at http://www-supernova.lbl.gov.

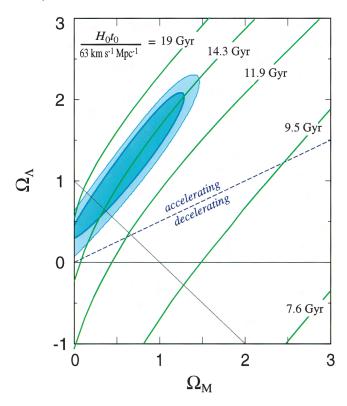


FIG. 9.—Isochrones of constant $H_0\,t_0$, the age of the universe relative to the Hubble time, H_0^{-1} , with the best-fit 68% and 90% confidence regions in the $\Omega_{\rm M}$ - Ω_{Λ} plane for the primary analysis, fit C. The isochrones are labeled for the case of $H_0=63~{\rm km~s^{-1}~Mpc^{-1}}$, representing a typical value found from studies of SNe Ia (Hamuy et al. 1996; RPK96; Saha et al. 1997; Tripp 1998). If H_0 were taken to be 10% larger (i.e., closer to the values in Freedman et al. 1998), the age labels would be 10% smaller. The diagonal line labeled accelerating/decelerating is drawn for $q_0\equiv\Omega_{\rm M}/2-\Omega_{\Lambda}=0$ and divides the cosmological models with an accelerating or decelerating expansion at the present time.

due to small-scale clumping of mass as a separate analysis case rather than as a contributing systematic error in our primary analysis; the total systematic uncertainty applies to this analysis as well. There are also several more hypothetical sources of systematic error discussed in § 4, which are not included in our calculation of identified systematics. These include gray dust [with $\mathcal{R}_B(z=0.5) > 2\mathcal{R}_B(z=0)$] and any SN Ia evolutionary effects that might change the zero point of the light-curve width-luminosity relation. We have presented bounds and tests for these effects, which give preliminary indications that they are not large sources of uncertainty, but at this time they remain difficult to quantify, at least partly because the proposed physical processes and entities that might cause the effects are not completely defined

To characterize the effect of the identified systematic uncertainties, we have refit the supernovae of fit C for the hypothetical case (fit J) in which each of the high-redshift supernovae were discovered to be 0.04 mag brighter than measured, or, equivalently, the low-redshift supernovae were discovered to be 0.04 mag fainter than measured. Figure 5e and Table 3 show the results of this fit. The bestfit flat-universe $\Omega_M^{\rm flat}$ varies from that of fit C by 0.05, less than the statistical error bar. The probability of $\Omega_\Lambda > 0$ is still over 99%. When we fitted with the smaller systematic error in the opposite direction (i.e., high-redshift supernovae discovered to be 0.03 mag fainter than measured), we find (fit I) only a 0.04 shift in $\Omega_M^{\rm flat}$ from fit C.

The measurement error of the cosmological parameters has contributions from both the low- and high-redshift supernova data sets. To identify the approximate relative importance of these two contributory sources, we reanalyzed the fit C data set, first fitting \mathcal{M}_B and α to the low-redshift data set (this is relatively insensitive to cosmological model) and then fitting Ω_M and Ω_{Λ} to the highredshift data set. (This is only an approximation, since it neglects the small influence of the low-redshift supernovae on Ω_M and Ω_{Λ} and of the high-redshift supernovae on \mathcal{M}_B and α , in the standard four-parameter fit.) Figure 5 shows this Ω_M - Ω_Λ fitted as a solid contour (labeled fit M) with the 1 σ uncertainties on \mathcal{M}_B and α included with the systematic uncertainties in the dashed-line confidence contours. This approach parallels the analyses of Permutter et al. (1997e, 1998b; 1997f) and thus also provides a direct comparison with the earlier results. We find that the more important contribution to the uncertainty is currently due to the lowredshift supernova sample. If three times as many wellobserved low-redshift supernovae were discovered and included in the analysis, then the statistical uncertainty from the low-redshift data set would be smaller than the other sources of uncertainty.

We summarize the relative statistical and systematic uncertainty contributions in Table 4.

6. CONCLUSIONS AND DISCUSSION

The confidence regions of Figure 7 and the residual plot of Figure 2b lead to several striking implications. First, the data are strongly inconsistent with the $\Lambda=0$, flat universe model (indicated with a circle) that has been the theoretically favored cosmology. If the simplest inflationary theories are correct and the universe is spatially flat, then the supernova data imply that there is a significant, positive cosmological constant. Thus the universe may be flat or there may be little or no cosmological constant, but the data are not consistent with both possibilities simultaneously. This is the most unambiguous result of the current data set.

Second, this data set directly addresses the age of the universe relative to the Hubble time, H_0^{-1} . Figure 9 shows that the Ω_M - Ω_Λ confidence regions are almost parallel to contours of constant age. For any value of the Hubble constant less than $H_0=70~{\rm km~s^{-1}~Mpc^{-1}}$, the implied age of the universe is greater than 13 Gyr, allowing enough time for the oldest stars in globular clusters to evolve (Chaboyer et al. 1998; Gratton et al. 1997). Integrating over Ω_M and Ω_Λ , the best-fit value of the age in Hubble-time units is $H_0\,t_0=0.93^{+0.06}_{-0.06}$ or, equivalently, $t_0=14.5^{+1.0}_{-1.1}(0.63/h)$ Gyr. The age would be somewhat larger in a flat universe: $H_0\,t_0^{11}=0.96^{+0.09}_{-0.07}$ or, equivalently, $t_0^{11}=14.9^{+1.4}_{-1.1}(0.63/h)$ Gyr.

Third, even if the universe is not flat, the confidence regions of Figure 7 suggest that the cosmological constant is a significant constituent of the energy density of the universe. The best-fit model (the center of the shaded contours) indicates that the energy density in the cosmological constant is ~ 0.5 more than that in the form of mass energy density. All of the alternative fits listed in Table 3 indicate a positive cosmological constant with confidence levels of order 99%, even with the systematic uncertainty included in the fit or with a clumped-matter metric.

Given the potentially revolutionary nature of this third conclusion, it is important to reexamine the evidence carefully to find possible loopholes. None of the identified

TABLE 4 Summary of Uncertainties and Cross-Checks

A. CALCULATED IDENTIFIED UNCERTAINTIES

| Source of Uncertainty | Uncertainty on $(\Omega_M^{\text{flat}}, \Omega_\Lambda^{\text{flat}}) = (0.28, 0.72)^a$ |
|---|--|
| Statistical uncertainties (see § 5): | |
| High-redshift supernovae | 0.05 |
| Low-redshift supernovae | 0.065 |
| Total | 0.085 |
| Systematic uncertainties from identified entities/processes: | |
| Dust that reddens, i.e., $\Re_{B}(z = 0.5) < 2\Re_{B}(z = 0)$ (see § 4.1.2) | < 0.03 |
| Malmquist bias difference (see § 4.2) | < 0.04 |
| K-correction uncertainty (see §§ 2 and 3) including zero points | < 0.025 |
| Evolution of average SN Ia progenitor metallicity | < 0.01 |
| affecting rest-frame B spectral features (see § 4.4) | |
| Total | 0.05 |

B. Uncertainties Not Calculated

| Proposed/Theoretical Sources of Systematic Uncertainties | Bounds and Tests (see text) |
|--|--|
| Evolving gray dust, i.e., $\mathcal{R}_B(z=0.5) < 2\mathcal{R}_B(z=0)$ (see §§ 4.4 and 4.1.3) Clumpy gray dust (see § 5) | Test with ≥3-filter color measurements Would increase SN mag residual dispersion with z Test that spectra match on appropriate date for all z Compare low- and high-redshift light-curve rise-times, and light-curve timescales before and after maximum. Test width-luminosity relation for low-redshift supernovae across wide range of environments. Compare low- and high-redshift subsets from ellipticals/spirals, cores/outskirts, etc. |

C. Cross Checks

| Sensitivity to (see § 4.5) | $\Delta_{\Omega_{M,\Lambda}^{ m flat}} =$ |
|---|---|
| Width-luminosity relation | < 0.03 |
| Non-SN Ia contamination | < 0.05 |
| Galactic extinction model | < 0.04 |
| Gravitational lensing by clumped mass (see § 4.3) | < 0.06 |

^a For the redshift distribution of supernovae in this work, uncertainties in $\Omega_{M,\Lambda}^{flat}$ correspond approximately to a factor of 1.3 times uncertainties in the relative supernova magnitudes. For ease of comparisons, this table does not distinguish the small differences between the positive and negative error bars; see Table 3 for these.

sources of statistical and systematic uncertainty described in the previous sections could account for the data in a $\Lambda = 0$ universe. If the universe does in fact have zero cosmological constant, then some additional physical effect or "conspiracy" of statistical effects must be operative—and must make the high-redshift supernovae appear almost 0.15 mag (~15% in flux) fainter than the low-redshift supernovae. At this stage in the study of SNe Ia, we consider this unlikely but not impossible. For example, as mentioned above, some carefully constructed smooth distribution of large-grain-sized gray dust that evolves similarly for elliptical and spiral galaxies could evade our current tests. Also, the full data set of well-studied SNe Ia is still relatively small, particularly at low redshifts, and we would like to see a more extensive study of SNe Ia in many different hostgalaxy environments before we consider all plausible loopholes (including those listed in Table 4B) to be closed.

Many of these residual concerns about the measurement can be addressed with new studies of low-redshift supernovae. Larger samples of well-studied low-redshift supernovae will permit detailed analyses of statistically significant SN Ia subsamples in differing host environments. For example, the width-luminosity relation can be checked and compared for supernovae in elliptical host galaxies, in

the cores of spiral galaxies, and in the outskirts of spiral galaxies. This comparison can mimic the effects of finding high-redshift supernovae with a range of progenitor ages, metallicities, and so on. So far, the results of such studies with small statistics has not shown any difference in width-luminosity relation for this range of environments. These empirical tests of the SNe Ia can also be complemented by better theoretical models. As the data sets improve, we can expect to learn more about the physics of SN Ia explosions and their dependence on the progenitor environment, strengthening the confidence in the empirical calibrations. Finally, new, well-controlled, digital searches for SNe Ia at low redshift will also be able to further reduce the uncertainties due to systematics such as Malmquist bias.

6.1. Comparison with Previous Results

A comparison with the first supernova measurement of the cosmological parameters in P97 highlights an important aspect of the current measurement. As discussed in § 3, the P97 measurement was strongly skewed by SN 1994H, one of the two supernovae that are clear statistical outliers from the current 42 supernova distribution. If SN 1994H had not been included in the P97 sample, then the cosmological measurements would have agreed within the 1 σ

^b The comparison of low- and high-redshift light-curve rise times discussed in § 4.4 theoretically limits evolutionary changes in the zero-point of the light-curve width-luminosity relation to less than ~ 0.1 mag, i.e., $\Delta_{\Omega_{M,\Delta}^{\text{flat}}} \lesssim 0.13$.

error bars with the current result. (The small changes in the K-corrections discussed in § 2 are not a significant factor in arriving at this agreement.) With the small P97 sample size of seven supernovae (only five of which were used in the P97 width-corrected analysis) and somewhat larger measurement uncertainties, it was not possible to distinguish SN 1994H as the statistical outlier. It is only with the much larger current sample size that it is easy to distinguish such outliers on a graph such as Figure 2c.

The fact that there are any outliers at all raises one cautionary flag for the current measurement. Although neither of the current two outliers is a clearly aberrant SN Ia (one has no SN Ia spectral confirmation, and the other has a relatively poor constraint on host-galaxy extinction), we are watching carefully for such aberrant events in future lowand high-redshift data sets. Ideally, the one-parameter width-luminosity relationship for SNe Ia would completely account for every single well-studied SN Ia event. This is not a requirement for a robust measurement, but any exceptions that are discovered would provide an indicator of as-yet-undetected parameters within the main SN Ia distribution.

Our first presentation of the cosmological parameter measurement (Perlmutter et al. 1997f), based on 40 of the current 42 high-redshift supernovae, found the same basic results as the current analysis: A flat universe was shown to require a cosmological constant, and only a small region of low-mass-density parameter space with all the systematic uncertainty included could allow for $\Lambda=0$. (Fit M of Figure 5f still shows almost the same confidence region, with the same analysis approach.) The current confidence region of Figure 7 has changed very little from the corresponding confidence region of Perlmutter et al. (1997f), but since most of the uncertainties in the low-redshift data set are now included in the statistical error, the remaining systematic error is now a small part of the error budget.

The more recent analyses of 16 high-redshift supernovae by Riess et al. (1998) also show a very similar Ω_M - Ω_{Λ} confidence region. The best fits for mass density in a flat universe are $\Omega_M^{\rm flat} = 0.28 \pm 0.10$ or $\Omega_M^{\rm flat} = 0.16 \pm 0.09$ for the two alternative analyses of their nine independent, wellobserved, spectroscopically confirmed supernovae. The best fits for the age of the universe for these analyses are $H_0 t_0 = 0.90^{+0.07}_{-0.05}$ and $H_0 t_0 = 0.98^{+0.07}_{-0.05}$. To first order, the Reiss et al. result provides an important independent cross-check for all three conclusions discussed above, since it was based on a separate high-redshift supernova search and analysis chain (see Schmidt et al. 1998). One caveat, however, is that their Ω_M - Ω_Λ confidence region result cannot be directly compared to ours to check for independent consistency, because the low-redshift supernova data sets are not independent: a large fraction of these supernovae with the highest weight in both analyses are from the Calán/Tololo Supernova Survey (which provided many well-measured supernovae that were far enough into the Hubble flow so that their peculiar velocities added negligible redshiftuncertainty). Moreover, two of the 16 high-redshift supernovae included in the Reiss et al. confidence-region analyses were from our sample of 42 Supernova Cosmology Project supernovae; Riess et al. included them with an alternative analysis technique applied to a subset of our photometry results. (In particular, their result uses the highest redshift supernova from our 42 supernova sample, which has strong weight in our analysis due to the excellent HST photometry.) Finally, although the analysis techniques are mostly

independent, the K-corrections are based on the same approach (Nugent et al. 1998) discussed above.

6.2. Comparison with Complementary Constraints on Ω_M and Ω_Λ

Significant progress is being made in the measurement of the cosmological parameters using complementary techniques that are sensitive to different linear combinations of Ω_M and Ω_{Λ} , and have different potential systematics or model dependencies. Dynamical methods, for example, are particularly sensitive to Ω_M , since Ω_{Λ} affects dynamics only weakly. Since there is evidence that dynamical estimates of Ω_{M} depend on scale, the most appropriate measures to compare with our result are those obtained on large scales. From the abundance—indeed, the mere existence—of rich clusters at high redshift, Bahcall & Fan (1998) find $\Omega_M =$ $0.2^{+0.3}_{-0.1}$ (95% confidence). The Canadian Network for Observational Cosmology collaboration (Carlberg et al. 1996; Carlberg et al. 1998) applies evolution-corrected mass-to-light ratios determined from virial mass estimates of X-ray clusters to the luminosity density of the universe and finds $\Omega_M = 0.17 \pm 0.07$ for $\Omega_{\Lambda} = 0$ (~90% confidence), with small changes in these results for different values of Ω_{Λ} (cf. Carlberg 1997). Detailed studies of the peculiar velocities of galaxies (e.g., Willick et al. 1997; Willick & Strauss 1998; Riess et al. 1997b; but see Sigad et al. 1998) are now giving estimates of $\beta = \Omega_M^{0.6}/b_{IRAS} \approx 0.45 \pm 0.11$ (95% confidence), where b is the ratio of density contrast in galaxies compared to that in all matter. Under the simplest assumption of no large-scale biasing for IRAS galaxies, b=1, these results give $\Omega_{M}\approx 0.26\pm 0.11$ (95% confidence), in agreement with the other dynamical estimates—and with our supernova results for a flat cosmology.

A form of the angular-size distance cosmological test has been developed in a series of papers (see Guerra & Daly 1998 and references therein) and implemented for a sample of 14 radio galaxies by Daly, Guerra, & Wan (1998). The method uses the mean observed separation of the radio lobes compared to a canonical maximum lobe size—calculated from the inferred magnetic field strength, lobe propagation velocity, and lobe width—as a calibrated standard ruler. The confidence region in the $\Omega_{\rm M}$ - Ω_{Λ} plane shown in Daly et al. (1998) is in broad agreement with the SN Ia results we report; they find $\Omega_{\rm M}=0.2^{+0.3}_{-0.2}$ (68% confidence) for a flat cosmology.

Quasi-stellar-object gravitational lensing statistics are dependent on both volume and relative distances and thus are more sensitive to Ω_{Λ} . Using gravitational lensing statistics, Kochanek (1996) finds $\Omega_{\Lambda} < 0.66$ (at 95% confidence for $\Omega_{\rm M}+\Omega_{\Lambda}=1)$ and $\Omega_{\rm M}>0.15.$ Falco, Kochanek, & Munoz (1998) obtained further information on the redshift distribution of radio sources, which allows calculation of the absolute lensing probability for both optical and radio lenses. Formally, their 90% confidence levels in the Ω_M - Ω_{Λ} plane have no overlap with those we report here. However, as Falco et al. (1998) discuss, these results do depend on the choice of galaxy subtype luminosity functions in the lens models. Chiba & Yoshii (1999) emphasized this point, reporting an analysis with E/S0 luminosity functions that yielded a best-fit mass density in a flat cosmology of Ω_M^{flat} = $0.3^{+0.2}_{-0.1}$, in agreement with our SN Ia results.

¹⁴ This is an error-weighted mean of Willick et al. (1997) and Riess et al. (1997b), with optical results converted to equivalent *IRAS* results using $b_{\rm Opt}/b_{IRAS}=1.20\pm0.05$ from Oliver et al. (1996).

Several papers have emphasized that upcoming balloon and satellite studies of the cosmic background radiation (CBR) should provide a good measurement of the sum of the energy densities, $\Omega_M + \Omega_\Lambda$, and thus provide almost orthogonal information to the supernova measurements (White 1998; Tegmark et al. 1999). In particular, the position of the first acoustic peak in the CBR power spectrum is sensitive to this combination of the cosmological parameters. The current results, while not conclusive, are already somewhat inconsistent with overclosed $(\Omega_M + \Omega_\Lambda \gg 1)$ cosmologies and "near-empty" $(\Omega_M + \Omega_\Lambda \lesssim 0.4)$ cosmologies and may exclude the upper right and lower left regions of Figure 7 (see, e.g., Lineweaver 1998; Efstathiou et al. 1998).

6.3. Cosmological Implications

If in fact the universe has a dominant energy contribution from a cosmological constant, there are two coincidences that must be addressed in future cosmological theories. First, a cosmological constant in the range shown in Figure 7 corresponds to a very small energy density relative to the vacuum—energy-density scale of particle physics energy zero points (see Carroll, Press, & Turner 1992 for a discussion of this point). Previously, this had been seen as an argument for a zero cosmological constant, since presumably some symmetry of the particle physics model is causing cancellations of this vacuum energy density. Now it would be necessary to explain how this value comes to be so small, yet nonzero.

Second, there is the coincidence that the cosmological constant value is comparable to the current mass-energy density. As the universe expands, the matter energy density falls as the third power of the scale, while the cosmological constant remains unchanged. One therefore would require initial conditions in which the ratio of densities is a special, infinitesimal value of order 10^{-100} in order for the two densities to coincide today. [The cross-over between mass-dominated and Λ -dominated energy density occurred at $z \approx 0.37$ for a flat $\Omega_M \approx 0.28$ universe, whereas the cross-over between deceleration and acceleration occurred when $(1+z)^3\Omega_M/2=\Omega_\Lambda$, that is at $z\approx 0.73$. This was approximately when SN 1997G exploded, over 6×10^9 yr ago.]

It has been suggested that these cosmological coincidences could be explained if the magnitude-redshift relation we find for SNe Ia is due not to a cosmological constant, but rather to a different, previously unknown physical entity that contributes to the universe's total energy density (see, e.g., Steinhardt 1996; Turner & White 1997; Caldwell, Dave, & Steinhardt 1998). Such an entity can lead to a different expansion history than the cosmological constant does, because it can have a different relation ("equation of state") between its density ρ and pressure p than that of the cosmological constant, $p_{\Lambda}/\rho_{\Lambda}=-1$. We can obtain constraints on this equation-of-state ratio, $w \equiv p/\rho$, and check for consistency with alternative theories (including the cosmological constant with w = -1) by fitting the alternative expansion histories to data; White (1998) has discussed such constraints from earlier supernova and CBR results. In Figure 10, we update these constraints for our current supernova data set for the simplest case of a flat universe and an equation of state that does not vary in time (see Garnavich et al. 1998b for comparison with their high-redshift supernova data set and Aldering et al. 1998 for time-varying equations of state fitted to our data set). In this simple case, a cosmological-constant equation of state can fit our data if the mass density is in the range $0.2 \lesssim \Omega_M \lesssim 0.4$. However, all the cosmological models shown in Figure 10 still require that the initial conditions for the new energy density be tuned with extreme precision to reach their current-day values. Zlatev, Wang, & Steinhardt (1999) have shown that some theories with timevarying w naturally channel the new energy density term to "track" the matter term as the universe expands, leading—without coincidences—to values of an effective vacuum energy density today that are comparable to the mass energy density. These models require $w \gtrsim -0.8$ at all times up to the present for $\Omega_M \geq 0.2$. The supernova data set presented here and future complementary data sets will allow us to explore these possibilities.

The observations described in this paper were primarily obtained as visiting/guest astronomers at the CTIO 4 m telescope, operated by the National Optical Astronomy Observatory under contract to the NSF; the Keck I and II 10 m telescopes of the California Association for Research in Astronomy; the WIYN telescope; the ESO 3.6 m telescope; the INT and WHT, operated by the Royal Greenwich Observatory at the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofisica de Canarias; the HST; and the Nordic Optical 2.5 m telescope. We thank the dedicated staffs of these observatories for their excellent assistance in pursuit of this project. In particular, Dianne Harmer, Paul Smith, and Daryl Willmarth were extraordinarily helpful as the WIYN queue observers. We thank Gary Bernstein and Tony Tyson for developing and supporting the Big Throughput Camera at the CTIO 4 m; this wide-field camera was important in the discovery of many of the high-redshift supernovae. David Schlegel, Doug Finkbeiner, and Marc Davis provided early access to and helpful discussions concerning their models of Galactic extinction. Megan Donahue contributed serendipitous HST observations of SN 1996cl. We thank Daniel Holz and Peter Höflich for helpful discussions. The larger computations described in this paper were performed at the U.S. Department of Energy's National Energy Research Science Computing Center. This work was supported in part by the

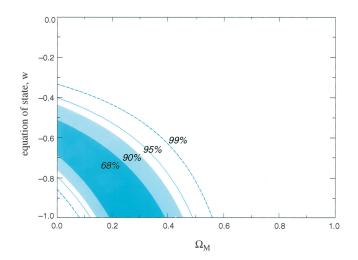


Fig. 10.—Best-fit 68%, 90%, 95%, and 99% confidence regions in the Ω_M w plane for an additional energy density component, Ω_w , characterized by an equation of state $w=p/\rho$. (If this energy density component is Einstein's cosmological constant, Λ , then the equation of state is $w=p_\Lambda/\rho_\Lambda=-1$.) The fit is for the supernova subset of our primary analysis, fit C, constrained to a flat cosmology ($\Omega_M+\Omega_w=1$). The two variables \mathcal{M}_B and α are included in the fit and then integrated over to obtain the two-dimensional probability distribution shown.

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APPENDIX

EXTINCTION CORRECTION USING A BAYESIAN PRIOR

Bayes's theorem provides a means of estimating the a posteriori probability distribution, $P(A \mid A_m)$, of a variable A given a measurement of its value, A_m , along with a priori information, P(A), about what values are likely:

$$P(A \mid A_m) = \frac{P(A_m \mid A)P(A)}{\int P(A_m \mid A)P(A)dA}.$$
 (A1)

In practice P(A) often is not well known but must be estimated from sketchy, and possibly biased, data. For our purposes here we wish to distinguish between the true probability distribution, P(A), and its estimated or assumed distribution, often called the Bayesian prior, which we denote as $\mathcal{P}(A)$. RPK96 present a Bayesian method of correcting SNe Ia for host galaxy extinction. For $\mathcal{P}(A)$ they assume a one-sided Gaussian function of extinction, $\mathcal{G}(A)$, with dispersion $\sigma_{\mathcal{G}} = 1$ magnitude:

$$\mathscr{P}(A) = \mathscr{G}(A) \equiv \begin{cases} \sqrt{2/(\pi\sigma_{\mathscr{G}}^2)} e^{-A^2/2\sigma_{\mathscr{G}}^2} & \text{for } A \ge 0 \\ 0 & \text{for } A < 0 \end{cases}, \tag{A2}$$

which reflects the fact that dust can only redden and dim the light from a supernova. The probability distribution of the measured extinction, A_m , is an ordinary Gaussian with dispersion σ_m , i.e., the measurement uncertainty. RPK96 choose the most probable value of $P(A \mid A_m)$ as their best estimate of the extinction for each supernova:

$$\hat{A}_{\mathscr{G}} = \text{mode } [P(A \mid A_m)] = \begin{cases} \frac{A_m \sigma_{\mathscr{G}}^2}{\sigma_{\mathscr{G}}^2 + \sigma_m^2} & \text{for } A_m > 0, \\ 0 & \text{for } A_m \le 0. \end{cases}$$
(A3)

Although this method provides the best estimate of the extinction correction for an individual supernova, provided $\mathcal{P}(A) = P(A)$, once measurement uncertainties are considered, its application to an ensemble of SNe Ia can result in a biased estimate of the ensemble average extinction whether or not $\mathcal{P}(A) = P(A)$. An extreme case that illustrates this point is where the true extinction is zero for all supernovae, i.e., P(A) is a delta function at zero. In this case, a measured value of E(B-V) < 0 (too blue) results in an extinction estimate of $\hat{A}_{\mathscr{G}} = 0$, while a measured value with $E(B-V) \ge 0$ results in an extinction estimate $\hat{A}_{\mathscr{G}} > 0$. The ensemble mean of these extinction estimates will be

$$\langle \hat{A}_{\mathscr{G}} \rangle = \frac{\sigma_m}{\sqrt{2\pi}} \left(\frac{\sigma_{\mathscr{G}}^2}{\sigma_{\mathscr{G}}^2 + \sigma_m^2} \right),$$
 (A4)

rather than 0 as it should be. (This result is changed only slightly if the smaller uncertainties assigned to the least extincted SNe Ia are incorporated into a weighted average.)

The amount of this bias is dependent on the size of the extinction-measurement uncertainties, $\sigma_m = \mathcal{R}_B \sigma_{E(B-V)}$. For our sample of high-redshift supernovae, typical values of this uncertainty are $\sigma_m \sim 0.5$, whereas for the low-redshift supernovae, $\sigma_m \sim 0.07$. Thus, if the true extinction distribution is a delta function at A=0, while the one-sided prior, $\mathcal{G}(A)$, of equation (A2) is used, the bias in $\langle \hat{A}_{\mathcal{G}} \rangle$ is about 0.13 mag in the sense that the high-redshift supernovae would be overcorrected for extinction. Clearly, the exact amount of bias depends on the details of the data set (e.g., color uncertainty and relative weighting), the true distribution P(A), and the choice of prior $\mathcal{P}(A)$. This is a worst-case estimate, since we believe that the true extinction distribution is more likely to have some tail of events with extinction. Indeed, numerical calculations using a one-sided Gaussian for the true distribution, P(A), show that the amount of bias decreases as the Gaussian width increases away from a delta function, crosses zero when P(A) is still much narrower than $\mathcal{P}(A)$, and then increases with opposite sign. One might use the mean of $P(A \mid A_m)$ instead of the mode in equation (A3), since the bias then vanishes if $\mathcal{P}(A) = P(A)$; however, this mean-calculated bias is even more sensitive to $\mathcal{P}(A) \neq P(A)$ than the mode-calculated bias.

We have only used conservative priors (which are somewhat broader than the true distribution, as discussed in § 4.1); however, it is instructive to consider the bias that results for a less conservative choice of prior. For example, an extinction distribution with only half of the supernovae distributed in a one-sided Gaussian and half in a delta function at zero extinction is closer to the simulations given by Hatano et al. (1998). The presence of the delta-function component in this less conservative prior assigns zero extinction to the vast majority of supernovae and thus cannot produce a bias even with different uncertainties at low and high redshift. This will lower the overall bias, but it will also assign zero extinction to many more supernovae than assumed in the prior, in typical cases in which the measurement uncertainty is not significantly smaller than the true extinction distribution. A restrictive prior, i.e., one that is actually narrower than the true distribution, can even lead to a bias in the opposite direction from a conservative prior.

It is clear from Bayes's theorem itself that the correct procedure for determining the maximum-likelihood extinction, \tilde{A} , of an ensemble of supernovae is to first calculate the a posteriori probability distribution for the ensemble:

$$P(A \mid \{A_{m_i}\}) = \frac{P(A) \sum P(A_{m_i} \mid A)}{\int P(A) \sum P(A_{m_i} \mid A) dA},$$
(A5)

and then take the most probable value of $P(A \mid \{A_{m_i}\})$ for \tilde{A} . For the above example of no reddening, this returns the correct value of $\tilde{A} = 0$.

In fitting the cosmological parameters generally one is not quite as interested in the ensemble extinction as in the combined impact of individual extinctions. In this case $P(A | \{A_{m_i}\})$ must be combined with other sources of uncertainty for each supernova in a maximum-likelihood fit, or the use of a Bayesian prior must be abandoned. In the former case a χ^2 fit is no longer appropriate, since the individual $P(A | \{A_{m_i}\})$'s are strongly non-Gaussian. Use of a Gaussian uncertainty for $\hat{A}_{\mathscr{G}}$ based on the second moment of $P(A | \{A_{m_i}\})$ may introduce additional biases.

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REFERENCES
 Aldering, et al. 1999, in preparation
Baade, W. 1938, ApJ, 88, 285
Bahcall, N. A., & Fan, X. 1998, ApJ, 504, 1
Branch, D. 1998, ARA&A, 36, 17
Branch, D., Lacy, C. H., McCall, M. L., Sutherland, P. G., Uomoto, A., Wheeler, J. C., & Wills, B. J. 1983, ApJ, 270, 123
Burstein, D., & Heiles, C. 1982, AJ, 87, 1165
Caldwell, R. R., Dave, R., & Steinhardt, P. J. 1998, Phys. Rev. Lett., 80, 1582
                                                                                                                                                                                       Malmquist, K. G. 1924, Medd. Lund Astron. Obs. Ser. II, 32, 64
                                                                                                                                                                                                       . 1936, Stockholm Obs. Medd., no. 26
                                                                                                                                                                                       Marvin, H., & Perlmutter, S., 1989, IAU Circ. 4727
Meikle, W. P. S., et al. 1996, MNRAS, 281, 263
Mihalas, D., & Binney, J. 1981, Galactic Astronomy: Structure and Kinematics (2d ed.; San Francisco: W.H. Freeman)
                                                                                                                                                                                     Cappellaro, E., Turatto, M., & Fernley, J. 1995, IUE - ULDA Access Guide 6, Supernovae (Noordwijk, The Netherlands: ESA)
Cardelli, J. A., Clayton, G. C., & Mathis, J. S. 1989, ApJ, 345, 245
Carlberg, R. G. 1997, ApJ, submitted (astro-ph/9708054)
Carlberg, R. G., Yee, H. K. C., Ellingson, E., Abraham, R., Gravel, P., Morris, S., & Pritchet, C. J. 1996, ApJ, 462, 32
Carlberg, R. G., et al. 1998, in Proc. 33d Recontres de Moriond, Fundamental Parameters in Cosmology, ed. J. Trân Thanh Vâng & Y. Giraud-Heraud (Paris: Editions frontières). in press
       Heraud (Paris: Editions frontières), in press
  Carroll, S. M., Press, W. H., & Turner, E. L. 1992, ARA&A, 30, 499
Chaboyer, B., DeMarque, P., Kernan, P. J., & Krauss, L. M. 1998, ApJ,
                                                                                                                                                                                                         1995b, IAU Circ. 6270
                                                                                                                                                                                                       . 1996, IAU Circ. 6621
. 1997a, IAU Circ. 6596
       494, 96
  Chiba, M., & Yoshii, Y. 1999, ApJ, 510, 42
                                                                                                                                                                                                       . 1997b, IAU Circ. 6540
 Clayton, G. C., & Cardelli, J. A. 1988, AJ, 96, 695
Colgate, S. 1979, ApJ, 232, 404
Daly, R. A., Guerra, E. J., & Wan, L. 1998, in Proc. 33d Recontres de Moriond, Fundamental Parameters in Cosmology, ed. J. Trân Thanh Vâng & Y. Giraud-Heraud (Paris: Editions frontières), in press
                                                                                                                                                                                                        1997c, IAU Circ. 6646
                                                                                                                                                                                                       . 1997d, IAU Circ. 6804
                                                                                                                                                                                                       . 1997e, ApJ, 483, 565 (P97)
. 1997f, BAAS, 29, 1351 (astroph/9812473)
                                                                                                                                                                                                        1998a, IAU Circ. 6881
 Fistathiou, G., et al. 1998, MNRAS, submitted
Falco, E. E., Kochanek, C. S., & Munoz, J. A. 1998, ApJ, 494, 47
Feldman, G. J., & Cousins, R. D. 1998, Phys. Rev. D, 57, 3873
Filippenko, A. V., et al. 1998, in preparation
Freedman, W. L., Mould, J. R., Kennicut, R. C., & Madore, B. F. 1998, in
IAU Symp. 183, Cosmological Parameters and the Evolution of the
                                                                                                                                                                                                        1998b, Nature, 391, 51; erratum 392, 311
                                                                                                                                                                                       Pettini, M., King, D. L., Smith, L. J., & Hunstead, R. W. 1997, ApJ, 478,
                                                                                                                                                                                       Phillips, M., et al. 1999, in preparation
                                                                                                                                                                                       Phillips, M. M. 1993, ApJ, 413, L105
Phillips, M. M., et al. 1987, PASP, 99, 592
                                                                                                                                                                                      Riess, A., Davis, M. H., & Kirshner, R. P. 1997b, ApJ, 488, L1
Riess, A., Press, W. H., & Kirshner, R. P. 1995, ApJ, 438, L17
———. 1996, ApJ, 473, 88 (RPK96)
Riess, A., et al. 1997a, AJ, 114, 722
       Universe, ed. K. Sato (Dordrecht: Kluwer) (astro-ph/9801080)
 Frieman, J. A. 1996, Comments Astroph, in press (astro-ph/9608068)
Fukugita, M., Hogan, C. J., & Peebles, P. J. E. 1998, ApJ, 503, 518
Garnavich, P., et al. 1998a, ApJ, 493, L53
                    1998b, ApJ, 509, 74
                                                                                                                                                                                                       . 1998, AJ, 116, 1009
 Goldhaber, G., et al. 1997, in Thermonuclear Supernova, ed. P. Ruiz-
Lapuente, R. Canal, & J. Isern (NATO ASI Ser. C, 486) (Dordrecht:
                                                                                                                                                                                       Ruiz-Lapuente, P. 1998, in Proc. Second International Conference on
                                                                                                                                                                                             Dark Matter in Astro and Particle Physics, ed. H. V. Klapdor-
Kleingrothaus & L. Baudis, in press (astro-ph/9810423)
Ruiz-Lapuente, P., Canal, R., & Burkert, A. 1997, in Thermonuclear Supernova, ed. P. Ruiz-Lapuente, R. Canal, & J. Isern (Dordrecht:
       Kluwer), 777
                                                                                                                                                                                            Kluwer), 205
                                                                                                                                                                                       Scha, A., et al. 1997, ApJ, 486, 1
Schlegel, D., Finkbeiner, D., & Davis, M. 1998, ApJ, 500, 525
Schmidt, B. P., et al. 1998, ApJ, 507, 46
Schramm, D. N. 1990, in Astrophysical Ages and Dating Methods, ed.
E. Vangioni-Flam et al. (Gif-sur-Yvette: Edition Frontières), 365
                                                                                                                                                                                       Sigad, Y., Eldar, A., Dekel, A., Strauss, M. A., & Yahil, A. 1998, ApJ, 495, 516
                                                                                                                                                                                      Smail, I., Hogg, D. W., Yan, L., & Cohen, J. G. 1995, ApJ, 449, L106
Steinhardt, P. J. 1996, Nature, 382, 768
Tammann, G. A. 1979, in ESA/ESO Workshop on Astronomical Uses of
the Space Telescope, ed. F. Macchetto, F. Pacini, and M. Tarenghi
                                                                                                                                                                                       (Geneva: ESO), 329
Tegmark, M., et al. 1999, ApJ, submitted (astro-ph/9805117)
Tripp, R. 1998, A&A, 331, 815
Turner, M. S., & White, M. 1997, Phys. Rev. D, 56, R4439
Vacca, W. D. & Leibundgut, B. 1996, ApJ, 471, L37
                                                                                                                                                                                      Turner, M. S., & White, M. 1997, Phys. Rev. D, 56, R4439
Vacca, W. D., & Leibundgut, B. 1996, ApJ, 471, L37
Wambsganss, J., Cen, R., & Ostriker, J. P. 1998, ApJ, 494, 29
Wang, L., Höflich, P., & Wheeler, J. C. 1997, ApJ, 483, L29
White, M. 1998, ApJ, 506, 495
Willick, J. A. 1994, ApJS, 92, 1
Willick, J. A., & Strauss, M. A. 1998, ApJ, 507, 64
Willick, J. A., Strauss, M. A., Dekel, A., & Tsafrir, K. 1997, ApJ, 486, 629
Zlatev, I., Wang, L., & Steinhardt, P. J. 1999, Phys. Rev. Lett., 82, 896
 Maddox, S. J., Sutherland, W. J., Loveday, J., & Peterson, B. A. 1990, MNRAS, 247, 1P
```