

Improved Constraints on Dark Energy From Chandra X-ray Observations of the Largest Relaxed Galaxy Clusters

S.W. Allen et al.

(Measuring Ω_Λ and Ω_m using X-ray Gas Mass Fraction)

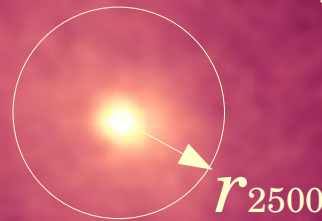
Technique

Overview of how f_{gas} is useful

1) Cluster gas from hot, relaxed clusters, is expected to be fair tracer of matter content of the universe (Baryonic mass fraction).

2) Measuring Gas Mass Fraction, f_{gas} , and using Ω_b , gives Ω_m . f_{gas} is also proportional to distances, and so traces expansion.

3) Measure X-ray surface brightness profiles – gives Temperature and mass profiles and thus f_{gas} profiles.



4) Compare f_{gas} profiles with expected dependence on cosmology. { $f_{\text{gas}}(z)$, and proportionality to Ω_m }

Data Sample

And Technical Details

MACSJ1423.8+2404

- 42 Clusters
- $0.05 < z < 1.1$
- At Chandra Observatory bet. 1999 – 2005
- Morphologically selected the following:
 - Hot: $kT > 5 \text{ keV}$ ($T \sim 5.8 * 10^{10} \text{ K}$)
 - f_{gas} does not depend on temperature for hot systems.
 - Dynamically Relaxed
 - Allows hydrostatic equilibrium assumption
- At Right: A galaxy cluster from data set.



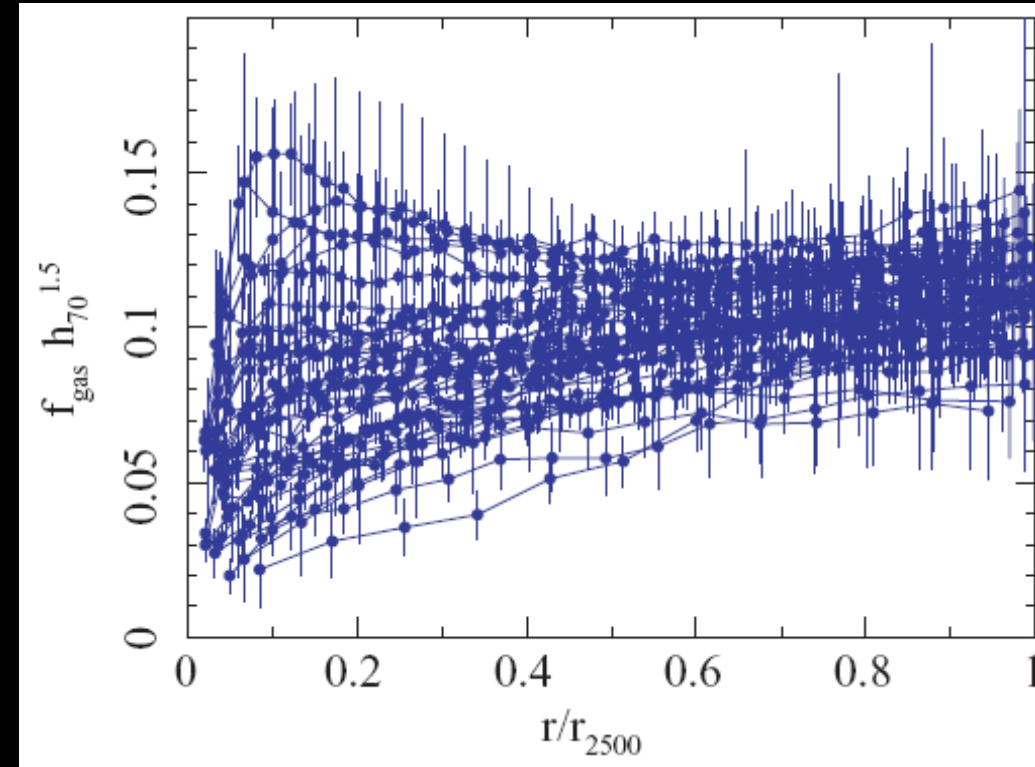
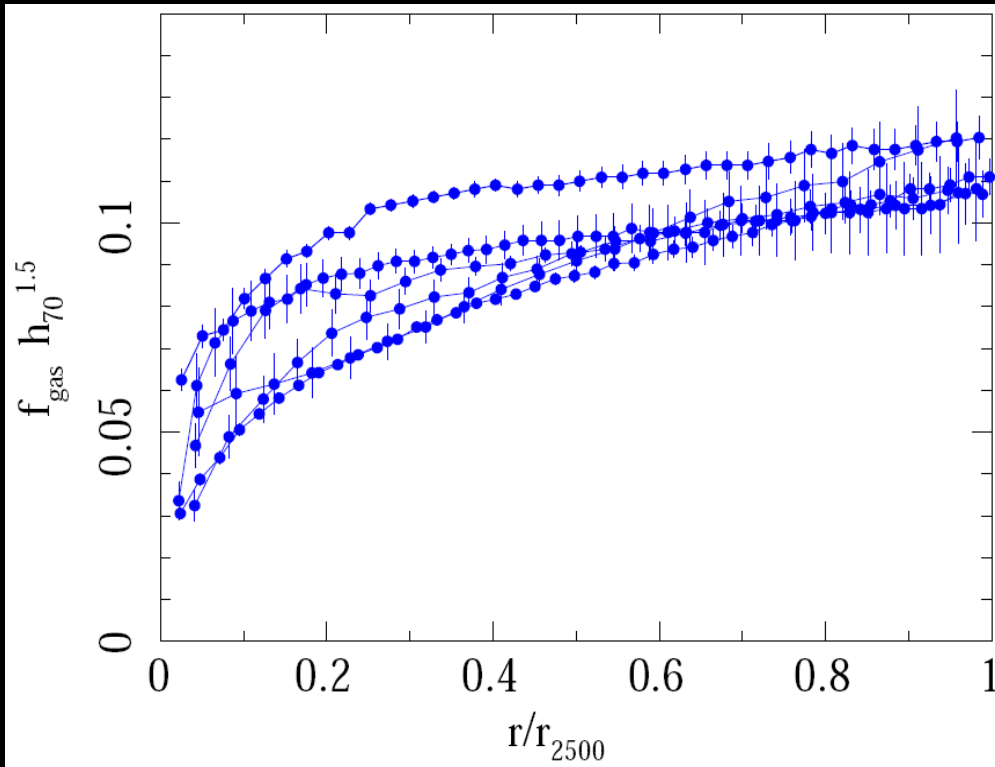
Scale: Image is 2.56 x 1.6 arcmin
(Credit: NAOJ/Subaru/H.Ebeling)

Scale: Image is 2.56 x 1.6 arcmin

(Credit: Optical: NAOJ/Subaru/H. Ebeling; X-Ray: NASA/CXC/ToA/S.Allen et al.)

F_{gas} Measurements

- Don't show measured surface-brightness profiles, or other data.
- But show radial profiles of f_{gas} , obtained from measured surface brightness profiles, and assumed NFW dark matter distribution. (Note convergence at r_{2500})
- Pick value of f_{gas} at r_{2500} (used in $f_{\text{gas}}(z)$ plots)
- Systematic errors up to 15 %



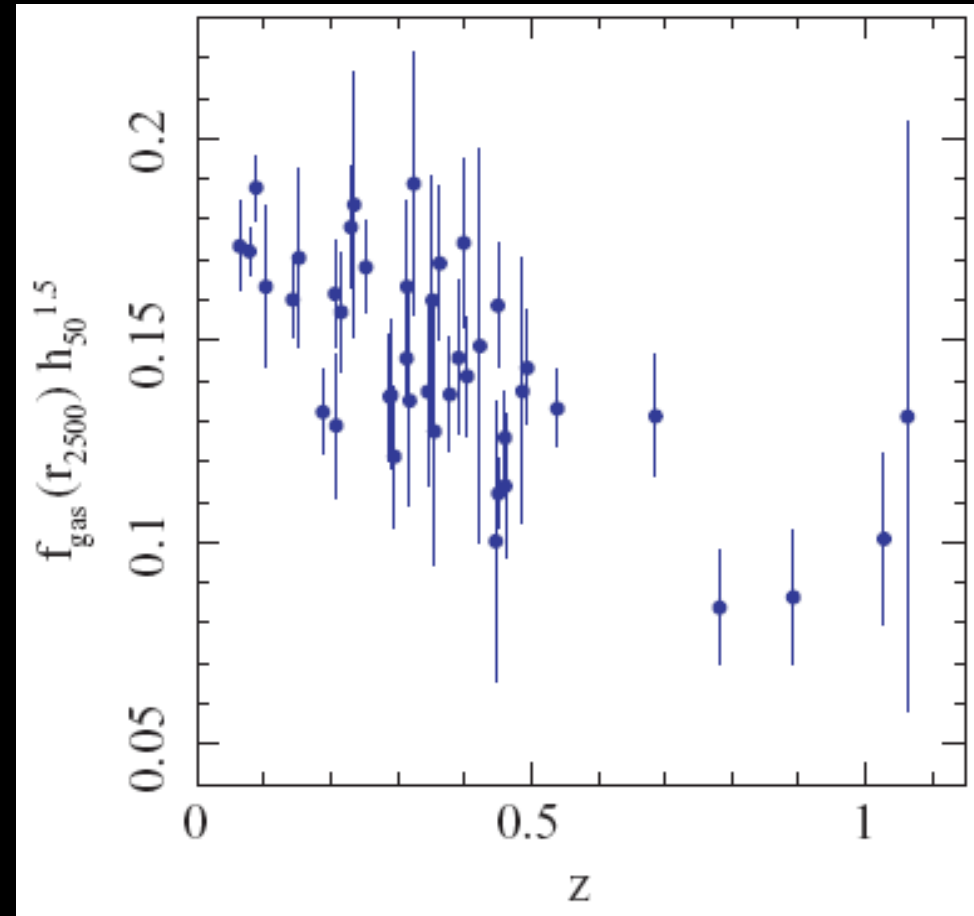
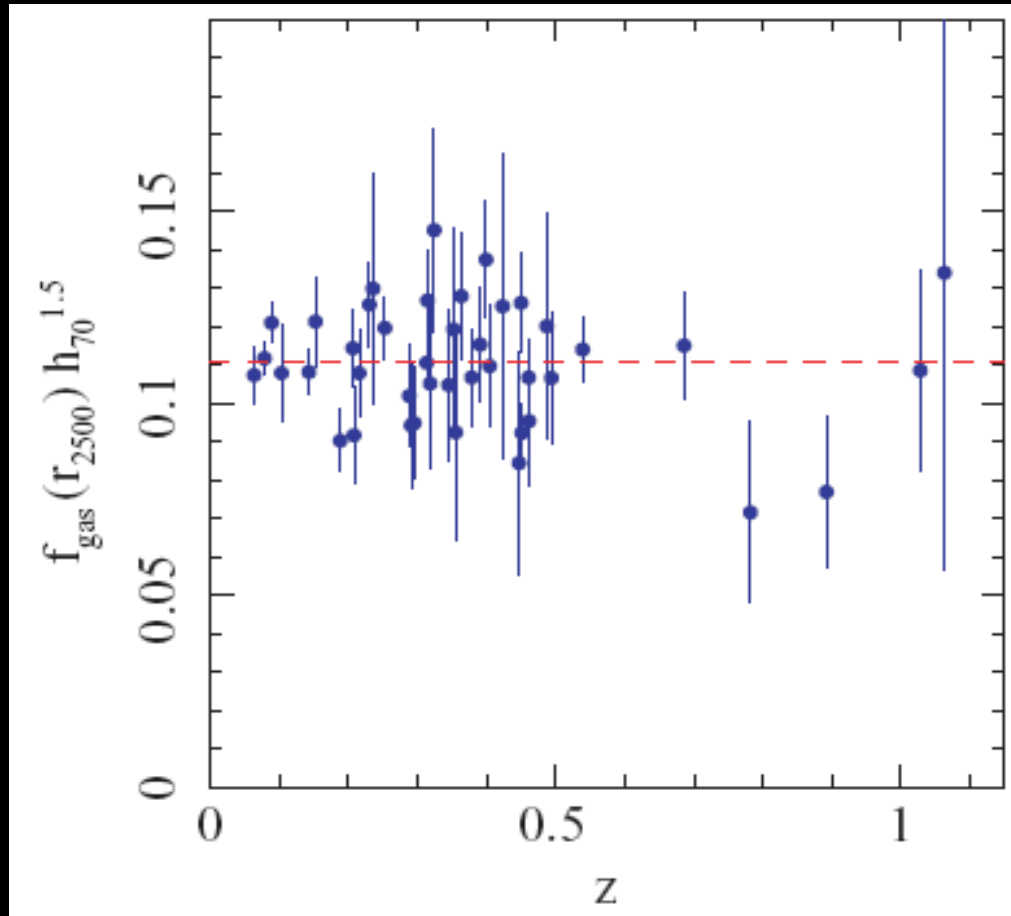
Variation of f_{gas} with redshift

$$f_{\text{gas}}^{\Lambda\text{CDM}}(z) = \frac{K A \gamma b(z)}{1 + s(z)} \left(\frac{\Omega_b}{\Omega_m} \right) \left[\frac{d_A^{\Lambda\text{CDM}}(z)}{d_A(z)} \right]^{1.5}$$

From Hydrodynamic simulations, expect correct cosmology to give no variation of f_{gas} with redshift.

ΛCDM : $\Omega_m = .3, \Omega_\Lambda = 0.7, h = 0.7$

SCDM : $\Omega_m = 1, h = 0.5$



Tested Models of Dark Energy

LCDM: $w = -1$

Other Constant w :
(including $w < -1$)

Evolving w : $w = \frac{w_{et}z + w_0z_t}{z + z_t} = \frac{w_{et}(1 - a)a_t + w_0(1 - a_t)a}{a(1 - 2a_t) + a_t}$

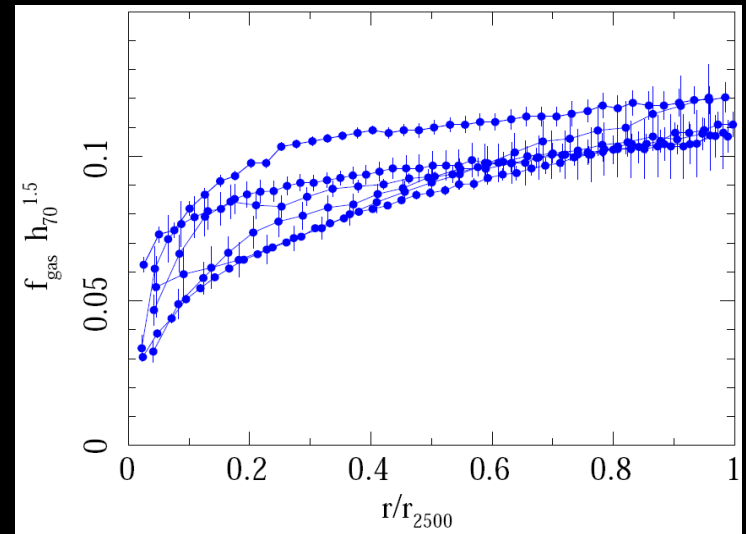
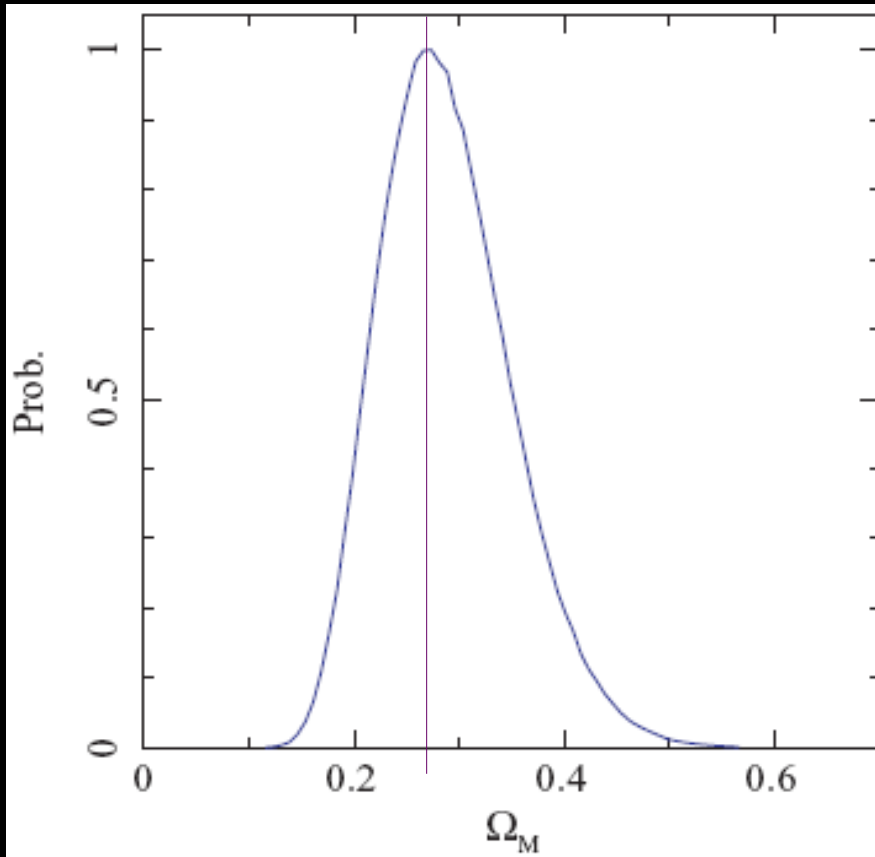
et = early time

o = present time

t = at transition

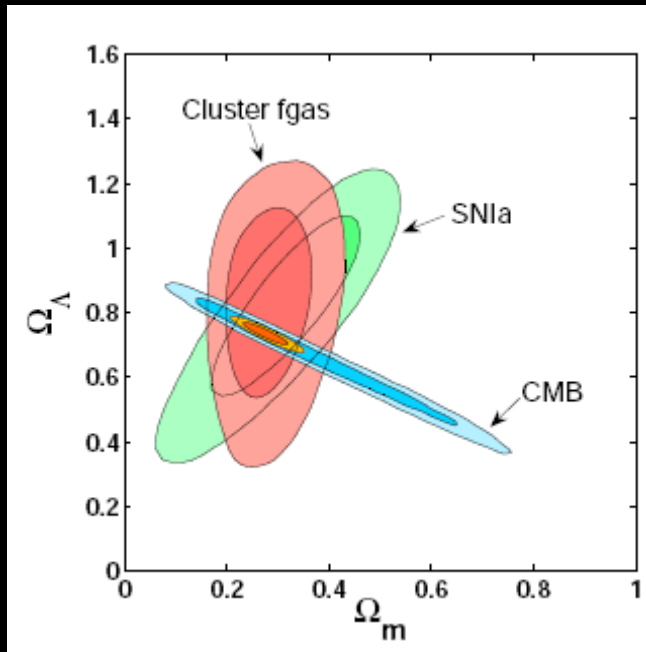
Ω_m Constraint

$\Omega_m = 0.28 \pm 0.06$ (68% Confidence) for Λ CDM



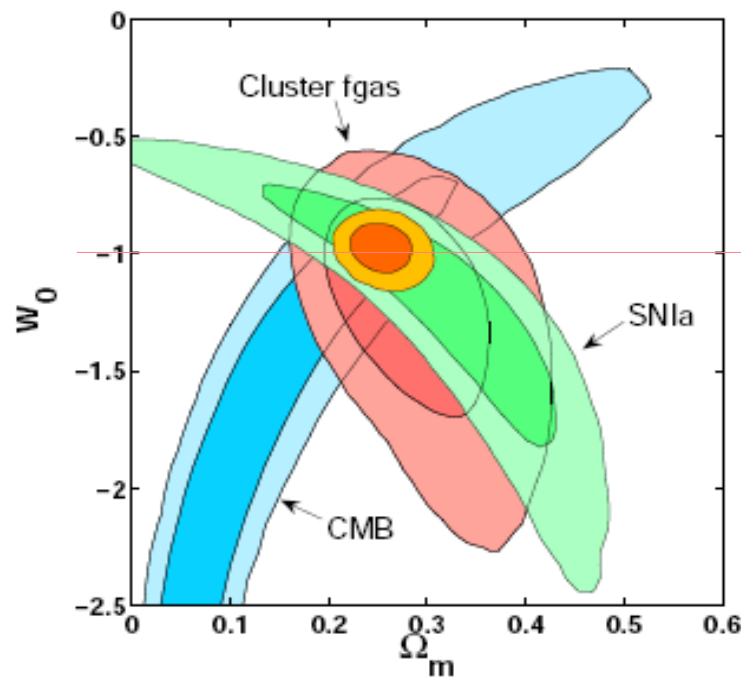
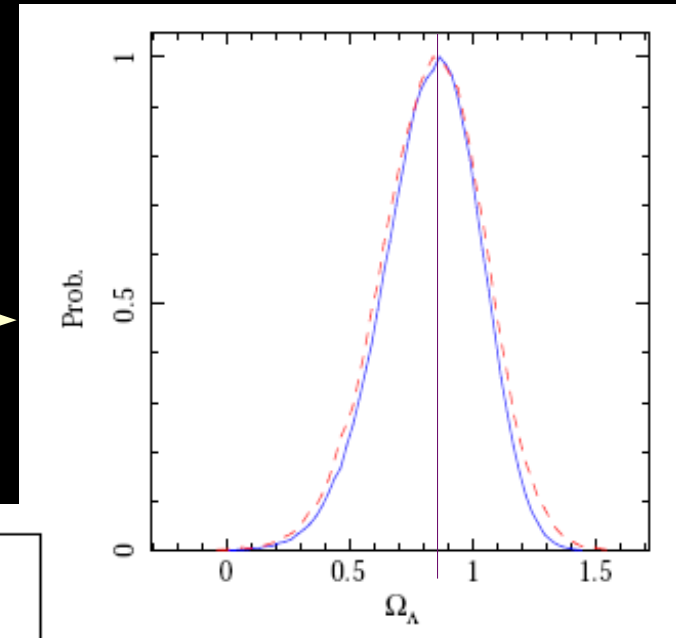
Above analysis done with 6 lowest redshift clusters shown at right. Value in good agreement with value obtained from rest of

Constraints on Lambda-CDM



$$\Omega_\Lambda = 0.86 \pm 0.21$$

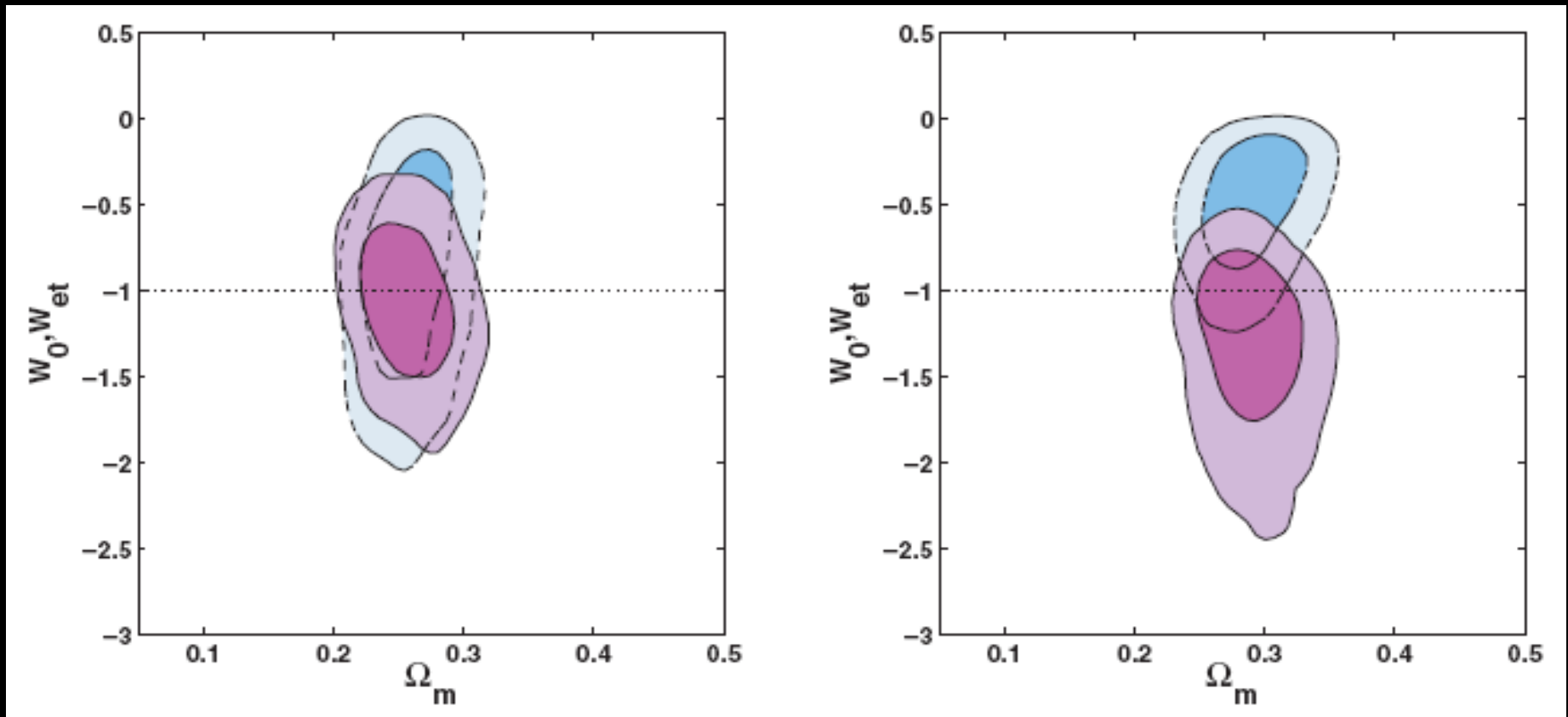
Cited as Dark
Energy Detection



Constraints on w evolution

Davis et al.

Reiss et al.



Consistent with no evolution in w

Constraints: Summary/Uncertainties

Data	Model	$\Omega_b h^2, h$ Priors	COSMOLOGICAL CONSTRAINTS			
			Ω_m	Ω_{DE}	w_0	w_{at}
low- z f_{gas}	Λ CDM ($0 < \Omega_\Lambda < 2.0$)	standard	0.28 ± 0.06	—	—	—
f_{gas}	Λ CDM	standard	0.27 ± 0.06	0.86 ± 0.19	—	—
f_{gas}	Λ CDM	weak	0.27 ± 0.09	0.86 ± 0.21	—	—
$f_{gas} + \text{CMB}$	Λ CDM	none	0.28 ± 0.06	0.73 ± 0.04	—	—
$f_{gas} + \text{CMB} + \text{SNIa}(1)$	Λ CDM	none	0.275 ± 0.033	0.735 ± 0.023	—	—
f_{gas}	constant w (flat)	standard	0.28 ± 0.06	—	$-1.14^{+0.27}_{-0.35}$	—
f_{gas}	constant w (flat)	weak	0.29 ± 0.09	—	$-1.11^{+0.31}_{-0.45}$	—
$f_{gas} + \text{CMB}$	constant w (flat)	none	0.243 ± 0.033	—	-1.00 ± 0.14	—
$f_{gas} + \text{CMB} + \text{SNIa}(1)$	constant w (flat)	none	0.253 ± 0.021	—	-0.98 ± 0.07	—
$f_{gas} + \text{CMB} + \text{SNIa}(1)$	constant w	none	0.310 ± 0.052	—	$-1.08^{+0.13}_{-0.19}$	—
$f_{gas} + \text{CMB} + \text{SNIa}(1)$	evolving w (flat)	none	0.254 ± 0.022	—	$-1.05^{+0.31}_{-0.26}$	$-0.83^{+0.48}_{-0.43}$
$f_{gas} + \text{CMB} + \text{SNIa}(1)$	evolving w	none	$0.29^{+0.09}_{-0.04}$	—	$-1.15^{+0.50}_{-0.38}$	$-0.80^{+0.70}_{-1.30}$
$f_{gas} + \text{CMB} + \text{SNIa}(2)$	evolving w (flat)	none	0.287 ± 0.026	—	$-1.19^{+0.29}_{-0.35}$	$-0.33^{+0.18}_{-0.34}$

10-15 % systematic uncertainty from : x-ray modeling (lots of assumptions), instrument calibration, non-thermal pressure support

Assumptions of spherical symmetry, hydrostatic equilibrium, dark matter profile (NFW), ...

Results comparable with SNIa data according to w_0, Ω_m ellipses.

Five Year WMAP Observations: Cosmological Interpretation

E. Komatsu et. al.

Constraining Dark Energy Models Via Accurately Measured Distances to
Specific Epochs

Distance Priors

2 Distance ratios, associated w/ decoupling epoch, can be measured very precisely by locating peaks and troughs of acoustic oscillations in CMB:

$$D_A(z^*)/r_s(z^*)$$

$$D_A(z^*)/H(z^*)/c$$

$D_A(z^*)$: Proper distance (not comoving) to decoupling epoch

$r_s(z^*)$: Comoving size of the sound horizon at the decoupling epoch.

$H(z^*)/c$: Hubble horizon size at the decoupling epoch

z^* : Defines decoupling epoch

$$l_A \equiv (1 + z_*) \frac{\pi D_A(z_*)}{r_s(z_*)} \quad R(z_*) \equiv \sqrt{\Omega_m H_0^2 (1 + z_*) D_A(z_*)}$$

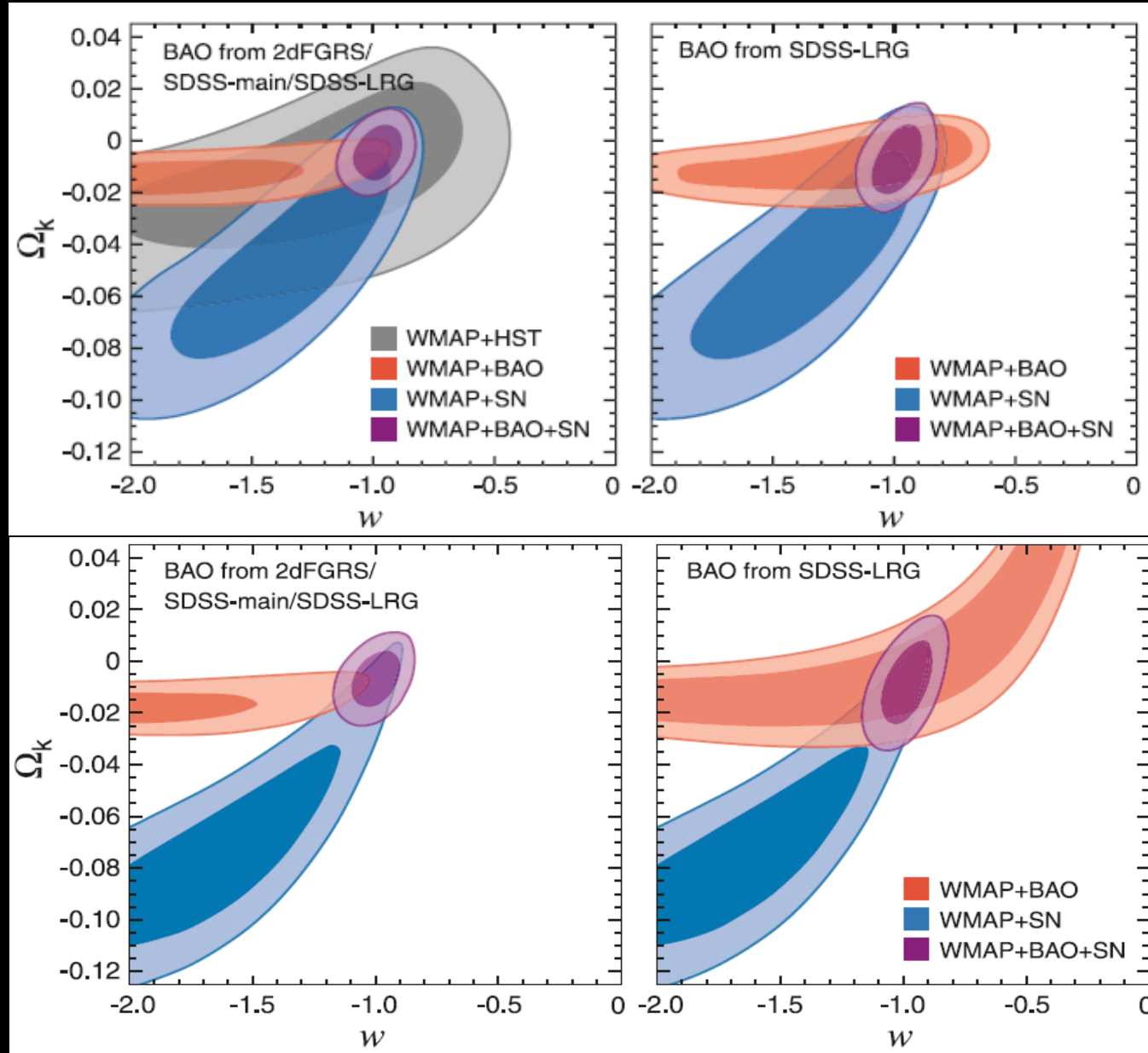
$$z_* = 1048 \left[1 + 0.00124 (\Omega_b h^2)^{-0.738} \right] \left[1 + g_1 (\Omega_m h^2)^{g_2} \right] \quad g_1 = \frac{0.0783 (\Omega_b h^2)^{-0.238}}{1 + 39.5 (\Omega_b h^2)^{0.763}} \quad g_2 = \frac{0.560}{1 + 21.1 (\Omega_b h^2)^{1.81}}$$

Priors alone provide decent results

Major Caveat: Full WMAP
Analysis

Requires
assumption of
cosmology!

Just distance
priors



How to use priors to constrain cosmology

Chi Square!

$$\chi_{WMAP}^2 \equiv -2 \ln L = (x_i - d_i)(C^{-1})_{ij}(x_j - d_j)$$

$$x_i = (l_A, R, z_*)$$

Computed using favorite cosmology (Ω_m, Ω_b, H_0 , etc..)

Minimize Chi Square with respect to H_0, Ω_b, Ω_m , which leaves you with a distribution of $w(a)$ and Ω_k

TABLE 10

WMAP DISTANCE PRIORS OBTAINED FROM THE WMAP 5-YEAR FIT TO MODELS WITH SPATIAL CURVATURE AND DARK ENERGY. THE CORRELATION COEFFICIENTS ARE:
 $r_{l_A, R} = 0.1109$, $r_{l_A, z_*} = 0.4215$, AND
 $r_{R, z_*} = 0.6928$.

	5-year ML ^a	5-year Mean ^b	Error, σ
$l_A(z_*)$	302.10	302.45	0.86
$R(z_*)$	1.710	1.721	0.019
z_* ^e	1090.04	1091.13	0.93

^aMaximum likelihood values (recommended)

^bMean of the likelihood

^cMaximum likelihood values (recommended)

^dMean of the likelihood

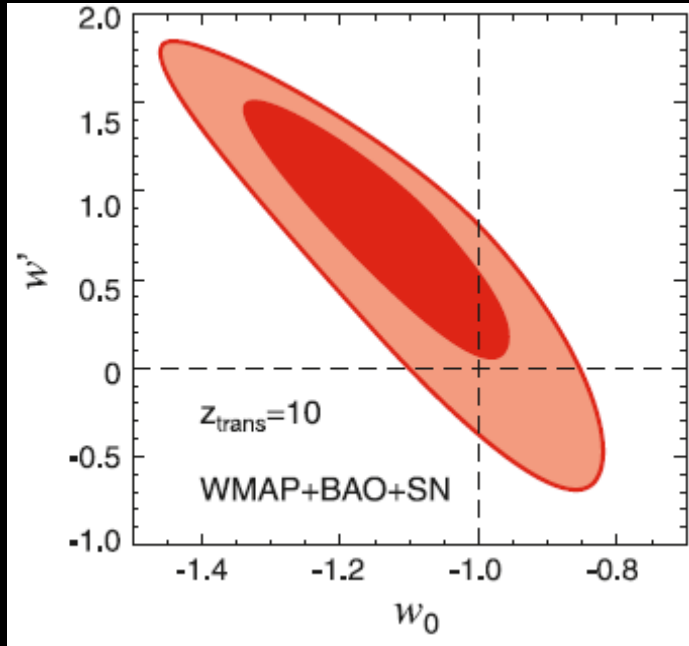
^eEquation (66)

TABLE 11

INVERSE COVARIANCE MATRIX FOR THE WMAP DISTANCE PRIORS

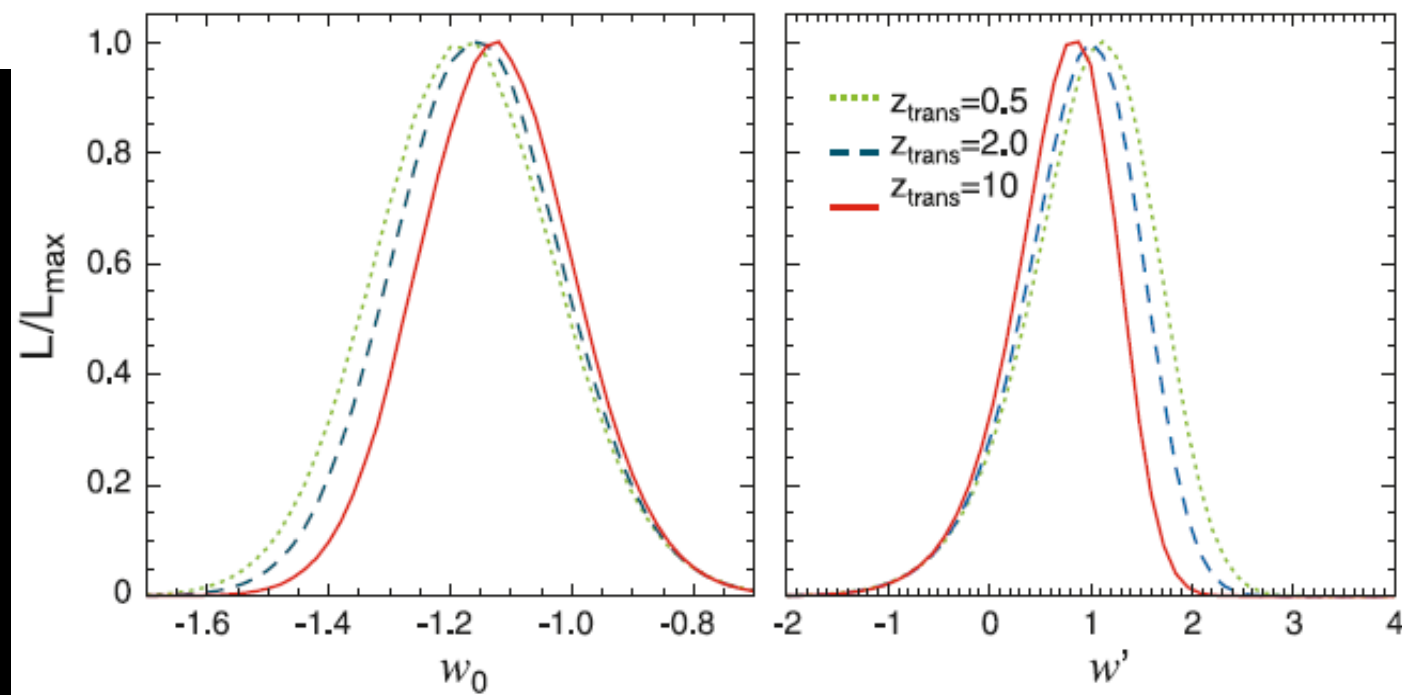
	$l_A(z_*)$	$R(z_*)$	z_*
$l_A(z_*)$	1.800	27.968	-1.103
$R(z_*)$		5667.577	-92.263
z_*			2.923

Measured w Evolution



$$w(a) = \frac{a\tilde{w}(a)}{a + a_{\text{trans}}} - \frac{a_{\text{trans}}}{a + a_{\text{trans}}}$$

$$\tilde{w}(a) = \tilde{w}_0 + (1 - a)\tilde{w}_a.$$



EXTRA SLIDES

Dark Energy equation of state

$$w_{\text{early}} = -1 \text{ and } w_{\text{late}} = w_0 + (1 - a)w_a$$

$$w(a) = \tilde{w}(a)f(a/a_{\text{trans}}) + (-1) [1 - f(a/a_{\text{trans}})]$$

$f(x)$ goes to zero for $x \ll 1$, and to unity for $x \gg 1$

$$w(a) = \frac{a\tilde{w}(a)}{a + a_{\text{trans}}} - \frac{a_{\text{trans}}}{a + a_{\text{trans}}}$$

$$\tilde{w}(a) = \tilde{w}_0 + (1 - a)\tilde{w}_a.$$

Dark Energy Models

Komatsu et al.

