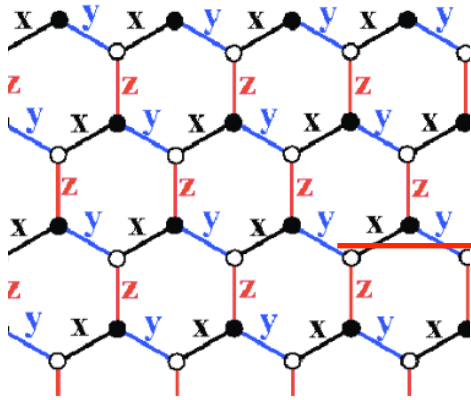
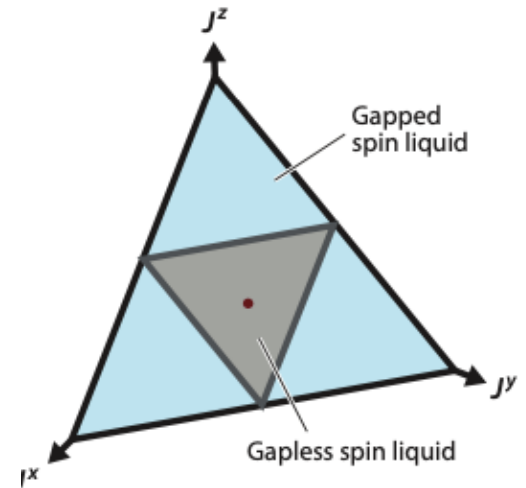


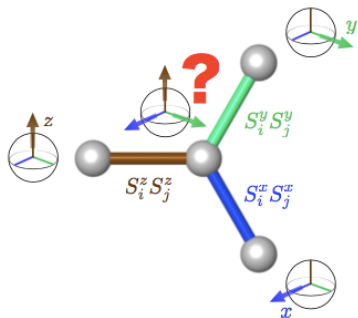
# Kitaev Spin Liquids



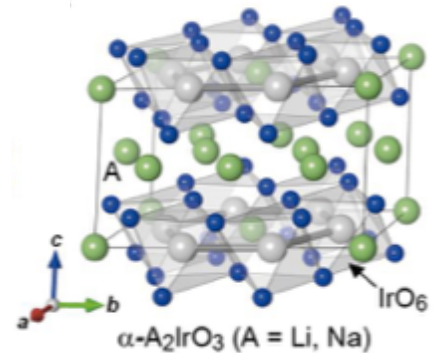
Context  
The Model

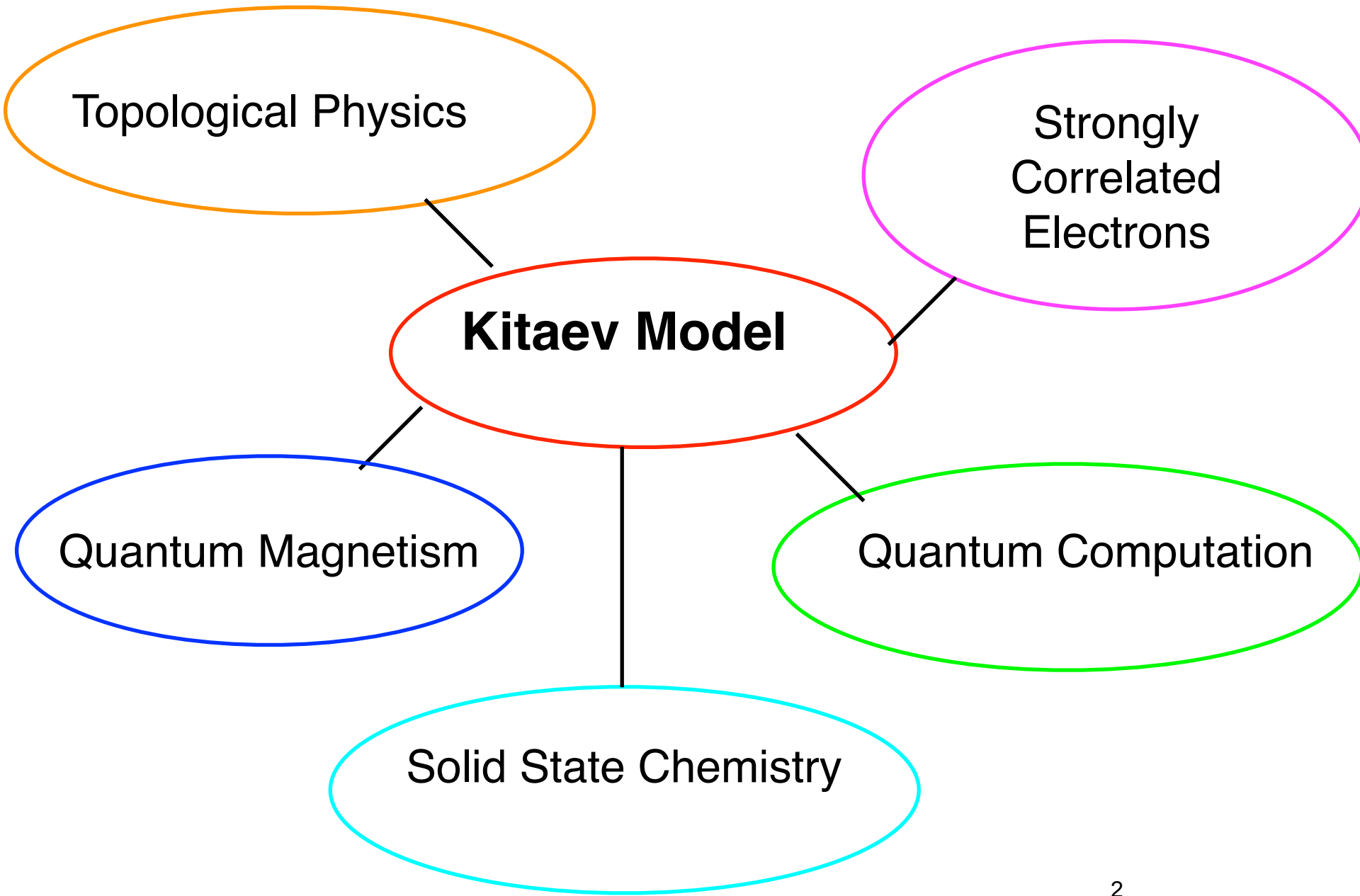


Ying-Ting “Layered Nickelates”  
 Michael “Thin-Film Pyrochlore Iridiates”  
 Skanda “Twisted Bilayer Graphene”

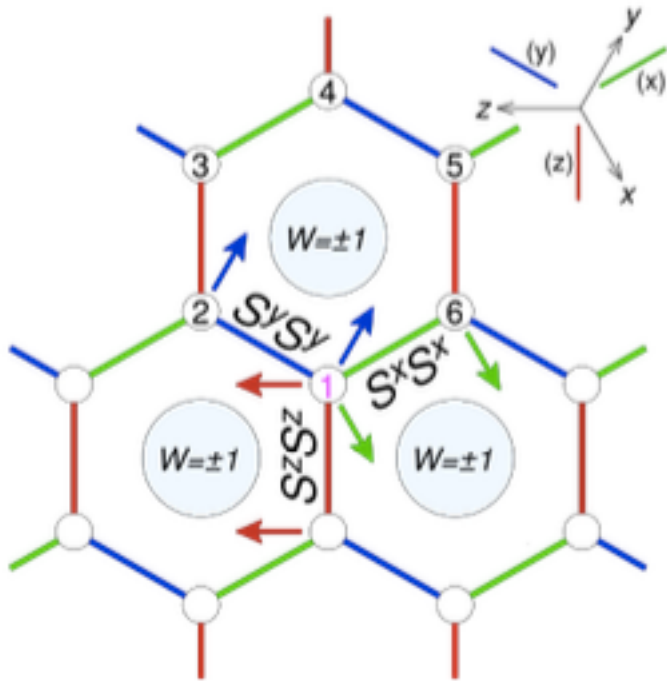


Experimental Realizations





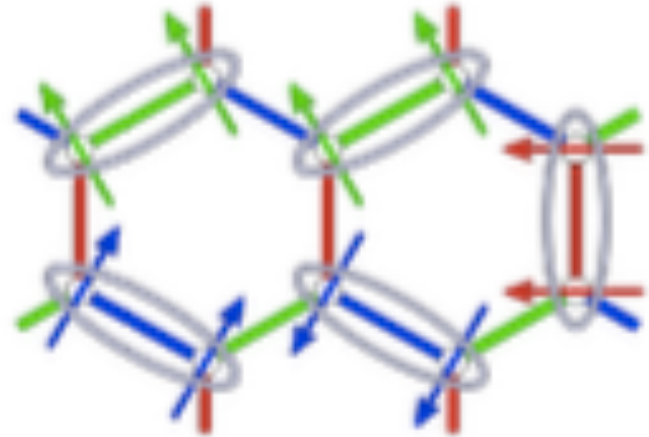
# The Kitaev Model on the Honeycomb Lattice



$$H = - \sum_{\langle ij \rangle_\gamma} K_\gamma S_i^\gamma S_j^\gamma$$

Ising Spins with Bond Anisotropies

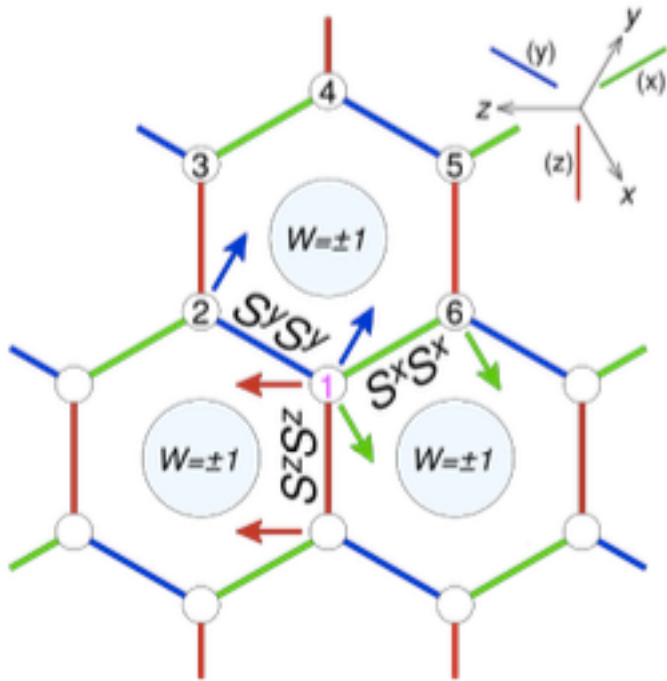
## Classical Model



Two “happy” bonds/plaquette

Classical Model has Extensive Ground State Degeneracy

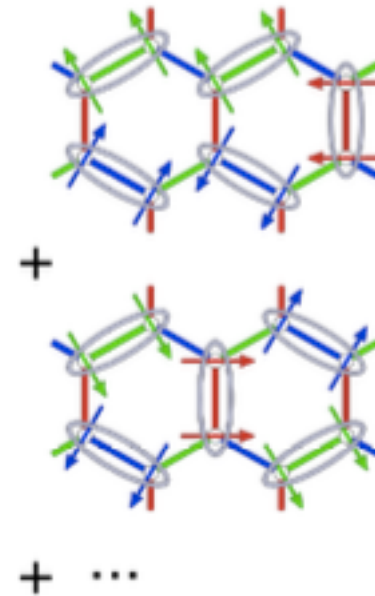
# The Kitaev Model on the Honeycomb Lattice



$$H = - \sum_{\langle ij \rangle_\gamma} K_\gamma S_i^\gamma S_j^\gamma$$

Ising Spins with Bond Anisotropies

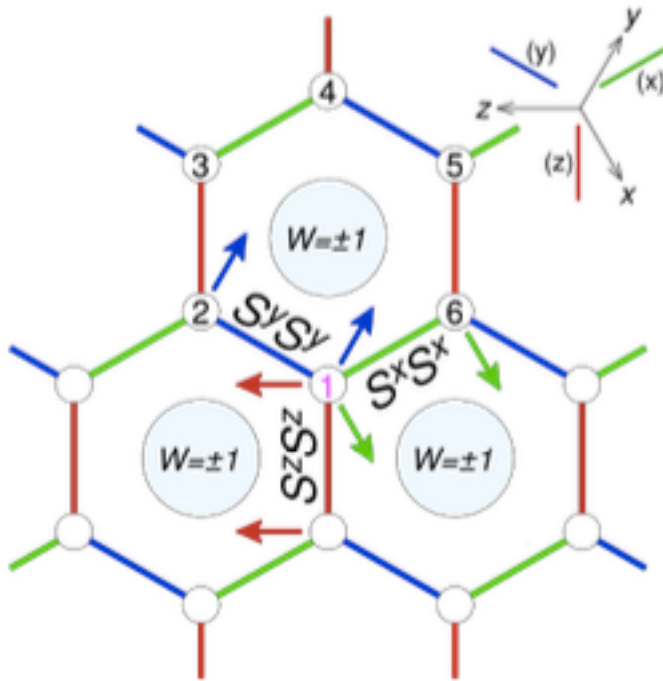
## Quantum Model



Superposition of Classical Configurations (similar to RVB)

Highly Entangled Quantum Spin Liquid State

# The Kitaev Model on the Honeycomb Lattice



$$H = - \sum_{\langle ij \rangle_\gamma} K_\gamma S_i^\gamma S_j^\gamma$$

Ising Spins with Bond Anisotropies

$$W_p = 2^6 S_1^z S_2^x S_3^y S_4^z S_5^x S_6^y$$

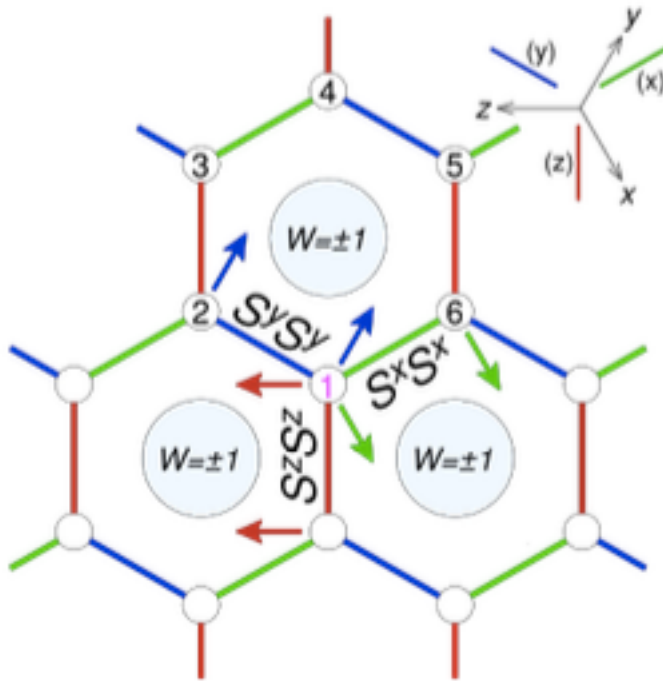
$$S_i^\gamma = \frac{\hbar}{2} \sigma^\gamma$$

$$\sigma^a \sigma^b = \delta_{ab} I + i \epsilon_{abc} \sigma^c$$

$$[\sigma^a, \sigma^b] = 2i \epsilon_{abc} \sigma^c$$

$$[W_p, H] = 0$$

# The Kitaev Model on the Honeycomb Lattice



$$H = - \sum_{\langle ij \rangle_\gamma} K_\gamma S_i^\gamma S_j^\gamma$$

Ising Spins with Bond Anisotropies

$$W_p = 2^6 S_1^z S_2^x S_3^y S_4^z S_5^x S_6^y$$

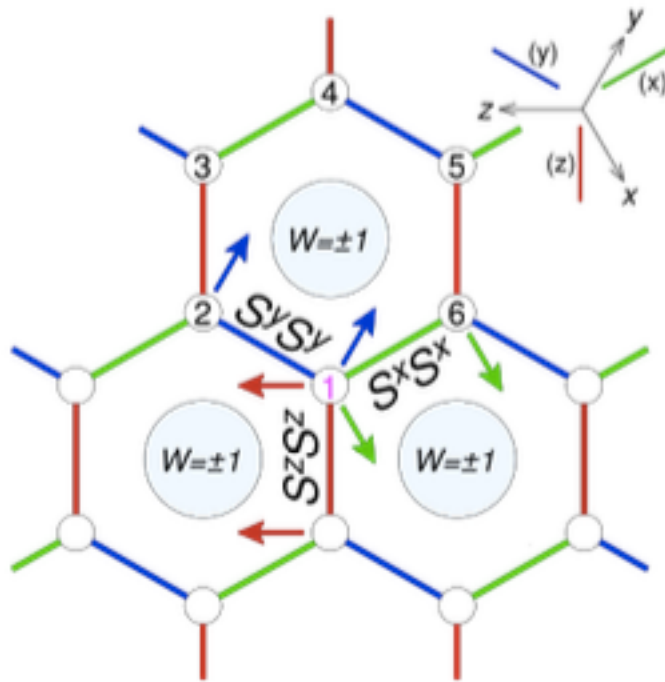
$$[W_p, H] = 0$$

Infinitely Many Conserved  
Quantities

$$W_p = \pm 1$$

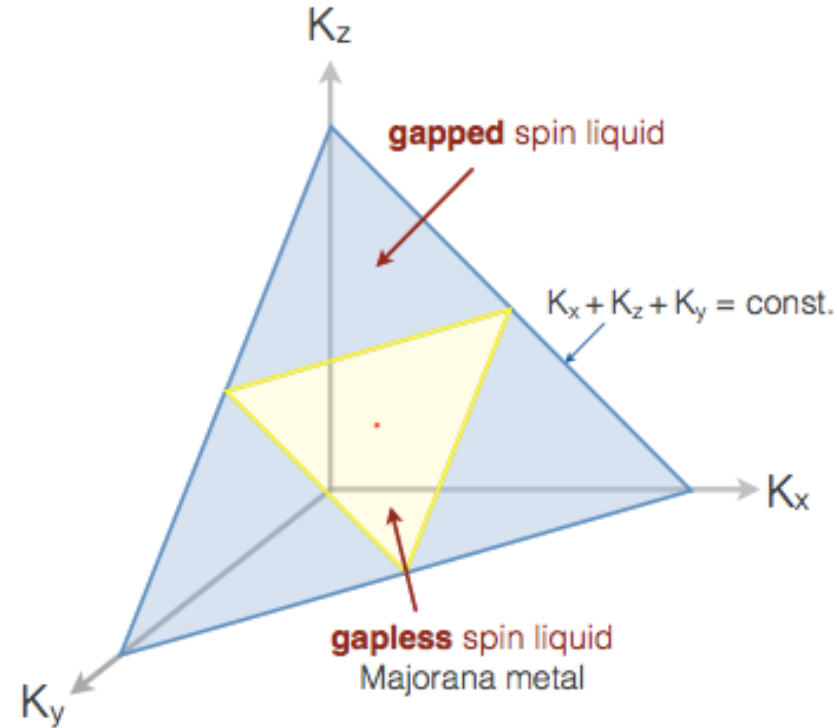
Each many-body eigenstate can  
be labelled by conserved flux  
quanta through each hexagon

# The Kitaev Model on the Honeycomb Lattice

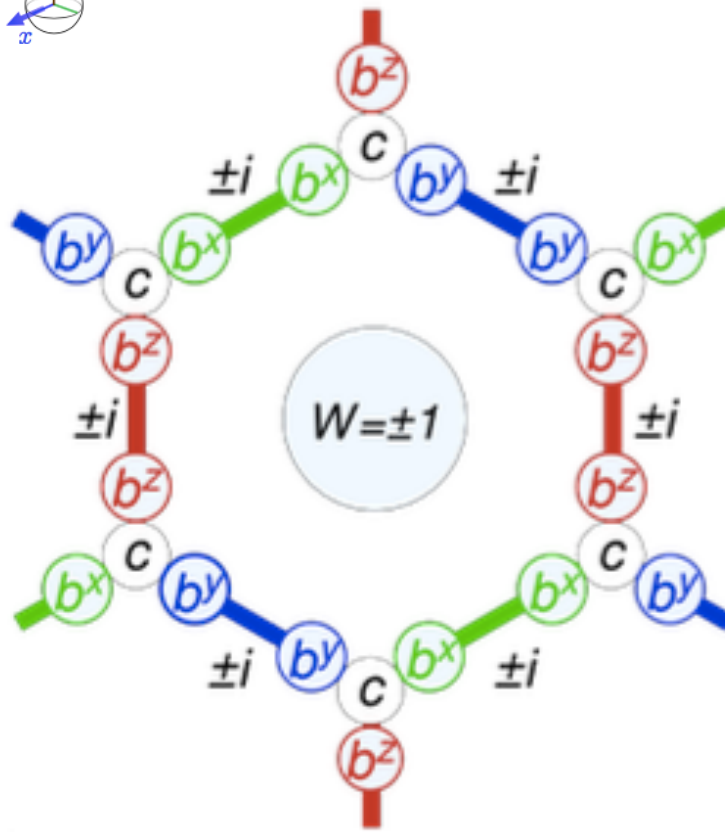
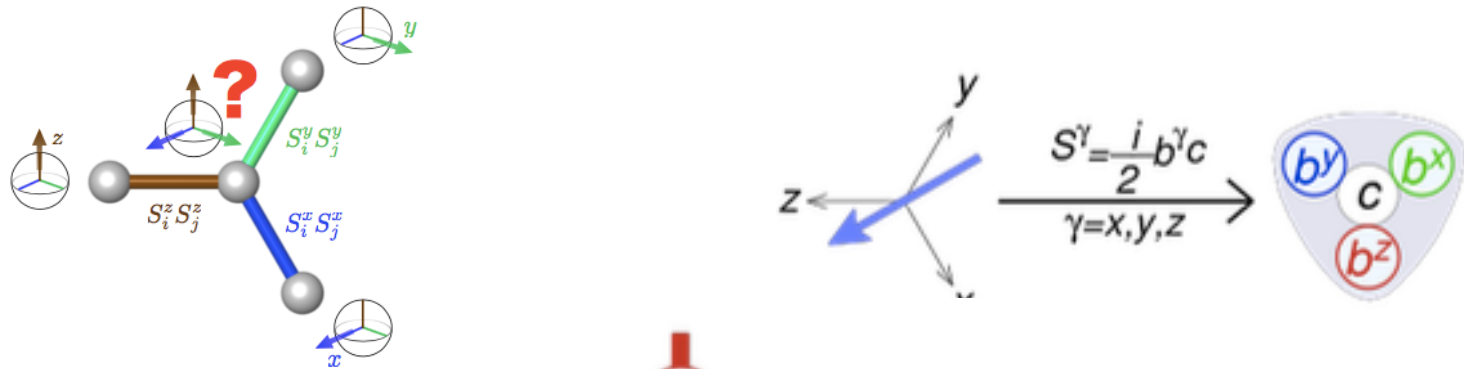


$$H = - \sum_{\langle ij \rangle_\gamma} K_\gamma S_i^\gamma S_j^\gamma$$

Ising Spins with Bond Anisotropies



# The Kitaev Model on the Honeycomb Lattice

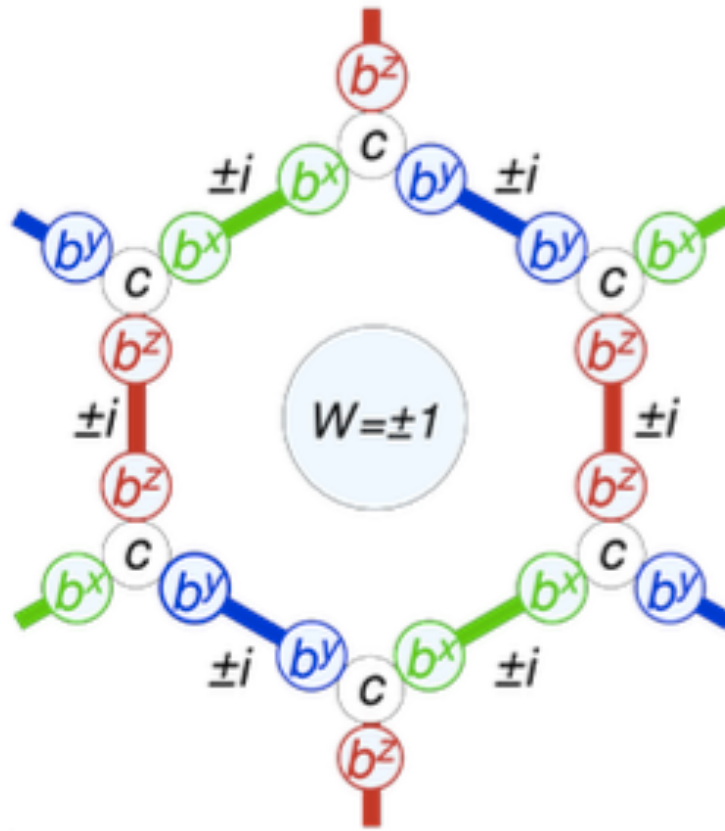




# The Kitaev Model on the Honeycomb Lattice

$$H = -\frac{1}{4} \sum_{\langle ij \rangle_\gamma} K_\gamma u_{ij}^\gamma c_i c_j$$

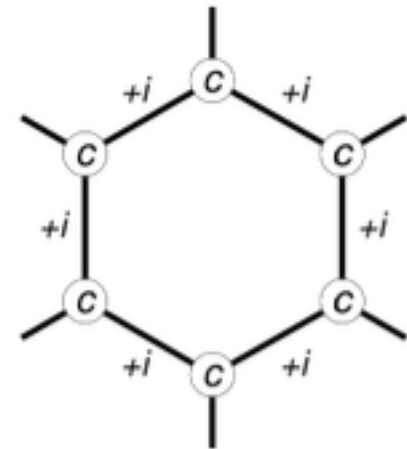
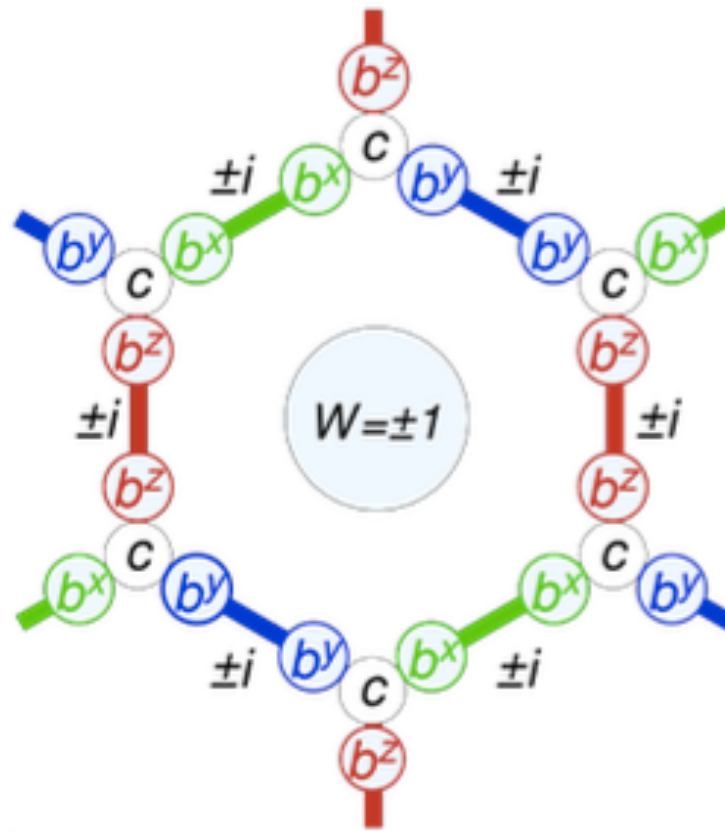
$$(u_{ij}^\gamma = b_i^\gamma b_j^\gamma)$$



# The Kitaev Model on the Honeycomb Lattice

$$H = -\frac{1}{4} \sum_{\langle ij \rangle_\gamma} K_\gamma u_{ij}^\gamma c_i c_j$$

$$(u_{ij}^\gamma = b_i^\gamma b_j^\gamma)$$

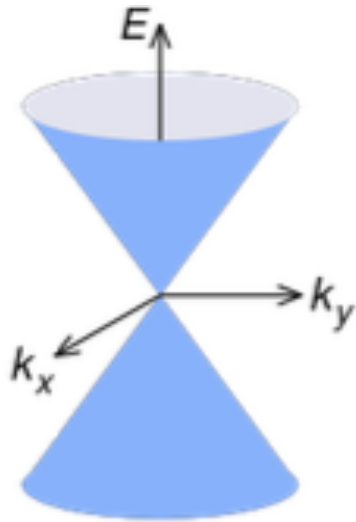


(if  $W = -1$ )

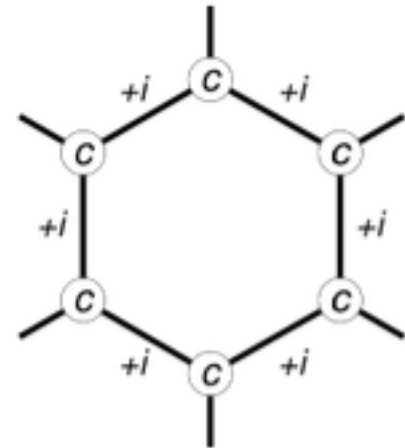
# The Kitaev Model on the Honeycomb Lattice

$$H = -\frac{1}{4} \sum_{\langle ij \rangle_\gamma} K_\gamma u_{ij}^\gamma c_i c_j$$

$$(u_{ij}^\gamma = b_i^\gamma b_j^\gamma)$$

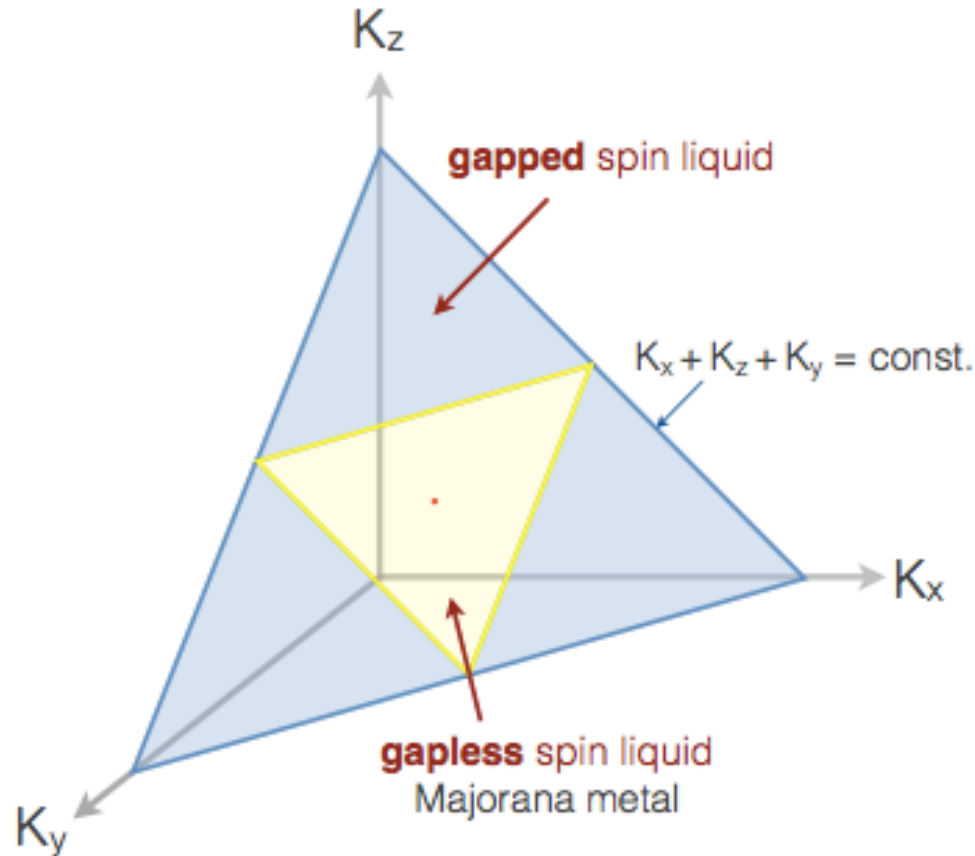


Dirac Dispersion



uniform phase

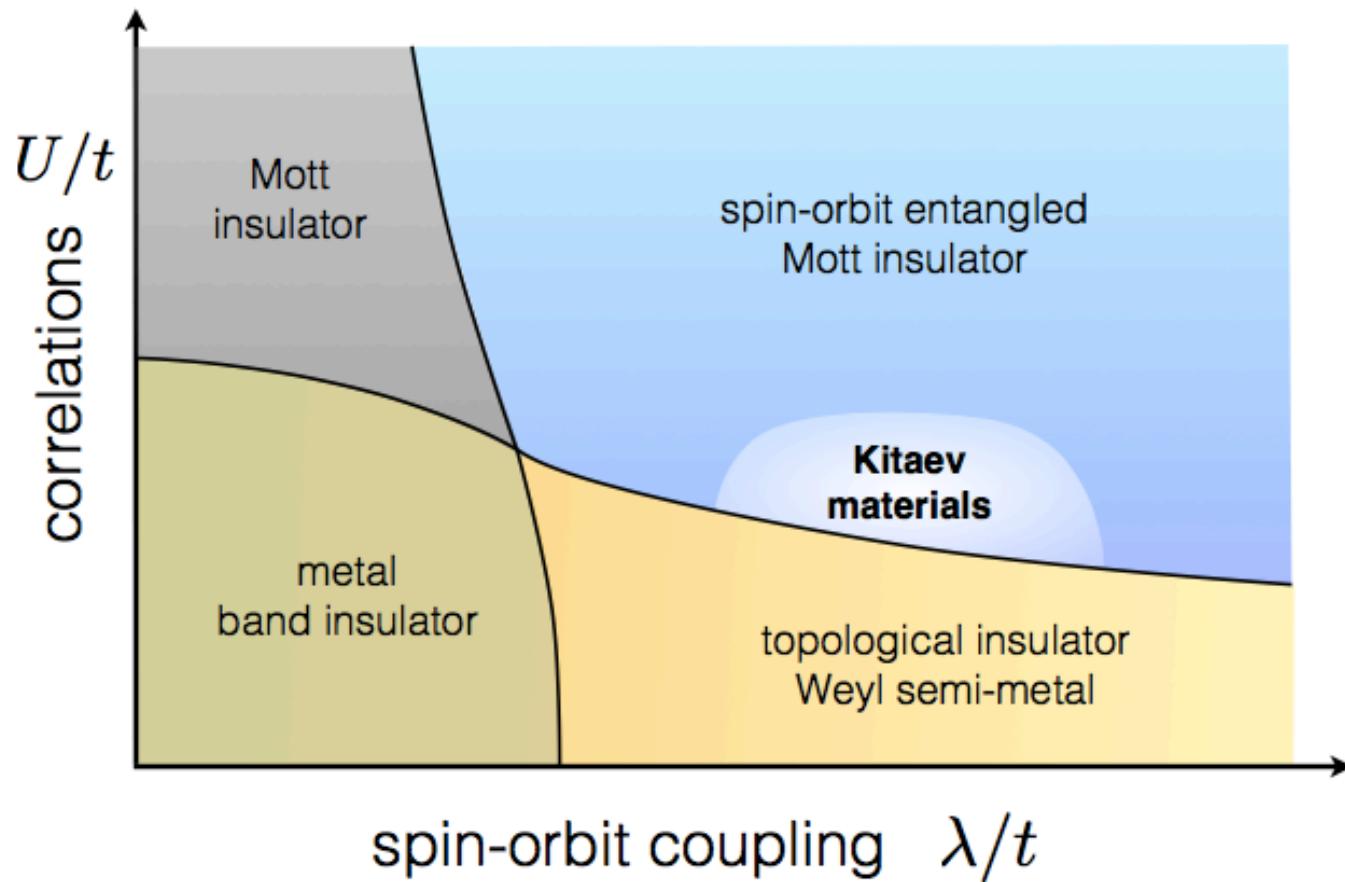
# The Kitaev Model on the Honeycomb Lattice

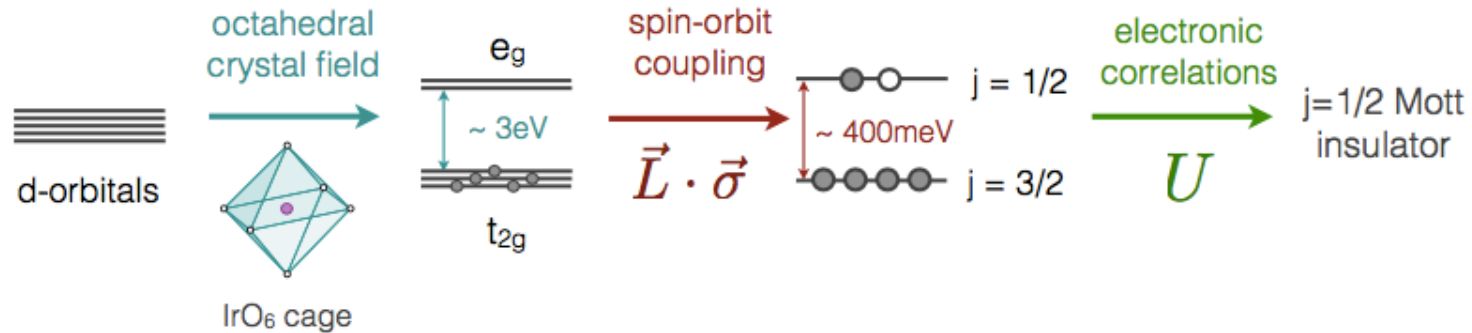


A. Kitaev and C. Laumann, "Topological Phases and Quantum Computation," <https://arxiv.org/pdf/0904.2771.pdf>

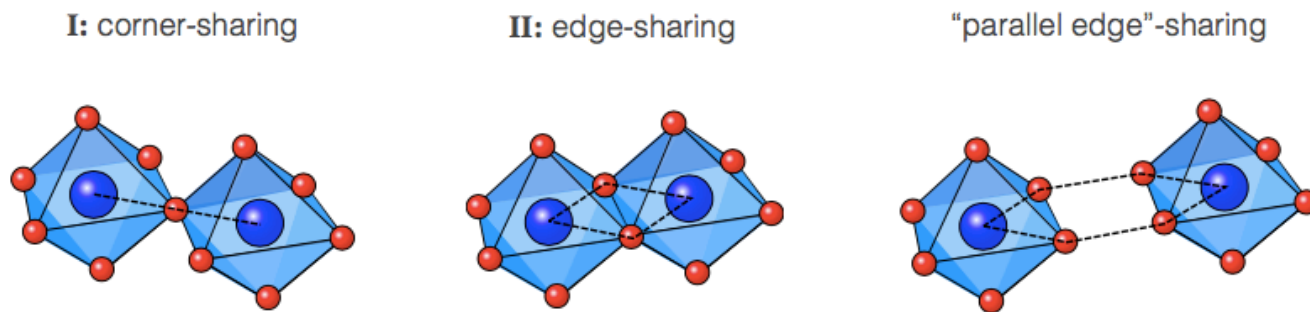


# Kitaev Materials





**Fig. 2:** Formation of spin-orbit entangled  $j = 1/2$  moments for ions in a  $d^5$  electronic configuration such as for the typical iridium valence  $\text{Ir}^{4+}$  or the ruthenium valence  $\text{Ru}^{3+}$ .



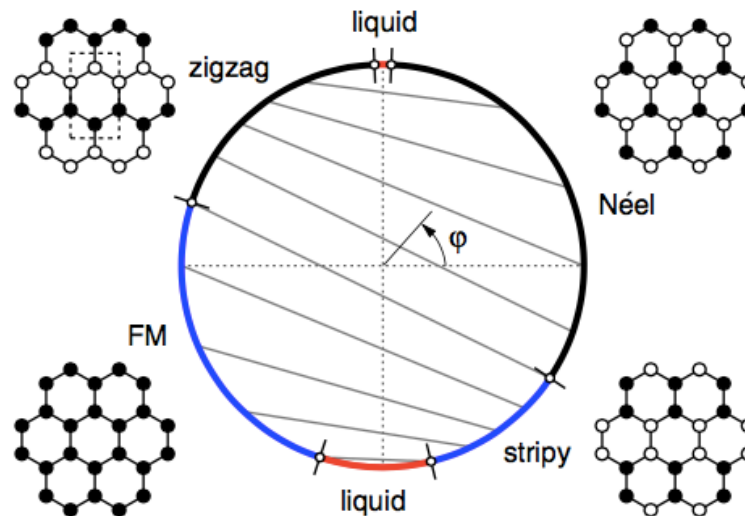
**Fig. 3:** Illustration of possible geometric orientations of neighboring  $\text{IrO}_6$  octahedra that give rise to different types of (dominant) exchange interactions between the magnetic moments located on the iridium ion at the center of these octahedra. For the corner-sharing geometry (I) one finds a dominant symmetric Heisenberg exchange, while for the edge-sharing geometries (II) one finds a dominant bond-directional, Kitaev-type exchange.

Ab Initio Calculations



$$H = - \sum_{\gamma\text{-bonds}} J \mathbf{S}_i \mathbf{S}_j + K S_i^\gamma S_j^\gamma + \Gamma \left( S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha \right)$$

$$J = \cos \phi, \quad K = \sin \phi$$



**Fig. 6:** Phase diagram of the Heisenberg-Kitaev model, reproduced from Ref. [63].