What kinds of OP?

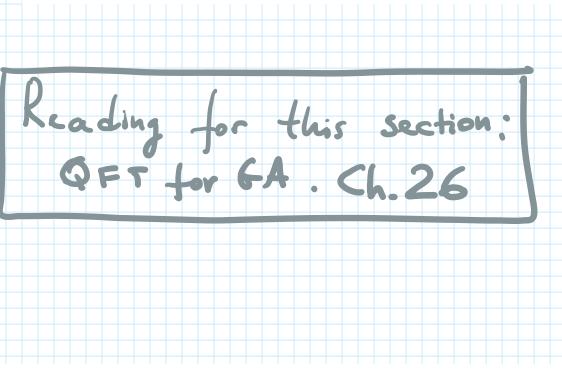
Thursday, September 20, 2018 9:37 AM

OP can be a scalar - periodic charge density in a crystal Vector - Magnetisation in a FM or FE Complex scalar - electron contensate wavefunction in SC - liquid crystels, aniso tropic SC or tensor superfluitity in He or high Te Sc. Symmetries allowed in a physical system trausi tious Topological withou SSB Ginszburg - Landau (SSB) with spontancous symmetry breaking even Ferks in F even + external fields even + odd Q or F dependent terms Complex, x, Lependet phase 1storder 2 st Weak (st order order Gold Store periodically Modulated excitations Structures

What happens when nature breaks symmetry?

Saturday, September 1, 2018 9:10 PM

- Phase transitions We saw that in Landau's example, the parameter a in the free energy was temperature dependent. At a temperature T_c , at which a changes sign, a phase transition takes place. The transition separates two distinct states of different symmetry. The low-temperature phase has lost some symmetry, more precisely it is missing a symmetry element.⁵
- New excitations Our philosophy has been that every particle is an excitation of the vacuum of a system. When a symmetry is broken we end up with a new vacuum (e.g. a vacuum with $M = -M_0$). The fact that the vacuum is different means that the particle spectrum should be expected to be different to that of the unbroken symmetry state (such as M = 0 in our example). We will see that new particles known as Goldstone modes can emerge upon symmetry breaking.⁶
- **Rigidity** Any attempt to deform the field in the broken symmetry state results in new forces emerging. Examples of rigidity include phase stiffness in superconductors, spin stiffness in magnets and the mechanical strength of crystalline solids.
- **Defects** These result from the fact that the symmetry may be broken in different ways in different regions of the system, and are topological in nature. An example is a domain wall in a ferromagnet. These are described in Chapter 29.



Excitation spectrum

Thursday, September 20, 2018 10:00 AM

Recall our approach was to describe condensed matter from the excitation spectrum point of view. Very generally, we can ask What kind of excitations we can expect in a symmetry broken state. Experimentally three are many examples of such excitations . etc. is there any general rule which tells if those excitation really exists? Meet the Goldstone theorem: if at the transition we break <u>a continuous symmetry</u>; there must exist in the ordered state of this material a collective mode or collective excitation with gapless energy spectrum.

But what about Superconductivity?

Do we live in superconducting Universe?

Thursday, September 20, 2018 3:25 PM

In the electro-weak theory of Weinberg-Salam there is a combined U(1) x SU(2) gauge symmetry. Due to coupling to the Higgs field whose symmetry is spontaneously broken one gauge field remains massless (the photon) and the other three become massive. These massive particles are the W+, W-, and Z bosons.

One of the key ideas first emphasized by Phil Anderson in 1963 was that a massless gauge field can acquire a mass in the presence of a coupling to a spontaneously broken field. A concrete realization of this occurs in superconductors. In the Meissner effect a superconductor thicker than the penetration depth expels magnetic fields. This is like the photon acquires a mass.

From <<u>http://condensedconcepts.blogspot.com/2012/07/the-higgs-boson-and-condensed-matter.html</u>>

In a type II superconductor, vortices are allowed in the superconducting order parameter field. Can such vortices occur in the Higgs field? They may have been important in the early universe.

On fascinating thing is that for the Higgs field the crucial ratio [between the London penetration length and the superconducting coherence length] that determines whether type II behavior is possible is the ratio of Higgs boson mass to W mass. The LHC results suggest that type II behavior is possible!

From P. Coleman's book, "Introduction to many-body..." page 246.

Shortly after the importance of this mechanism for relativistic Yang Mills theories was noted by Higgs and Anderson, Weinberg and Salem independently applied the idea to develop the theory of "electro-weak" interactions. According to this picture, the universe we live is a kind of cosmological Meissner phase, formed in the early universe, which excludes the weak force by making the vector bosons which carry it, become massive. It is a remarkable thought that the very same mechanism that causes superconductors to levitate lies at the heart of the weak nuclear force responsible for nuclear fusion inside stars. In trying to discover the Higg's particle, physicists are in effect trying to probe the cosmic superconductor above its gap energy scale.

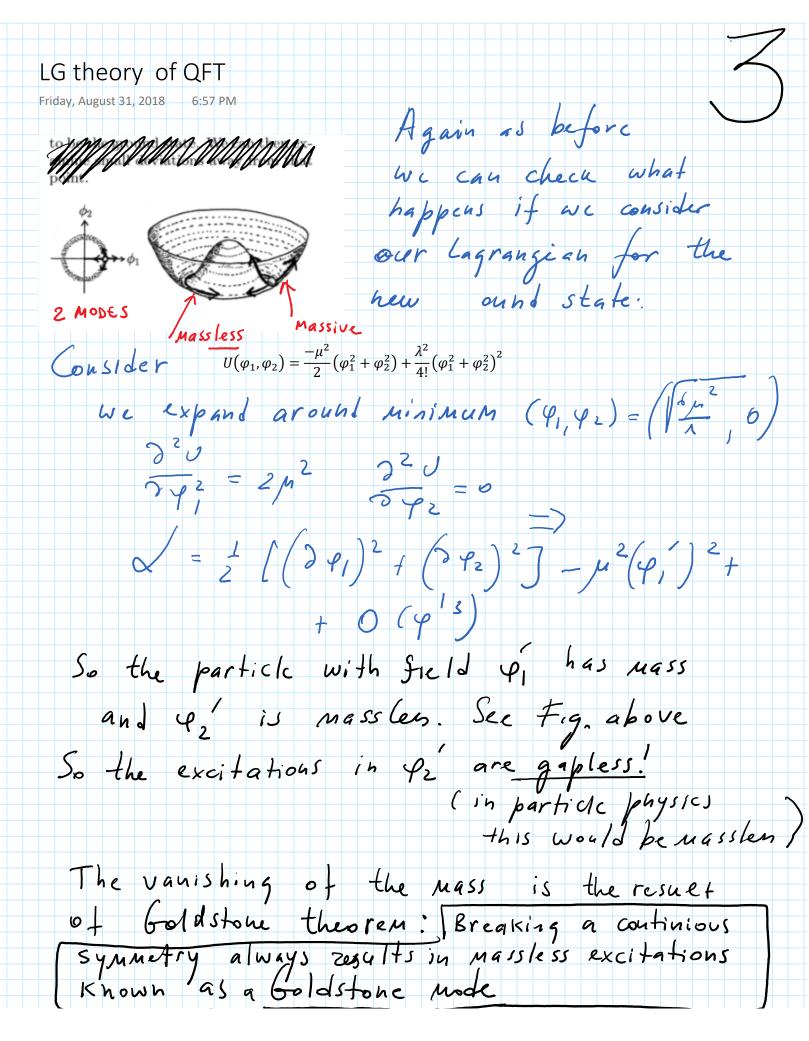
100 µm

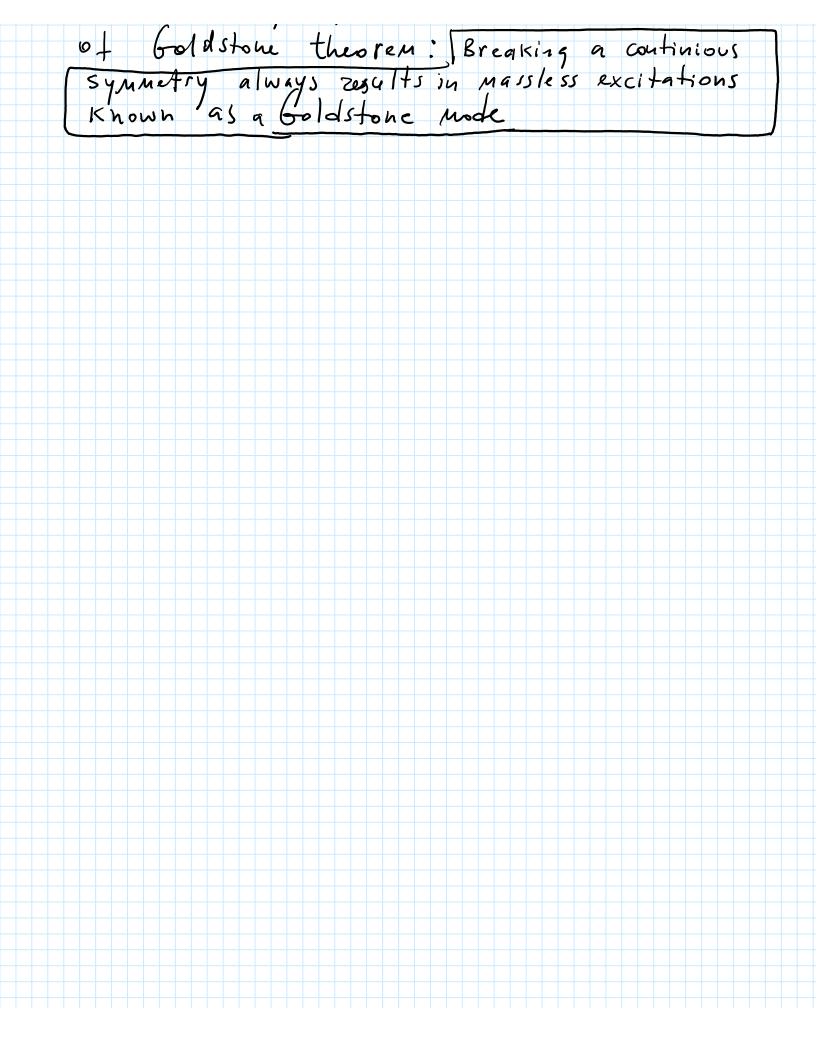
Vortices in a 200nm-thick YBCO film imaged by scanning SQUID microscopy

| LG theory in QFT Friday, August 31, 2018 2:47 PM | | | | | | | | | | | | | | 4 | |
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Field theory and L-6 theory. - Breaking symmetry with Lagrangian. What we do in QFT is searching for a ground state of year) For simplicity lets start with a simple model ! $d = \frac{1}{2} \left(\frac{\partial \mu}{\partial p} \right)^2 - U(\phi) \quad \text{where } U(\phi) = \frac{\mu^2}{2} \phi^2 + \frac{1}{2} \phi^2 + \frac{1}{2} \phi^4$ we move to a very $+ \frac{1}{2} \phi^4$ Now we move to a very interesting case : pizo Viq pr >0 in this case $\frac{2}{2}\varphi = 0 \quad 0 = -\mu^2 \varphi + \frac{1}{3}\varphi^3$ ø (0, ± 6, 1/2 hotice and 20 =0 => - p2 + 20 d -> d if 9-1-9 =0 => => => => => => => == < tor 10=0 = +2 p for p = + V6p 1/A and This is very stronge as our system has two ground stak is brocked hew Vacua and it happens spontaneously What happens to excitations in the new ground state? To investigate this lets select a new vacuum. e.g. + 40, and excite the field around the ground state. The Taylor expansion gives: $U(\varphi - \varphi_0) = U(\varphi_0) + \left(\frac{3U}{3\varphi}\right) |_{\varphi_0} (\varphi - \varphi_0) +$ $+\frac{1}{2!}\frac{\partial\varphi_{2}}{\partial\varphi_{2}}\left|\varphi_{0}\left(\varphi-\varphi_{0}\right)^{2}+\cdots\right|=$ $= \frac{U(\varphi_0)}{Const} + \mu^2 (\varphi - \varphi_0)^2 + \dots$ = ϕ' The final Lagrangian is : $\Delta = \frac{1}{2} (2 \varphi')^2 - \mu^2 \varphi'^2 + O(\varphi'^3)$ less compare this to the original theory L= { (24) - 2 4 + 1 4' > p + TZp Notice, the Lagrangian donit break the symmetry, it is Still & >-p invariant But the symmetry is braken in the ground stak. As the result, the vacuum gets a non-zero amplitude $\gamma_0 = \left(\frac{\delta_{\mu}^2}{\lambda}\right)^{1/2}$ and becomes heavier.

LG theory in QFT Friday, August 31, 2018 2:58 PM Modes Goldstone Consider a 2-component QFT: $\alpha = \frac{1}{2} \left(\frac{\partial_{\mu} \varphi_{j}}{\partial_{\mu}} + \frac{\partial_{\mu} \varphi_{z}}{\partial_{\mu}} \right) + \frac{\mu^{2}}{2} \left(\frac{\varphi_{z}}{\varphi_{z}} + \frac{\varphi_{z}^{2}}{\varphi_{z}} \right)$ $\frac{1}{4!} \left(\varphi_1^2 + \varphi_2^2 \right)^2 \leftarrow it has SO(2) symmetry$ around internal q1(x) - q2(x) There are infinite number & of local minima. $U(x) = -\frac{\mu^2}{2}x + \frac{1}{\sqrt{1}}x^2$ Fig. 26.6 (a) The potential for the SO(2) symmetry breaking looks like the bottom of a punted wine bottle. $\chi = \varphi_1^2 + \varphi_2^2 = 2 = 2 = 2 = 2$ (b) There is a maximum at the point $\phi_1 = \phi_2 = 0$, but surrounding this there is a set of minima which lie on a circle. (c) The circle of minima are shown on a ϕ_1 - ϕ_2 plot (this is therefore q1+ q2 = 6/2/1 viewing the surface sketched in (b) from 'above'). The symmetry can then be broken by choosing a particular point in the circle of minima and setting this to be the ground state. We can then ex-Lets imagine we break symmetry amine small deviations away from that point. $(q, q_2) = (+ | q_1 | q_2) = (+ | q_1 | q_2)$ and invenstigate the excitations around the ground state. $\varphi_{1} = \varphi_{1} - \frac{1}{4} \frac{1}{4} \frac{1}{4} = \varphi_{2}$ See next figure to get a better idea.



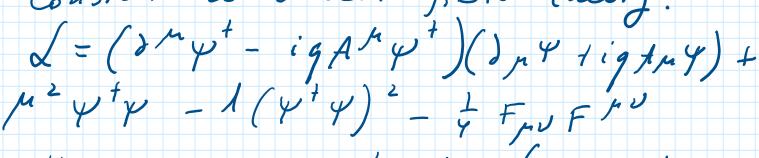


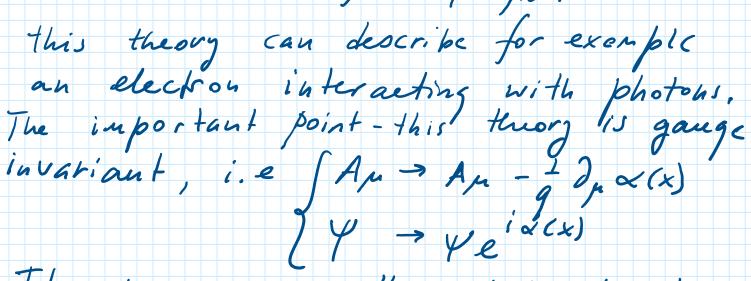
Breaking symmetry in a gauge theory

The most amazing effect occur when we apply the same ideas to the broken ground state in a gauge theory.

Here we want to discuss the

fanous Higgs Mechanism. Consider a scalar field theory:





The throng as written above describes

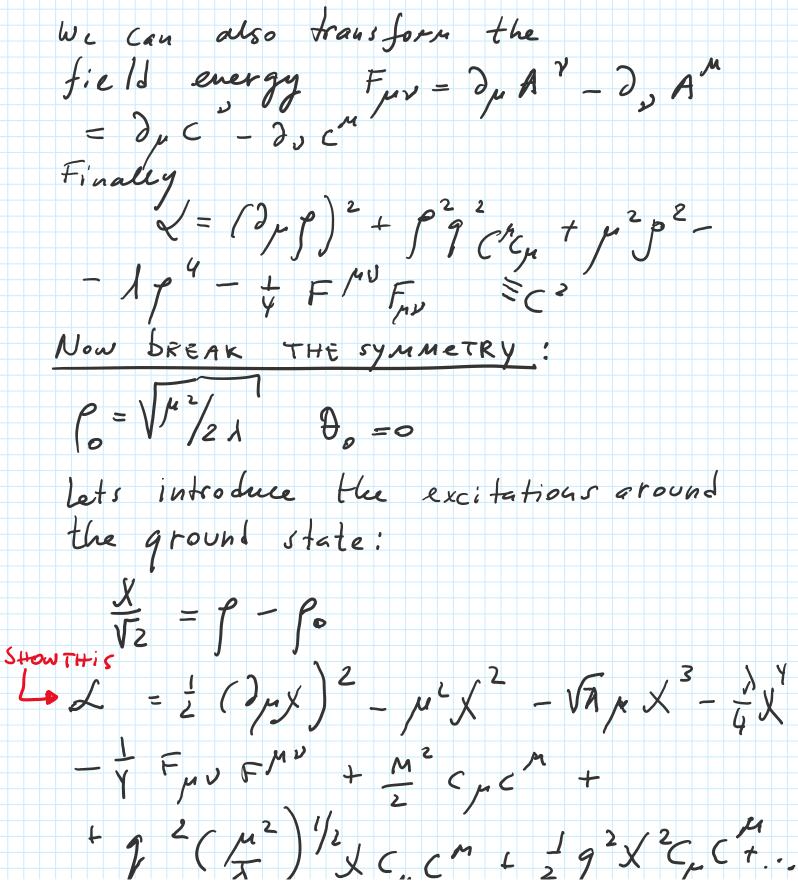
2 massive scalar particle $E_p = (p^2 + M^2)^{1/2}$ and



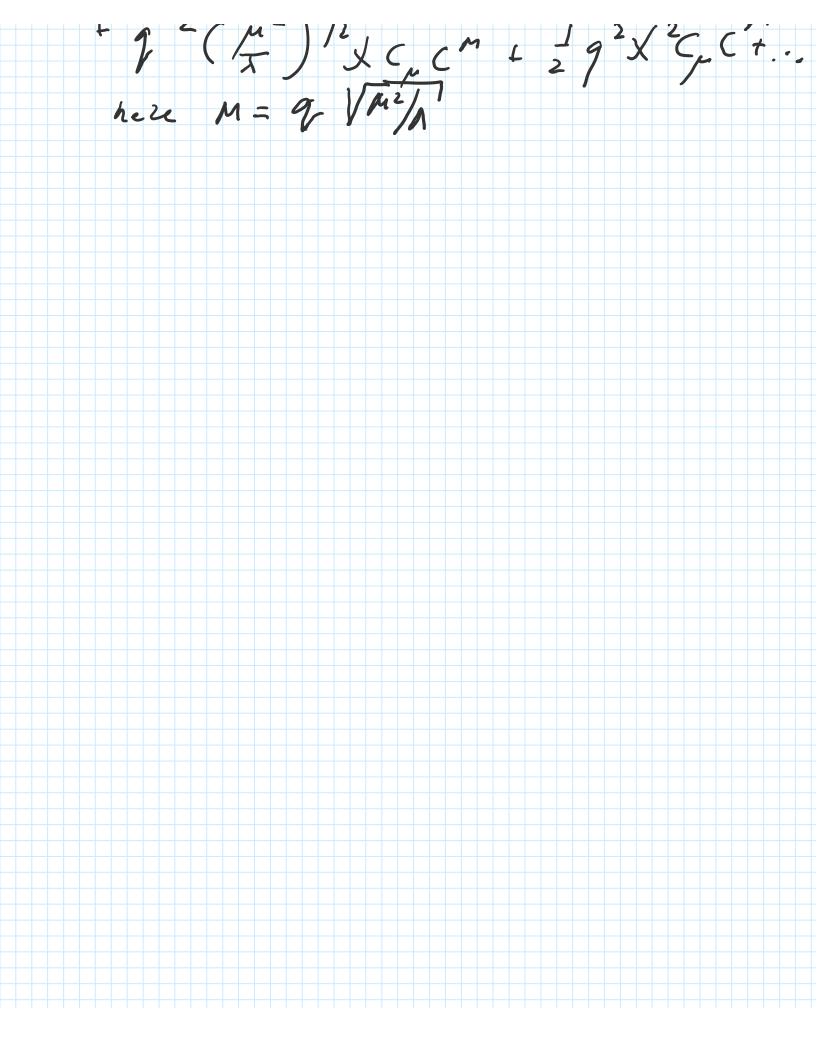
Higgs Anderson mechanism Monday, September 3, 2018 Nonday, September 3, 2018 10:54 AM Now we will break the square try Lets more to the polar coordinates: $i\Theta(x)$ $\Psi(x) = f(x) l$ and select some unique $angle \Theta_0$ for all x. 10:54 AM So we seat at this specific state and want to know what excitations can encrye around this state? $\partial_{\mu} \Psi + i q A_{\mu} \Psi = (\partial_{\mu} \rho cx) \ell^{i\Theta(x)} +$ $+i(\partial_{\mu}\vartheta(x)\rho e^{i\vartheta} + qA_{\mu}\rho e^{i\vartheta} = (\partial_{\mu}\vartheta)e^{i\vartheta} + i\rho e^{i\vartheta}(\partial_{\mu}\vartheta + qA_{\mu})$ Compare to (dug + ig Any) we introduce a new gauge field $\mu + i \eta A_{\mu} + \frac{1}{\eta} \partial_{\mu} \Theta \equiv C_{\mu}$ So the term $(\partial \mu \psi^{\dagger} - iq A^{\mu} \psi^{\dagger}) (\partial_{\mu} \psi - iq A_{\mu} \psi) =$ = $(\partial_{\mu} \rho)^{2} + \rho^{2} q^{2} C_{\mu} C^{\mu} + SHow THis$

Higgs Anderson Mechanism

Monday, September 3, 2018 11:03 AM



Order parameter Page 13



Higgs Anderson Mechanism

Monday, September 3, 2018 11:10 AM

Now we see that we have X field excitations with mass Ven But CM which was massless gauge field analog of An now has mass M. Also & which was marsles how is Not in the Theory and we instead have a massive term CM the massless photon field Ap has eaten O(x) and got mass Cp (x) So we have: $\chi_{x1} \in p = (p^2 + (V_2 p)^2)^{1/2}$ t 3 Vector fields $C_{\mu}(x) = \sum_{p=1}^{p} \frac{q^{2}}{(q^{2})} \frac{1}{2}$ Summary: By applying a gauge transformation

