What kinds of OP?

Thursday, September 20, 2018 9:37 AM

Of can be a scalar - periodic charge density in a crystal<br>vector - uagnetisation in a FM or FE<br>Couplex scalar - electron condensate vavefunction in SC - liquid crystals, ansotropic SC or teusor superfluitity in the or high  $T_c$  Sc. Synnetries allowed in a physical system *<u><u>Arausi</u>* frous</u> Topological<br>withou SSB Ginszburg - Landau (SSB)<br>with spontaneous symmetry breaking even Germs in F  $even + odd$ q or F<br>dependent<br>terms even + external fields Complex, xm<br>dependet phase  $\frac{1}{1}$  or der  $\overline{z}$ order  $\frac{st}{1}$  Weak  $\frac{st}{1}$  order  $G<sub>o</sub>/J$  stone periodically<br>Modulated *Rxcitctions* Structures

## What happens when nature breaks symmetry ?

Saturday, September 1, 2018 9:10 PM

- Phase transitions We saw that in Landau's example, the parameter  $a$  in the free energy was temperature dependent. At a temperature  $T_c$ , at which a changes sign, a phase transition takes place. The transition separates two distinct states of different symmetry. The low-temperature phase has lost some symmetry, more precisely it is missing a symmetry element.<sup>5</sup>
- New excitations Our philosophy has been that every particle is an excitation of the vacuum of a system. When a symmetry is broken we end up with a new vacuum (e.g. a vacuum with  $M = -M_0$ ). The fact that the vacuum is different means that the particle spectrum should be expected to be different to that of the unbroken symmetry state (such as  $M = 0$  in our example). We will see that new particles known as Goldstone modes can emerge upon symmetry breaking.<sup>6</sup>
- Rigidity Any attempt to deform the field in the broken symmetry state results in new forces emerging. Examples of rigidity include phase stiffness in superconductors, spin stiffness in magnets and the mechanical strength of crystalline solids.
- Defects These result from the fact that the symmetry may be broken in different ways in different regions of the system, and are topological in nature. An example is a domain wall in a ferromagnet. These are described in Chapter 29.



### Excitation spectrum

Thursday, September 20, 2018 10:00 AM

Recall our approach was to describe condensed metter from the excitation spectrum point of view. Very generally, we can ase Twhat kind of excitations  $Ex$  perimentally there are using examples of such  $exch$  tations  $exchation$ <br>  $- isotropic ferrouqget with solving  
\n $etc.\int$  with acoorfc phonsu  
\n $\omega$$ is there any general rule which tells  $if$  those excitation eally exists? Meet the 6-1d stone theoren: if at the transition we break a continuous symmetry, there rust exist in the ordered state of this naterial a collective mode or collective excitation with gapless energy spectrum.

But what about Superconductivity?

# Do we live in superconducting Universe ?

Thursday, September 20, 2018 3:25 PM

In the electro-weak theory of Weinberg-Salam there is a combined U(1) x SU(2) gauge symmetry. Due to coupling to the Higgs field whose symmetry is spontaneously broken one gauge field remains massless (the photon) and the other three become massive. These massive particles are the W+, W-, and Z bosons.

One of the key ideas first emphasized by Phil Anderson in 1963 was that a massless gauge field can acquire a mass in the presence of a coupling to a spontaneously broken field. A concrete realization of this occurs in superconductors. In the Meissner effect a superconductor thicker than the penetration depth expels magnetic fields. This is like the photon acquires a mass.

From <<http://condensedconcepts.blogspot.com/2012/07/the-higgs-boson-and-condensed-matter.html>>

In a type II superconductor, vortices are allowed in the superconducting order parameter field. **Can such vortices occur in the Higgs field?** They may have been important in the early universe.

On fascinating thing is that for the Higgs field the crucial ratio [between the London penetration length and the superconducting coherence length] that determines whether type II behavior is possible is the ratio of Higgs boson mass to W mass. The **LHC results suggest that type II behavior is possible!**

#### From P. Coleman's book, "Introduction to many-body..." page 246.

Shortly after the importance of this mechanism for relativistic Yang Mills theories was noted by Higgs and Anderson, Weinberg and Salem independently applied the idea to develop the theory of "electro-weak" interactions. According to this picture, the universe we live is a kind of cosmological Meissner phase, formed in the early universe, which excludes the weak force by making the vector bosons which carry it, become massive. It is a remarkable thought that the very same mechanism that causes superconductors to levitate lies at the heart of the weak nuclear force responsible for nuclear fusion inside stars. In trying to discover the Higg's particle, physicists are in effect trying to probe the cosmic superconductor above its gap energy scale.



Vortices in a 200 nm-thick YBCO film imaged by scanning SQUID microscopy



Field theory and L-6 theory. - Breaking symmetry with Lagrangian. What we do in PFT is searching for a ground state of  $\varphi$  (x) For simplicity lets start with a simple no del :  $\alpha' = \frac{1}{2} (P\mu \phi)^2 - U(\phi)$  where  $C(\phi) = \frac{\mu^2}{2} \phi^2 +$ <br>we move to a very  $\frac{1}{2} \frac{1}{2} \phi^2$ Now we nove to a very interesting case:  $\mu^2 \omega$  $|U(\varphi)|$  $\mu^2$ > in this case  $\frac{36}{99}$  = 0 = - $\frac{1}{9}$  +  $\frac{1}{51}$   $\frac{1}{9}$ ø  $(0, 160)$ hotice and  $\frac{3^{2}U}{2V^{2}}=0 = 2-\mu^{2}+\frac{1}{2}\phi^{2}$  $d \rightarrow d$  $49 - 49$  $= 0$  =>  $\frac{34}{86}$  $f^2 \mu^2$  for  $\phi = \pm \sqrt{6 \mu^2/\pi}$ an d This is very stronge as our system has two hew vacua ground stak is <u>brockey</u> and it happens spontaneously What happers to excitations in the new To investigate this lets select a new vacuum.<br>e.g. +40, and excite the field around<br>the ground state. The Taylor expansion gives:  $U(\varphi-\varphi_{o}) = U(\varphi_{o}) + (\frac{\partial U}{\partial \varphi})|_{\varphi_{o}} (\varphi-\varphi_{o}) +$  $+\frac{1}{2!} \frac{3^{2}0}{24^{2}}|_{\rho_{b}} (\varphi - \varphi_{o})^{2} + ...$ =  $U(\varphi_0) + \mu^2 (\varphi - \varphi_0)^2 + ...$ <br>Const  $\varphi'$ The final Lagrangian is:  $d = \frac{1}{2} (2 \varphi)^2 - \mu^2 \varphi'^2 + O(\varphi'^3)$ Lets coupare this to the original theory  $\alpha = \frac{1}{2} (2\gamma)^2 - \frac{\mu^2}{2} \gamma^2 + \frac{\lambda}{2!} \gamma^3$  $\rightarrow$   $\mu \rightarrow$   $\pi \mu$ Notice, the Lagrancian don't brook<br>the symmetry, it's  $\frac{1}{2}$  till  $\frac{1}{4}$   $\$ amplitude  $\varphi_o = \left(\frac{6\mu^2}{4}\right)^{1/2}$ and becomes<br>heavier.

LG theory in QFT Friday, August 31, 2018 2:58 PM Modes Goldstone Consider a 2-component QFT:  $\alpha = \frac{1}{2} (2\mu \varphi_1)^2 + (2\mu \varphi_2)^2 + \frac{\mu^2}{2} (\varphi_1^2 + \varphi_2^2)$  $\frac{1}{4!}(\varphi_{1}^{2}+\varphi_{2}^{2})^{2}$   $\leftarrow$  it has SO(2) symmetry around internal  $\varphi_1(x) - \varphi_2(x)$ There are infinite number  $U(x) = -\frac{\mu^2}{2}x + \frac{\lambda^2}{yT}x^2$ Fig. 26.6 (a) The potential for the  $SO(2)$  symmetry breaking looks like the bottom of a punted wine bottle.  $x = \varphi_1^2 + \varphi_2^2 \implies \frac{\partial u}{\partial x} = 0 \implies$ (b) There is a maximum at the point  $\phi_1 = \phi_2 = 0$ , but surrounding this there is a set of minima which lie on a circle. (c) The circle of minima are shown on a  $\phi_1$ - $\phi_2$  plot (this is therefore  $\varphi_1^2 + \varphi_2^2 = 6\mu^2/1$ viewing the surface sketched in (b) from 'above'). The symmetry can then be broken by choosing a particular point in the circle of minima and setting this to be the ground state. We can then ex-Lets inagine we break symmetry amine small deviations away from that  $f(x,y)=(1-\frac{1}{2})^{2}$ and invenstigate the excitations around the<br>ground state.<br> $\varphi_1 = \varphi_1 - \sqrt{6\mu^2/2}$  $\varphi_{1}^{\prime} = \varphi_{1} - \sqrt{6\mu_{A}^{2}} \qquad \varphi_{2}^{\prime} = \varphi_{L}$ See next figure to get a better idea.



Order parameter Page 8



# Breaking symmetry in a gauge theory

The most amazing effect occur when we apply the same ideas to the broken ground state in a gauge theory.

Here we want to discuss the

famous Higgs mechanism.<br>Consider a scalar field theory:

 $\alpha = (\partial^{\mu}\psi^{+} - igA^{\mu}\psi^{+})(\partial_{\mu}\psi + igA_{\mu}\psi) +$ <br> $\mu^{2}\psi^{+}\psi - \lambda(\psi^{+}\psi)^{2} - \frac{1}{\gamma}F_{\mu\nu}F^{\mu\nu}$ 

this theory can describe for exemple<br>an electron interacting with photons,<br>The important point-this theory is gauge<br>invariant, i.e  $\int A_{\mu} \rightarrow A_{\mu} - \frac{1}{2} \partial_{\mu} \propto x$ )

The Huory as written above describes

2 *massive* scalar particle<br>Ep = (p<sup>2</sup>+ M<sup>2</sup>) 1/2 and



Higgs Anderson mechanism Monday, september 3, 2018 10:54 AM<br>
Now we will break the squiretry<br>
Lets nove to the polar coordinates:<br>  $\psi(x) = \rho(x) e^{i \theta(x)}$  and select some unique<br>
angle  $\theta_o$  for all x. So we seat at this specific state and want to know what excitations<br>can encrye around this state?  $\partial_{\mu}\psi + i\gamma A_{\mu}\psi = (\partial_{\mu}\rho c x) e^{i\Theta c x} +$  $f'(0\mu\theta(x))$  =  $(0\mu f)e^{i\theta} + i\int e^{i\theta}e^{i\theta} =$ <br>=  $(0\mu f)e^{i\theta} + i\int e^{i\theta}e^{i\theta} + 1\mu\theta$ Compare to (due +ig Aux) we introduce a new gauge  $f_{rel}(\frac{3\mu}{\mu} + i\gamma A\mu)$  $(2)^n y^{\dagger} - i y A^{\dagger} y^{\dagger}$  (  $2\mu y - i y A_{\mu}\nu$ ) =<br>=  $(2\mu p)^{\dagger}z + p^2 y^2$   $C_{\mu}C^{\mu}$  + SHow THIS

## Higgs Anderson Mechanism

Monday, September 3, 2018 11:03 AM<br>We Can also transform the<br>field energy  $F_{\mu\nu} = \partial_{\mu} A^{\nu} - \partial_{\nu} A^{\mu}$ <br>=  $\partial_{\mu} C - \partial_{\nu} C^{\mu}$ Finally  $-\lambda y=(\frac{3}{4}y)^{2}+ \int_{\frac{3}{4}y}^{2}(\frac{1}{4}y+\frac{3}{4}z)^{2}-$ Now BREAK THE SYMMETRY:  $\int_{0}^{\infty}=\sqrt{\frac{\mu^{2}}{2}}\int_{0}^{\infty}1\quad\theta_{0}=0$ Lets introduce the excitations around<br>the ground state:  $\frac{y}{\sqrt{2}} = \int - \int_{2}$  $\frac{1}{4}x^2 = \frac{1}{2}(2\mu x)^2 - \mu^2 x^2 - \sqrt{4}x x^3 - \frac{\lambda}{4}x^4$  $-\frac{1}{\gamma}F_{\mu\nu}F^{\mu\nu} + \frac{m^{2}}{2}C_{\mu}c^{\mu} +$ +  $2^2(\mu^2)^{1/2}$   $\sqrt{c}$   $\mu$   $\mu$   $\frac{1}{2}$   $g^2$   $\sqrt{c}$   $c^2$ 



# Higgs Anderson Mechanism

Monday, September 3, 2018 | 11:10 AM

Now we see that we have & field excitations with mass VzM But C<sup>M</sup> which was nessless gauge field analog of Ap now<br>has nass M. Also & which was naisles<br>how is Not in the Y theory<br>and we instead have a nassive<br>term CM the messless photos field Ap has<br>eaten O(x) and got mass  $C_p$  (x) So we have.  $X(t)$   $\in$   $p = (p^2 + (p^2)^2)^{1/2}$ +<br>3 Vector fields<br> $C_{\mu}(x)$   $E_{\mu} = \left[ \mu + \left( \frac{q^{2} \mu^{2}}{\lambda} \right) \right]$  //2<br>Sammary: By applying a gauge freustornation

